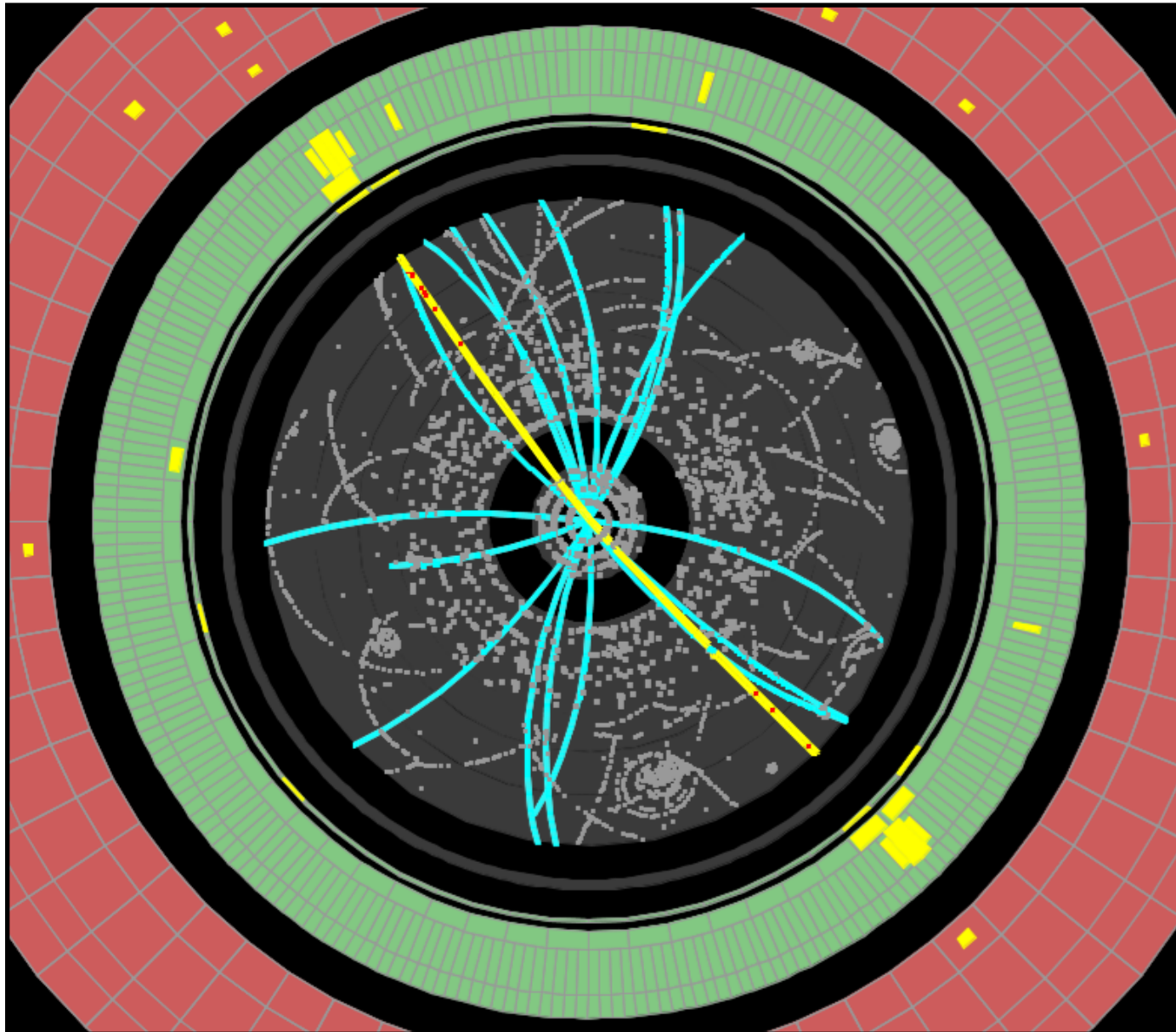


Experimental High Energy Physics at Colliders

Lecture 1: Experiments & Accelerators



Z \rightarrow ee Candidate
[September 2010]

Toni Baroncelli
INFN RomaTRE

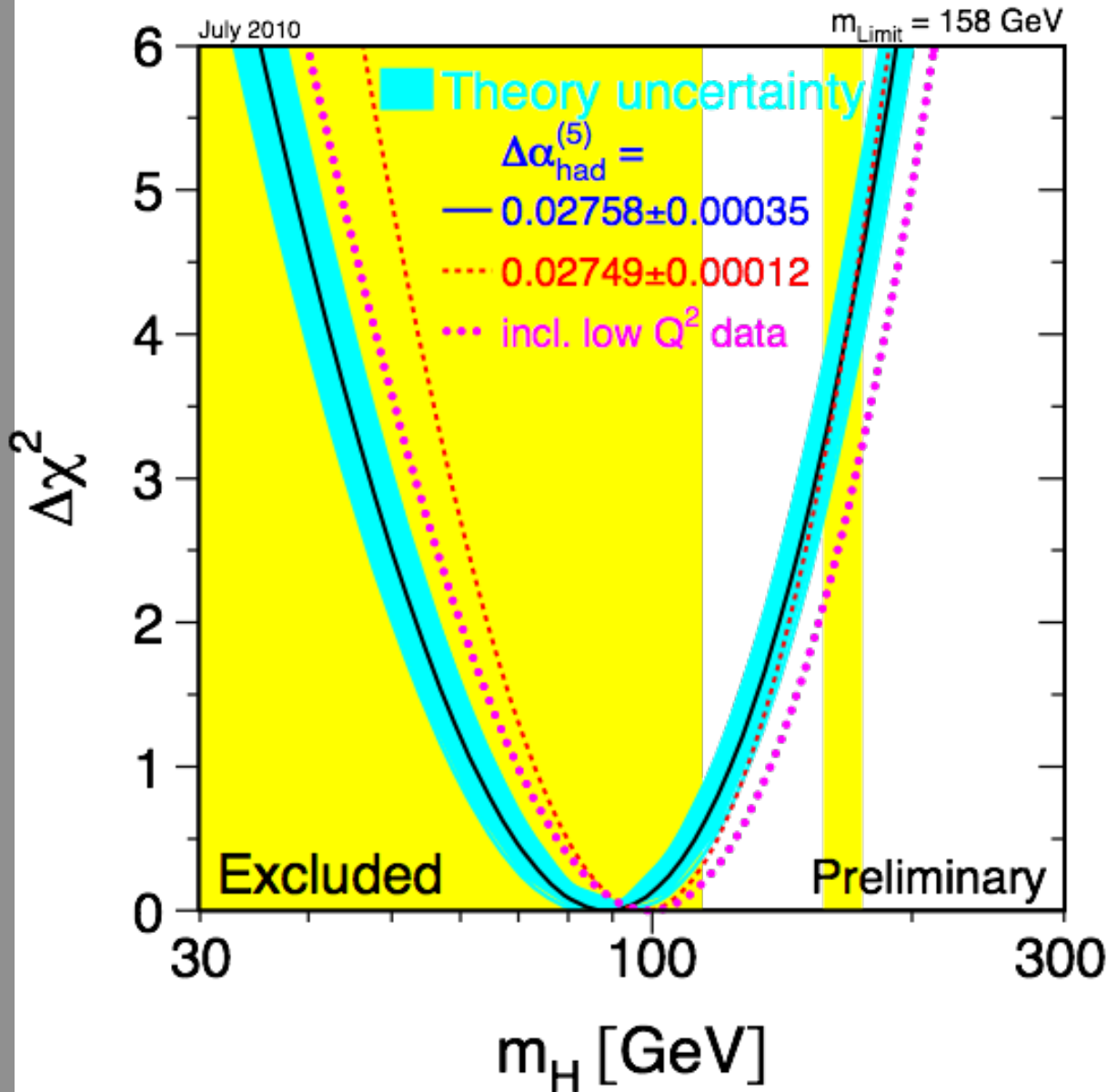
Hans-Christian Schultz-Coulon
Kirchhoff-Institut für Physik

Introduction & Motivation

The LHC and its Experiments



Our Knowledge about the Higgs before its discovery



EW-Fits:

$$M_H = 89 \quad \text{GeV}$$

$$M_H < 158 \text{ GeV} @ 95\% \text{ CL}$$

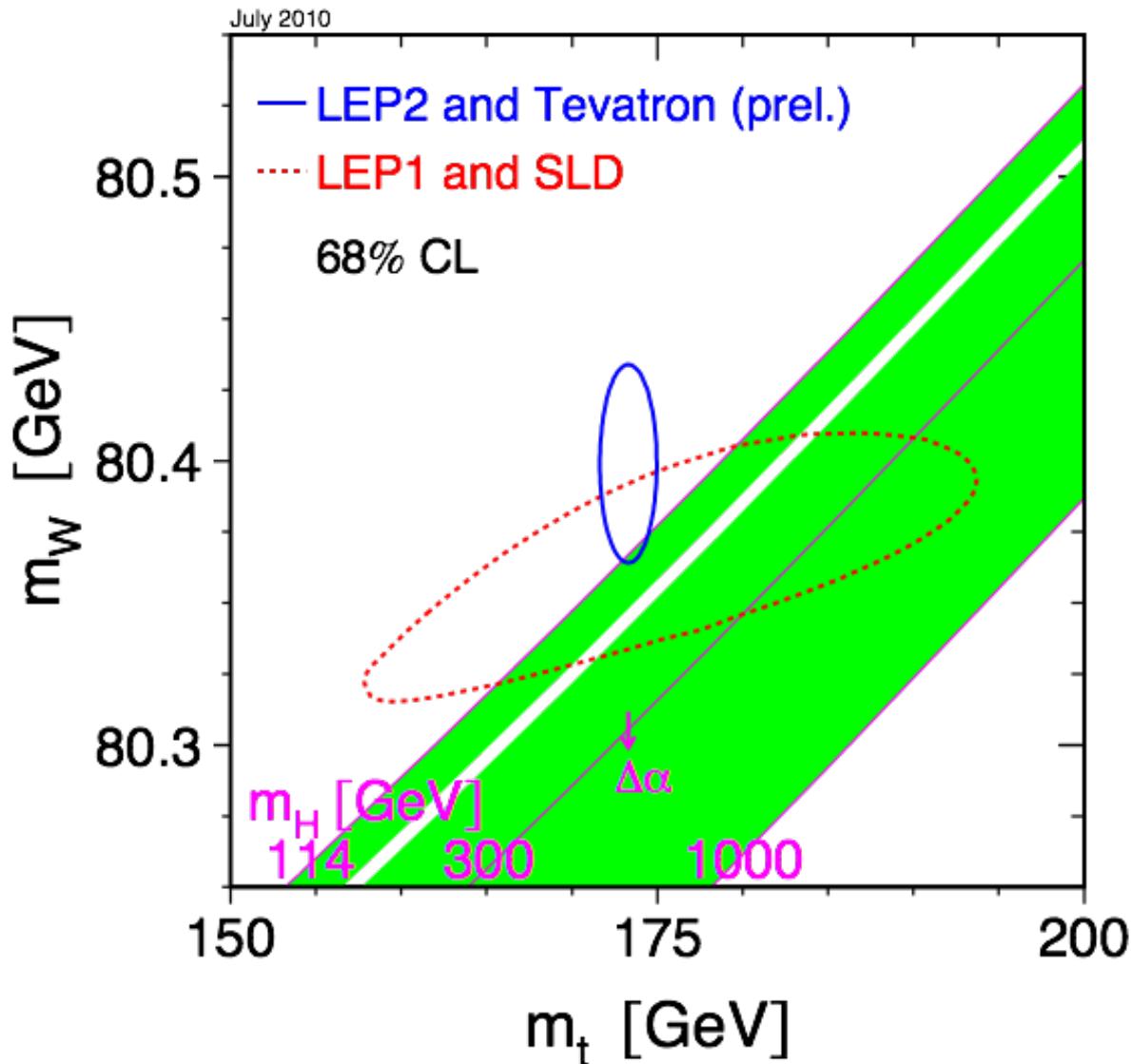
From direct
search at LEP:

$$M_H > 114 \text{ GeV} @ 95\% \text{ CL}$$

From direct
search at Tevatron:

$$158 < M_H < 175 \text{ GeV} @ 95\% \text{ CL}$$

Our Knowledge about the Higgs before its discovery



EW-Fits:

$$M_H = 89^{+35}_{-26} \text{ GeV}$$

$$M_H < 158 \text{ GeV @ 95\% CL}$$

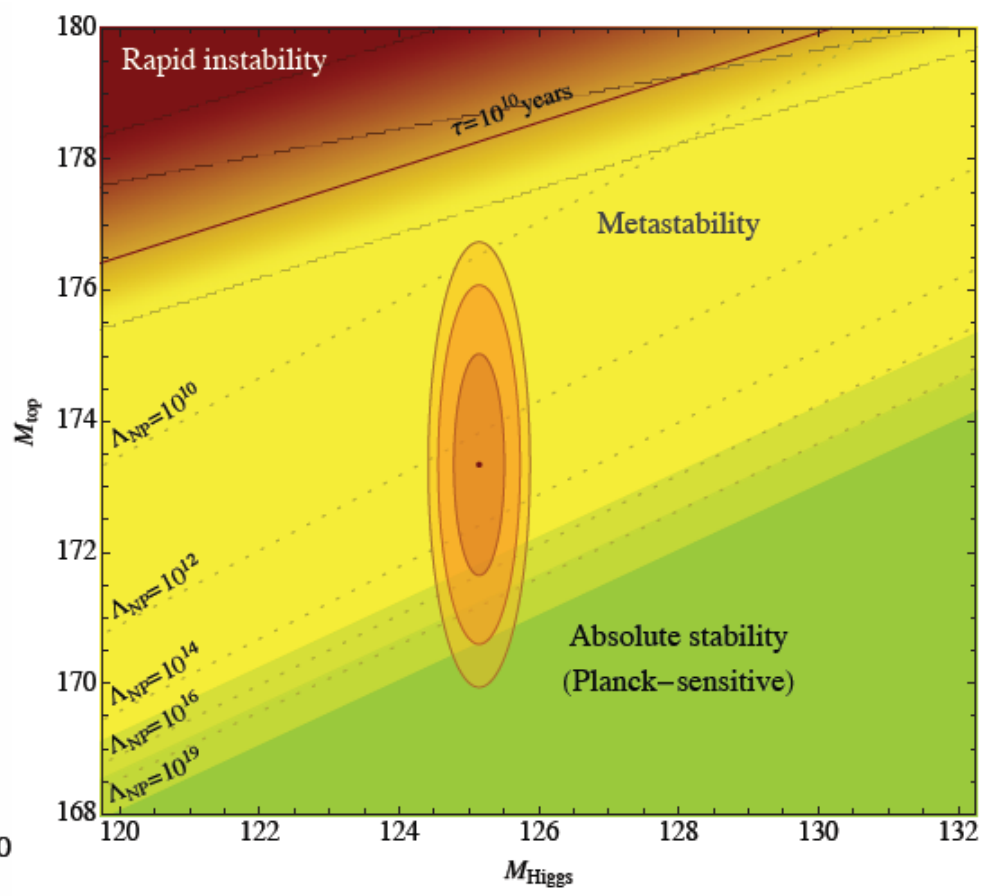
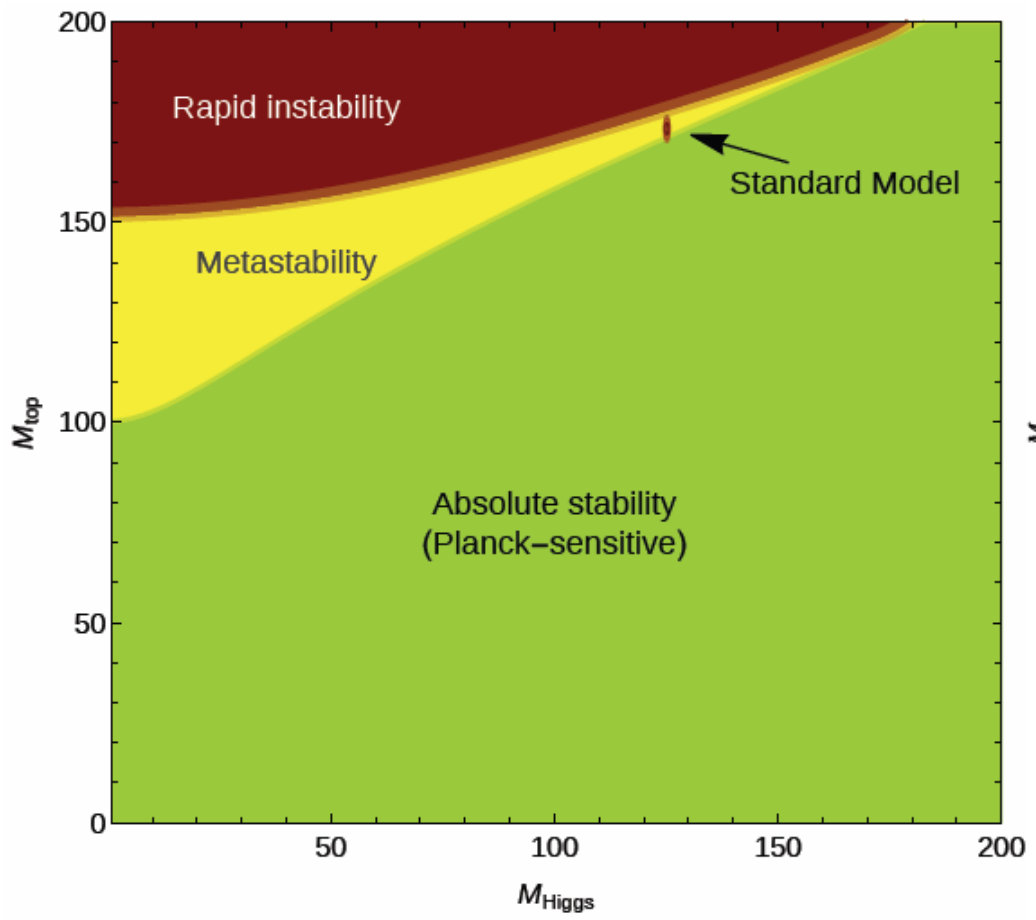
From direct
 search at LEP:

$$M_H > 114 \text{ GeV @ 95\% CL}$$

From direct
 search at Tevatron:

$$158 < M_H < 175 \text{ GeV @ 95\% CL}$$

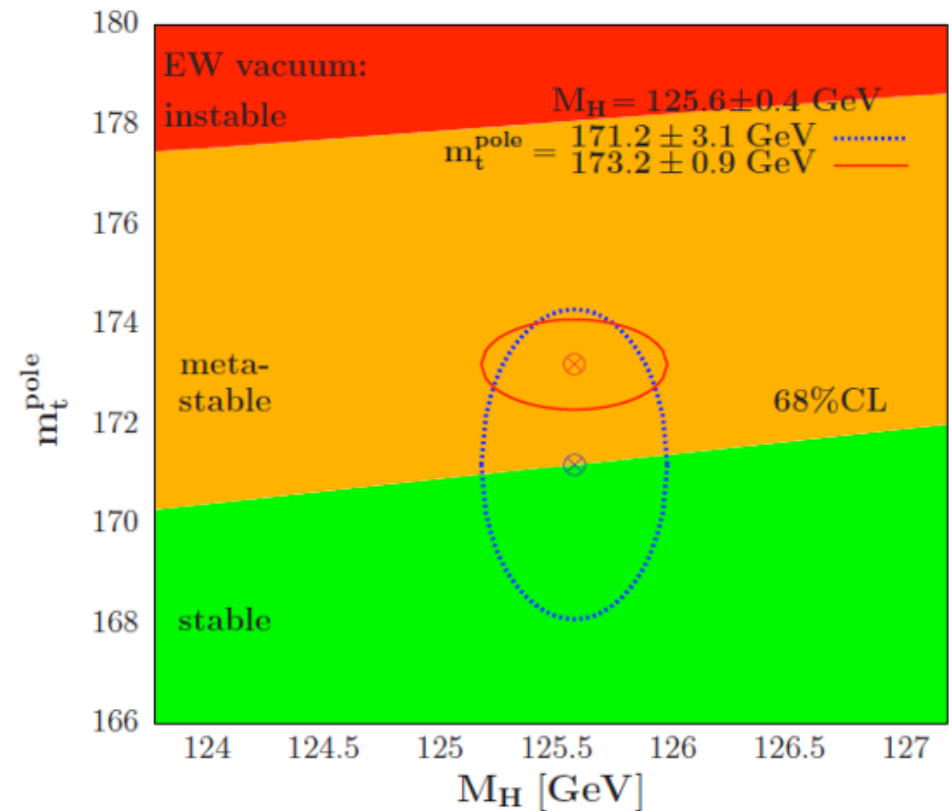
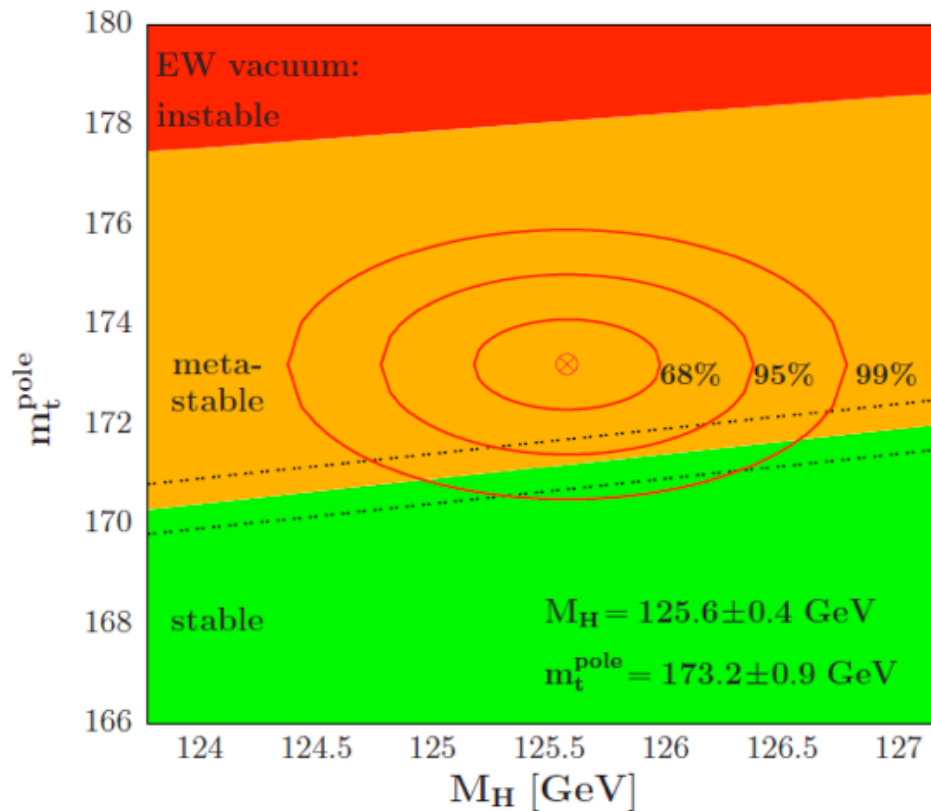
After the Higgs discovery: m_{top} vs m_{Higgs} and stability of the Universe



$$m_h^{\text{pole}} = (125.14 \pm 0.23) \text{ GeV}$$

$$m_t^{\text{pole}} = (173.34 \pm 1.12) \text{ GeV}$$

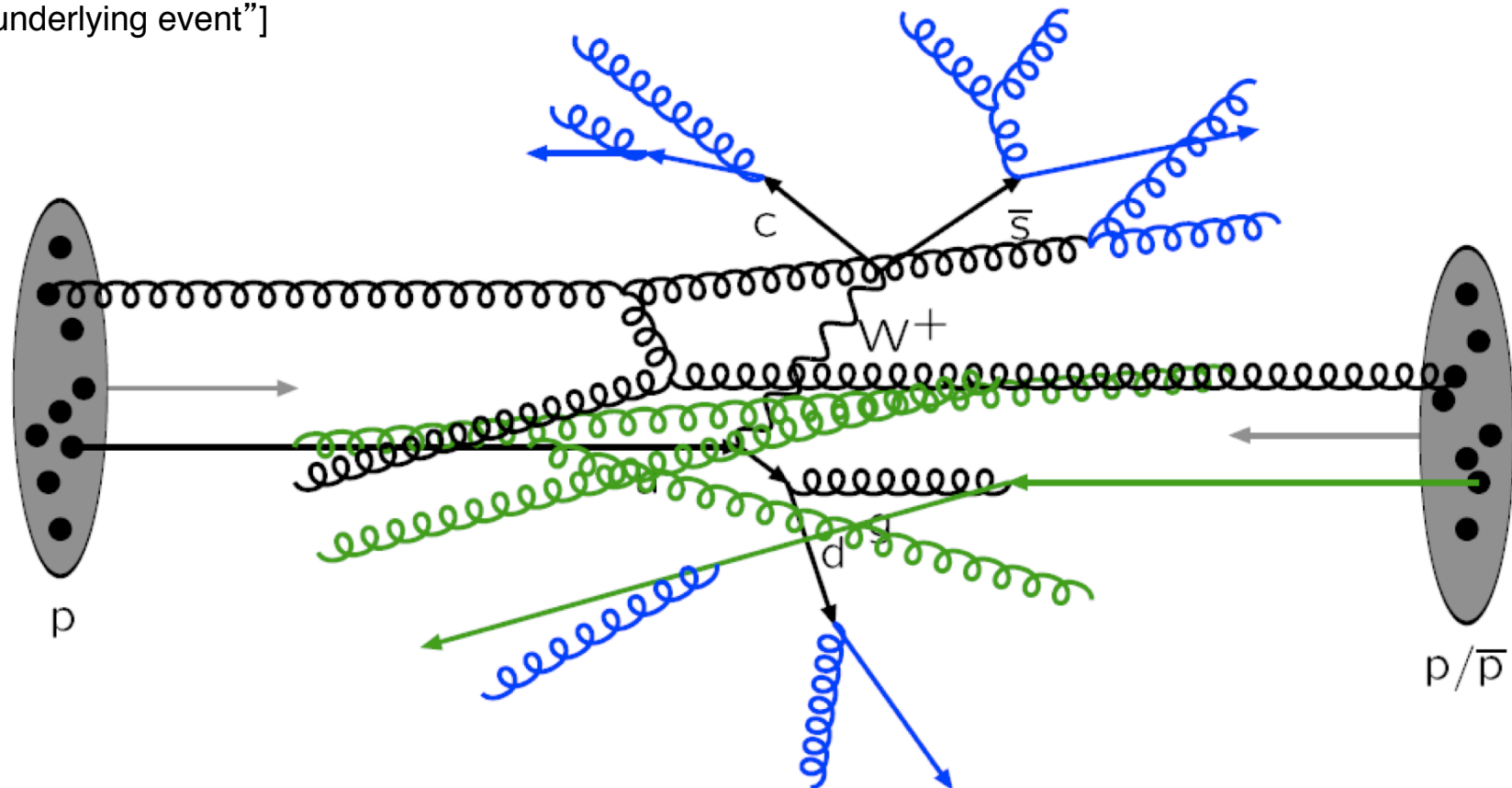
After the Higgs discovery: m_{top} vs m_{Higgs} and stability of the Universe



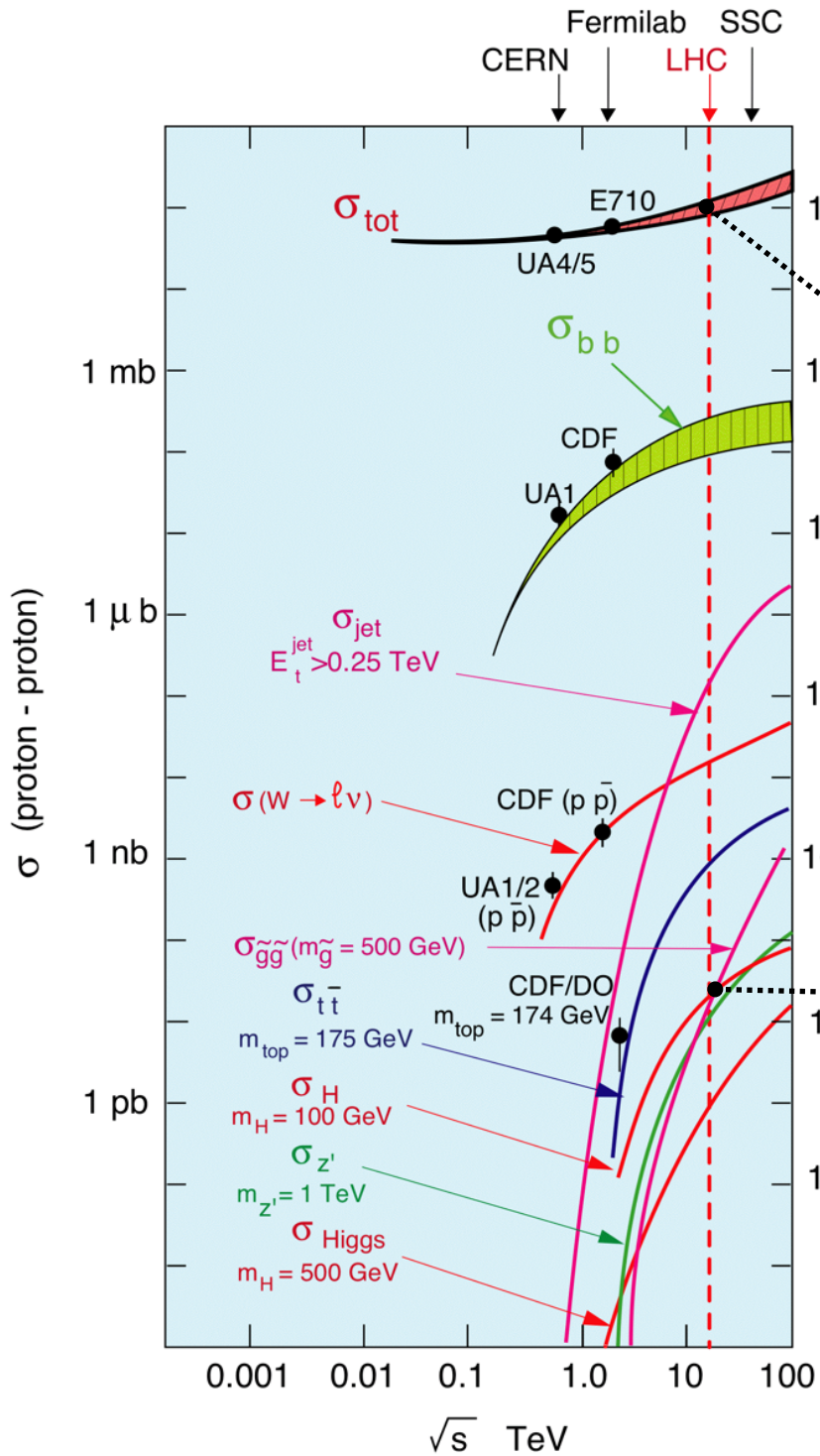
The ellipses in the $[M_H, m_t^{\text{pole}}]$ plane with the inputs $M_H = 125 \pm 0.4$ GeV and $\alpha_s = 0.1187$ are confronted with the areas in which the SM vacuum is absolutely stable, metastable and unstable up to the Planck scale. Left plot m_t^{pole} is identified with the Tevatron measured top mass $m_t = 173.2 \pm 0.9$ GeV, Right: m_t^{pole} is taken as the one measured at the Tevatron $m_t = 171.2 \pm 3.1$ GeV extracted for the $t\bar{t}$ production cross section

Proton-Proton Scattering @ LHC

- Hard interaction: qq , gg , qg fusion
- Initial and final state radiation (ISR,FSR)
- Secondary interaction
[“underlying event”]



Needle in a Haystack



Events / sec for $\mathcal{L} = 10^{34} \text{ cm}^{-2} \text{ sec}^{-1}$

10^9 Events/sec
[1 Mbyte/Event]

$\sim 10^{10}$

Efficient rate reduction needed
[Storage rate: 100 Hz]

10 Events/min
[$m_H \approx 100$ GeV]

with 0.2% $H \rightarrow \gamma\gamma$
1.5% $H \rightarrow ZZ$

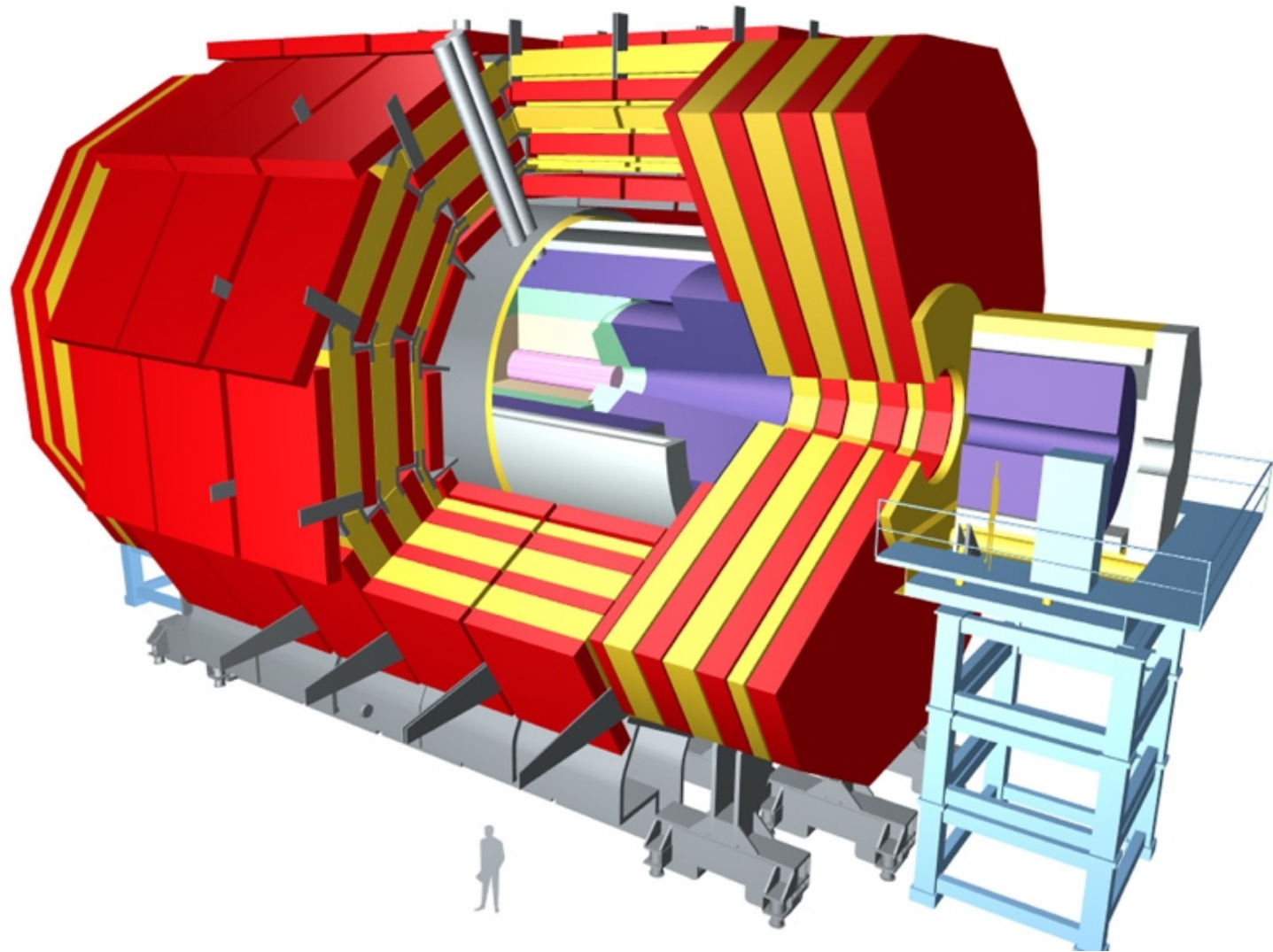
Trigger !

Experiments

The LHC and its Experiments

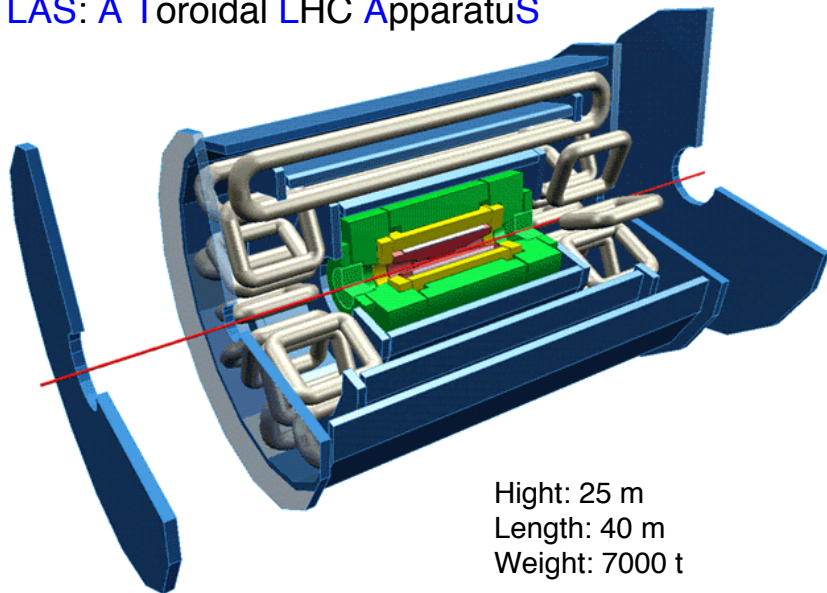


LHC Detectors, mostly ATLAS & CMS



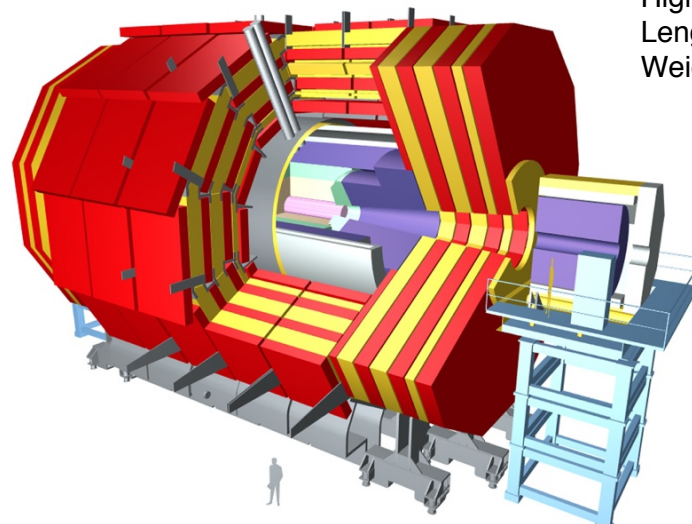
Basic Design Concepts

ATLAS: A Toroidal LHC ApparatuS

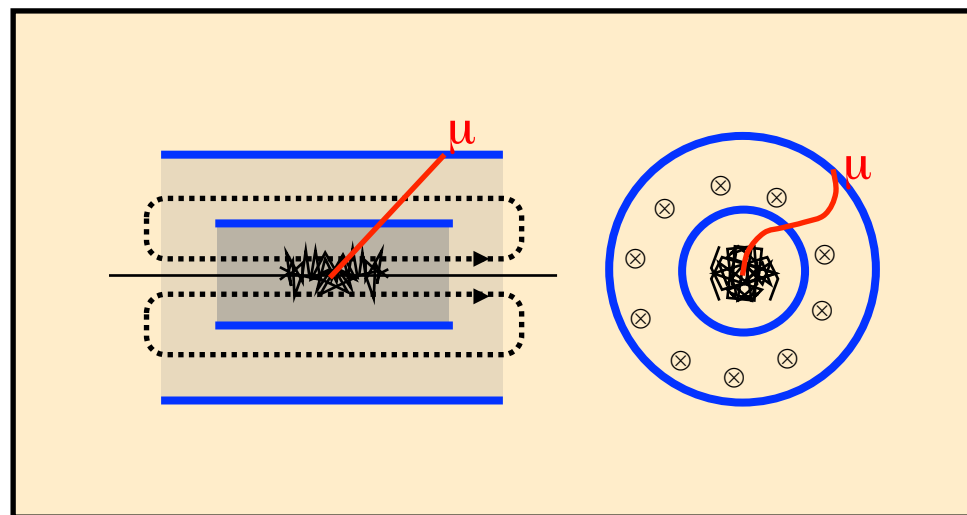
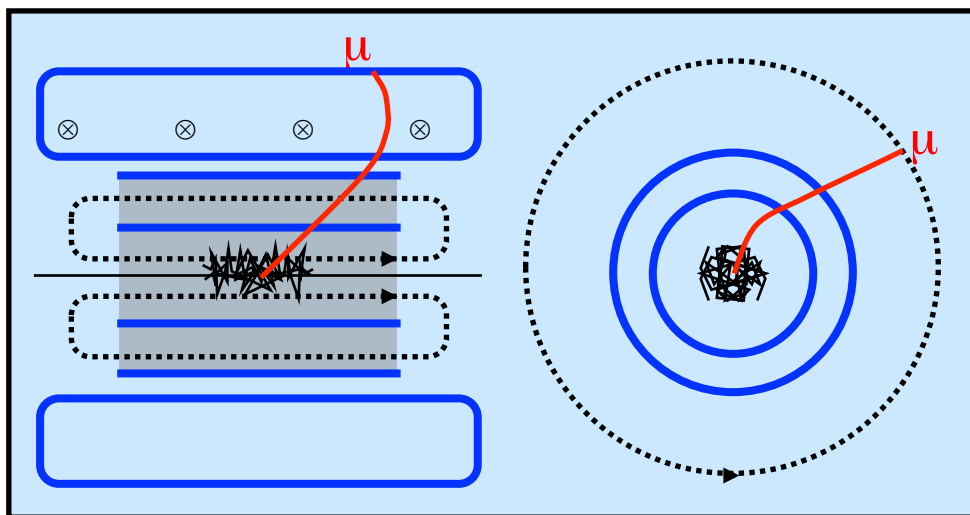


Height: 25 m
Length: 40 m
Weight: 7000 t

CMS: Compact Muon Solenoid



Height: 15 m
Length: 22 m
Weight: 12500 t



The ATLAS Detector

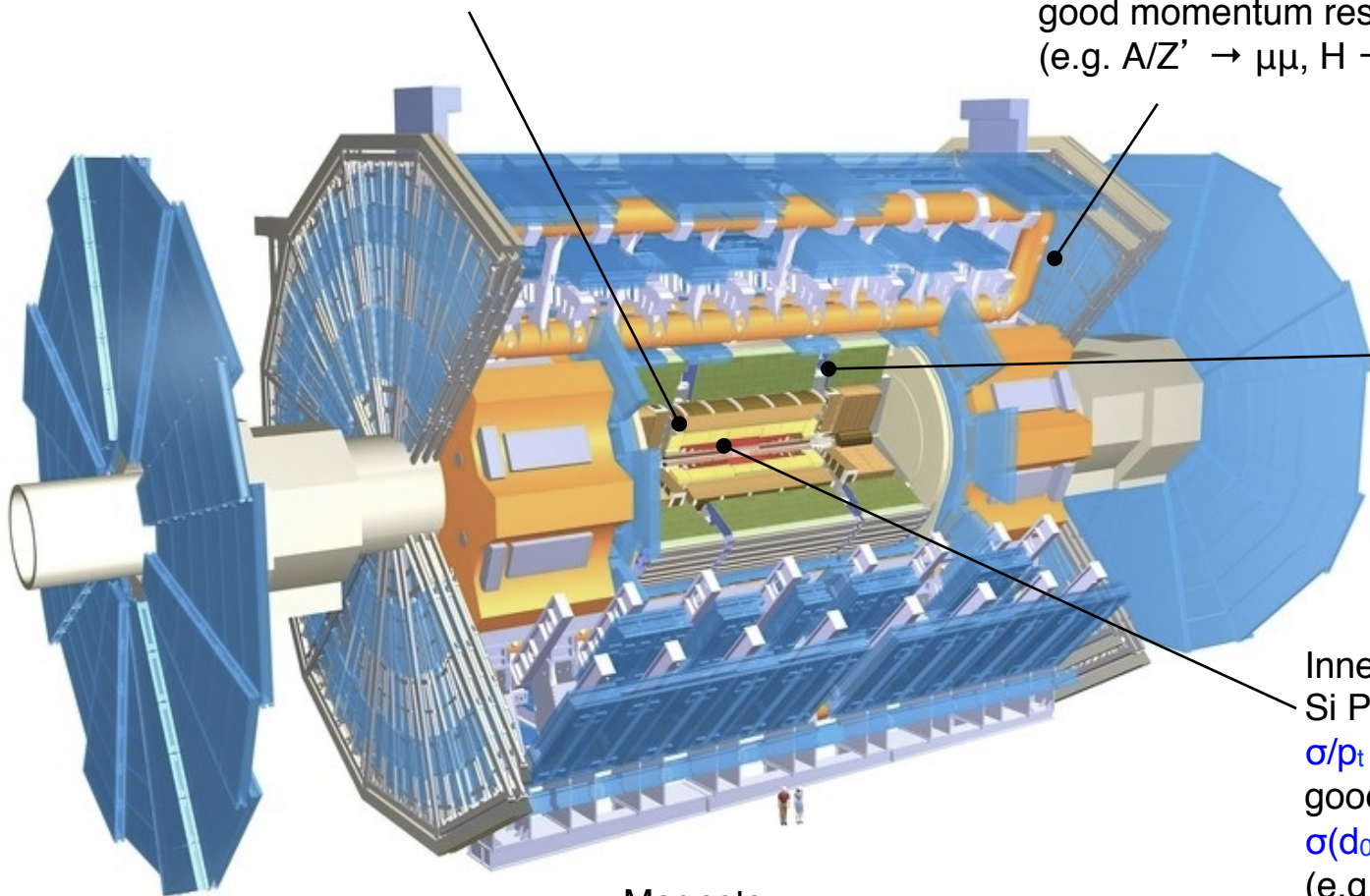
EM Calorimeters: $\sigma/E \approx 10\%/\sqrt{E} \oplus 0.7\%$
 excellent e/ γ identification
 good energy resolution (e.g. for $H \rightarrow \gamma\gamma$)

Precision Muon Spectrometer: $\sigma/p_t \approx 10\% @ 1 \text{ TeV}$
 fast trigger response
 good momentum resolution
 (e.g. $A/Z' \rightarrow \mu\mu$, $H \rightarrow 4\mu$)

Hadron Calorimeter:
 $\sigma/E \approx 50\%/\sqrt{E} \oplus 3\%$
 good jet resolution
 good missing E_T resolution
 (e.g. $H \rightarrow \tau\tau$)

Inner Detector:
 Si Pixel & strips; TRT
 $\sigma/p_t \approx 5 \cdot 10^{-4} p_t \oplus 0.001$
 good impact parameter res., i.e.
 $\sigma(d_0) \approx 15 \mu\text{m} @ 20 \text{ GeV}$
 (e.g. $H \rightarrow b\bar{b}$)

Magnets:
 Solenoid (inner detector): 2 T
 Toroid (muon spectrometer): 0.5 T



The CMS Detector

EM Calorimeters:

$$\sigma/E \approx 3\%/ \sqrt{E} \oplus 0.5\%$$

[cf. ATLAS: $\sigma/E \approx 10\%/ \sqrt{E} \oplus 0.7\%$]

Inner Detector:

$$\sigma/p_t \approx 5 \cdot 10^{-4} p_t \oplus 0.001$$

[cf. ATLAS $\sigma/p_t \approx 5 \cdot 10^{-4} p_t \oplus 0.001$]

Hadron Calorimeter:

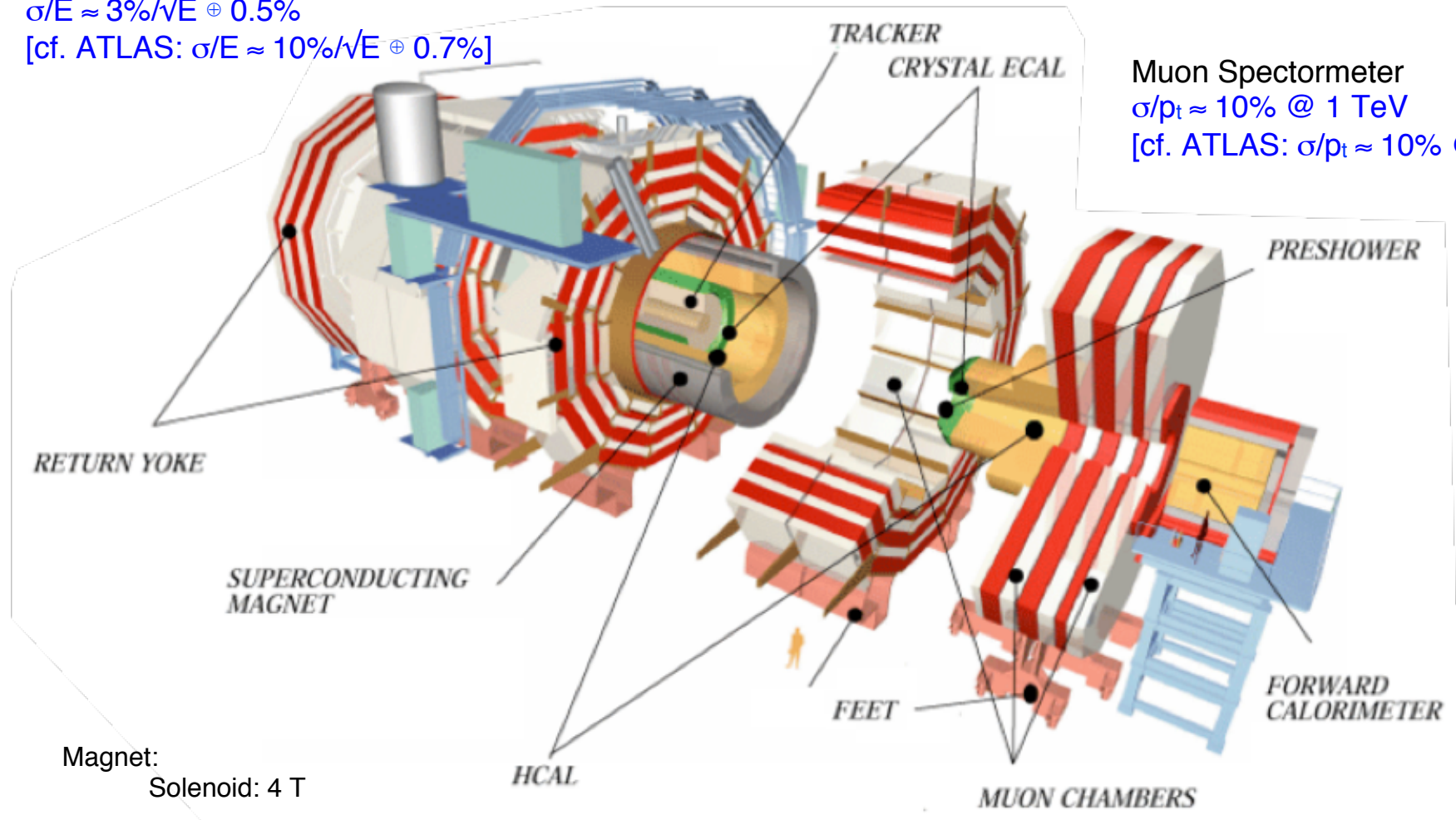
$$\sigma/E \approx 100\%/ \sqrt{E} \oplus 5\%$$

[cf. ATLAS: $\sigma/E \approx 50\%/ \sqrt{E} \oplus 3\%$]

Muon Spectrometer

$$\sigma/p_t \approx 10\% \text{ @ } 1 \text{ TeV}$$

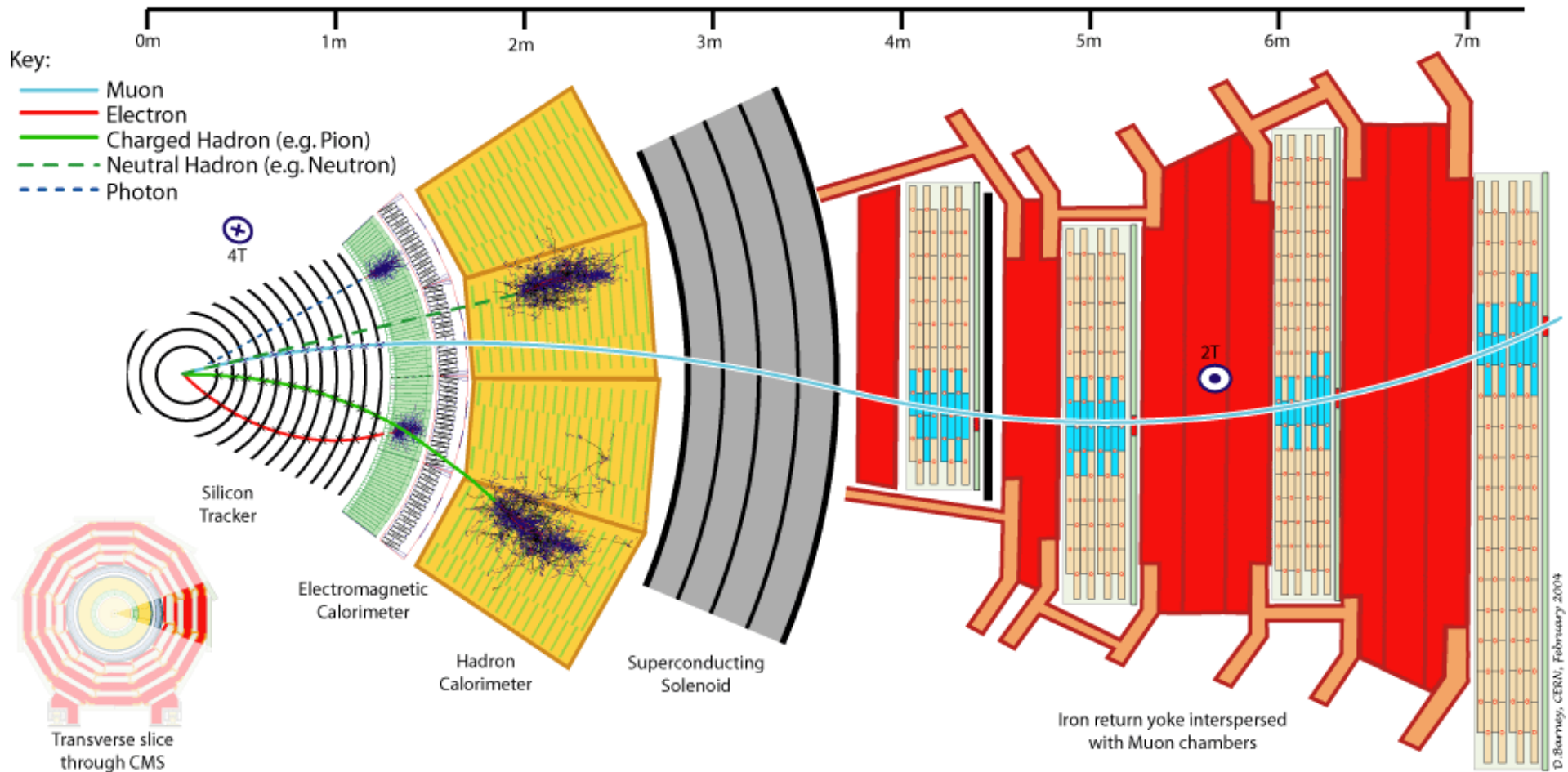
[cf. ATLAS: $\sigma/p_t \approx 10\% \text{ @ } 1 \text{ TeV}$]



Magnet:

Solenoid: 4 T

The CMS Detector - 2



ATLAS vs CMS

ATLAS

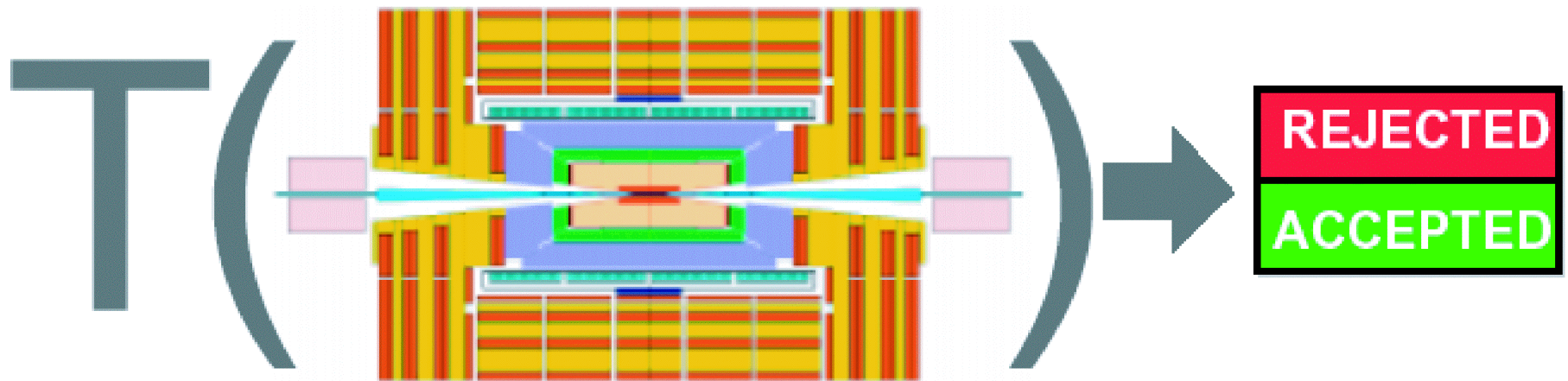
<p>Silicon pixels; Silicon strips; Transition Radiation Tracker; 2 T magnetic field</p>	<p>Inner Detector</p>	<p>Silicon pixels, Silicon strips, 4 T magnetic field</p>
<p>Lead plates as absorbers; active medium: liquid argon; outside solenoid</p>	<p>Electrom. Calorimeter</p>	<p>Lead tungsten (PbWO_4) crystals; both absorber and scintillator; inside solenoid</p>
<p>Central region: Iron absorber with plastic scintillating tiles; Endcaps: copper and tungsten absorber with liquid argon</p>	<p>Hadronic Calorimeter</p>	<p>Stainless steel and copper with plastic scintillating tiles</p>
<p>Large air-core toroid magnet; muon chambers: drift tubes and resistive plate chambers; 0.5 T magnetic field</p>	<p>Muon Chambers</p>	<p>Magnetic field from return yoke (solenoid field: 4 T); muon chambers: drift tubes and resistive plate chambers</p>

CMS

Challenge 1: Fast Trigger System

Fast selection of interesting Events

Number of necessary decisions: 40 million/sec

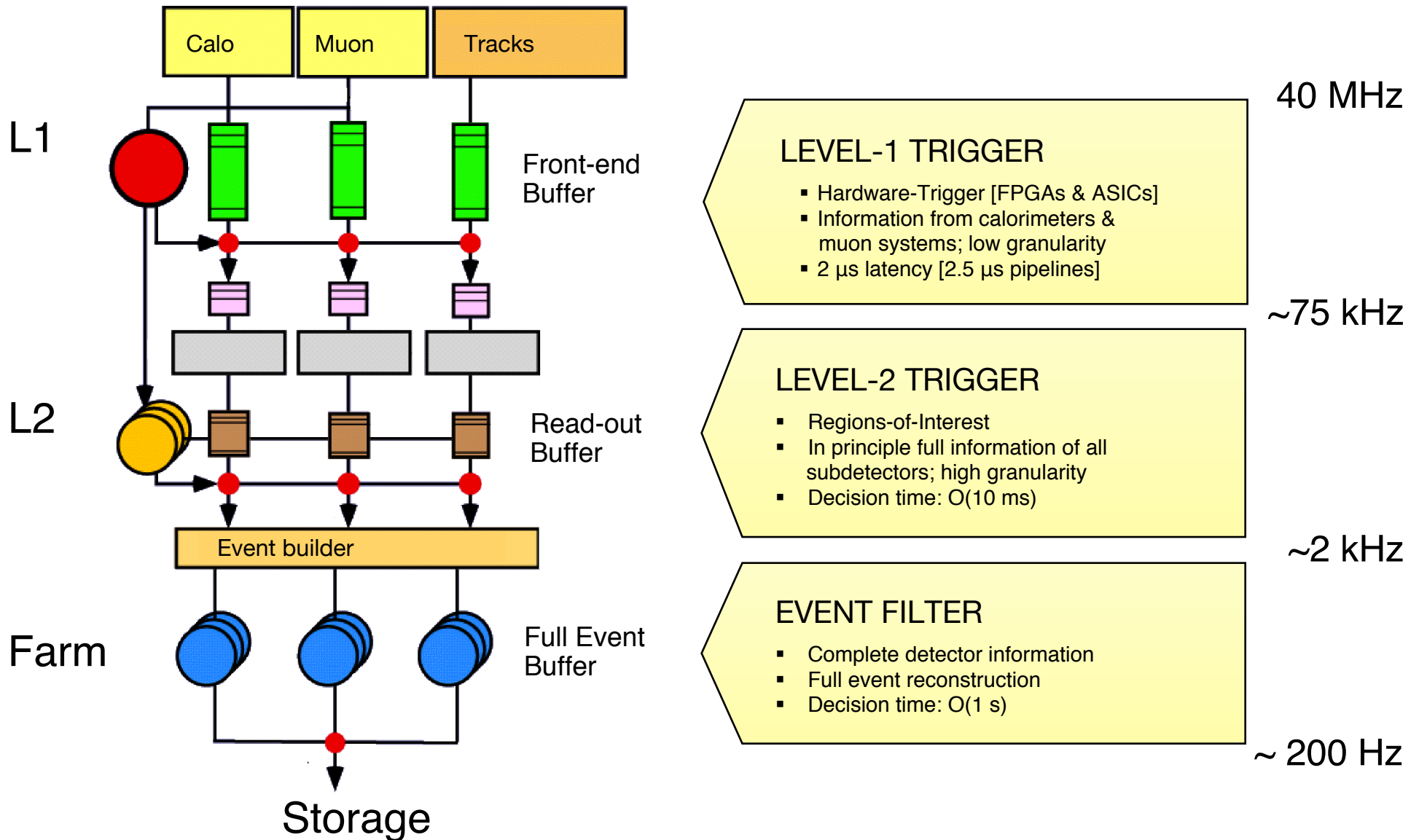


Function $T(\dots)$ is highly complex
Detector data not directly available

→ Stepwise decision

→ Trigger Levels

Challenge 1: Fast Trigger System



Accelerators

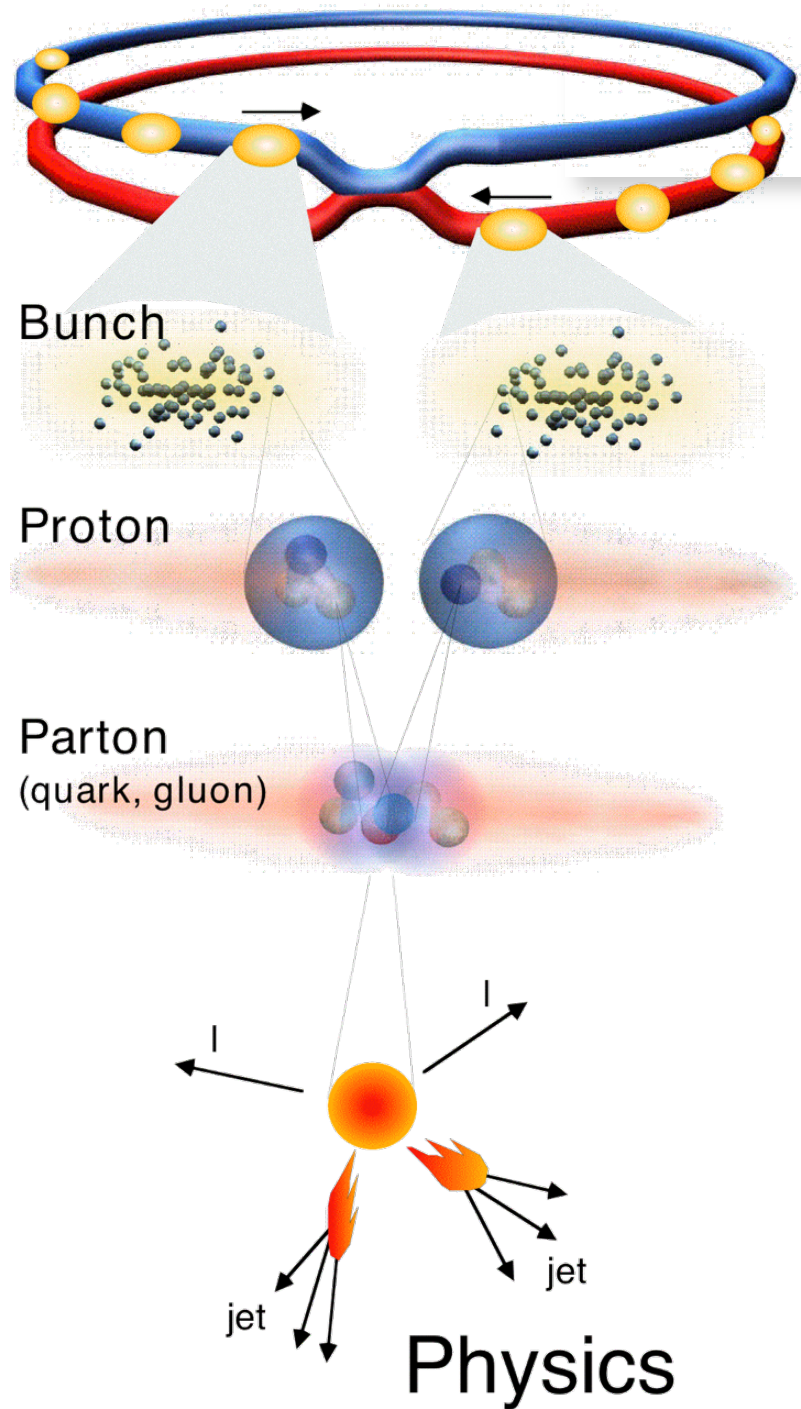
The LHC and its Experiments



The Large Hadron Collider



Proton-Proton



Some numbers (relevant for ATLAS & CMS)

~ 3564x3564 proton bunches
distance: 7.5 m [25 ns]

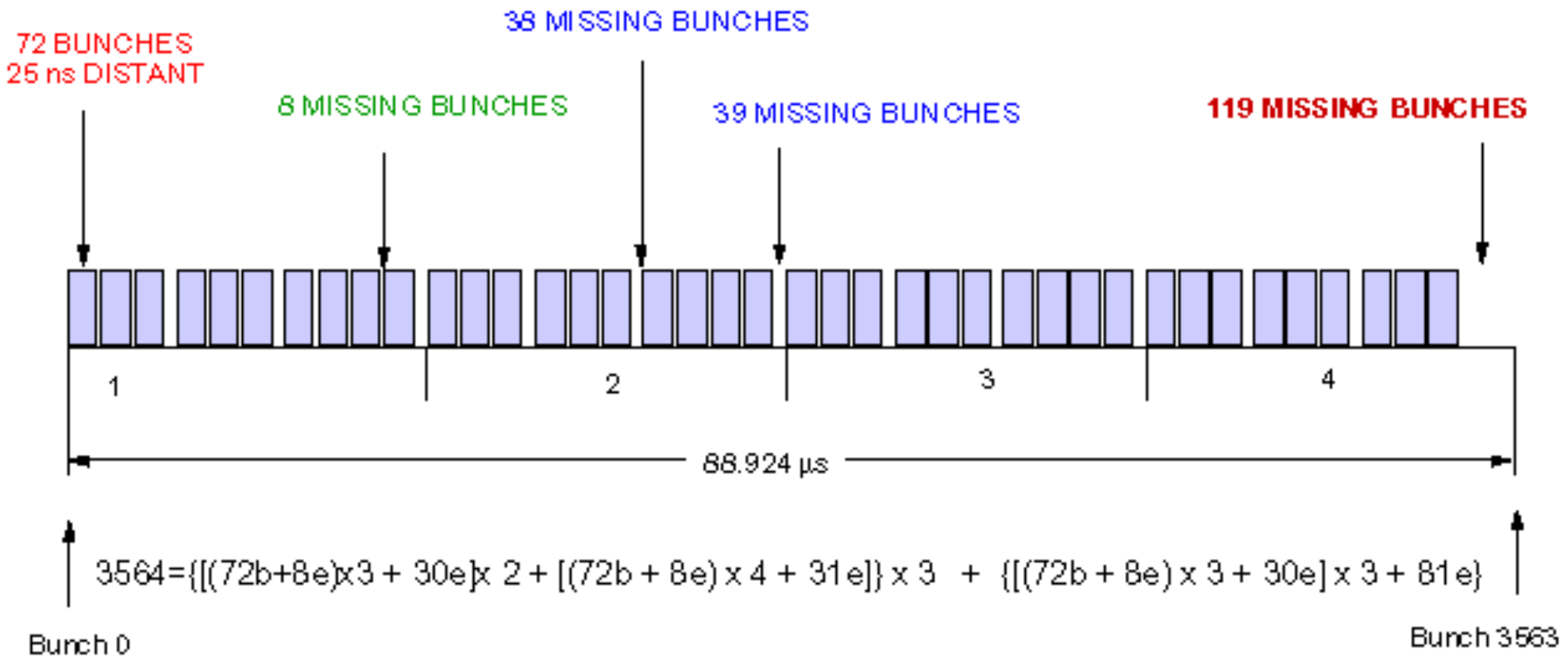
10^{11} protons/bunch
bunch crossing rate: 40 MHz

10^9 pp-collisions/sec
[i.e.: 23 pp-interactions/bunch crossing.]

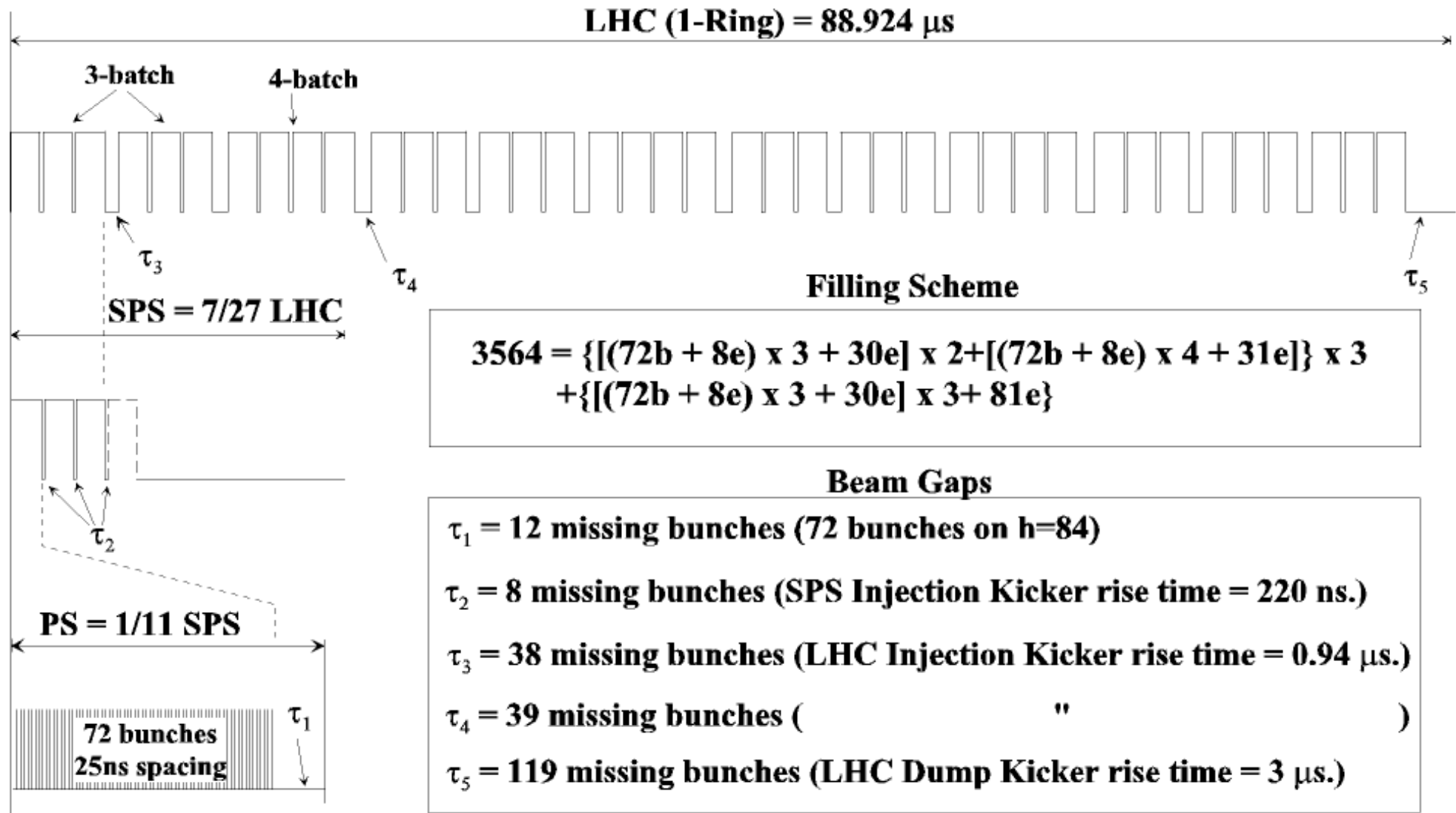
Dominant Interactions:
gluon-gluon, quark-quark and
quark-gluon scattering

Physics

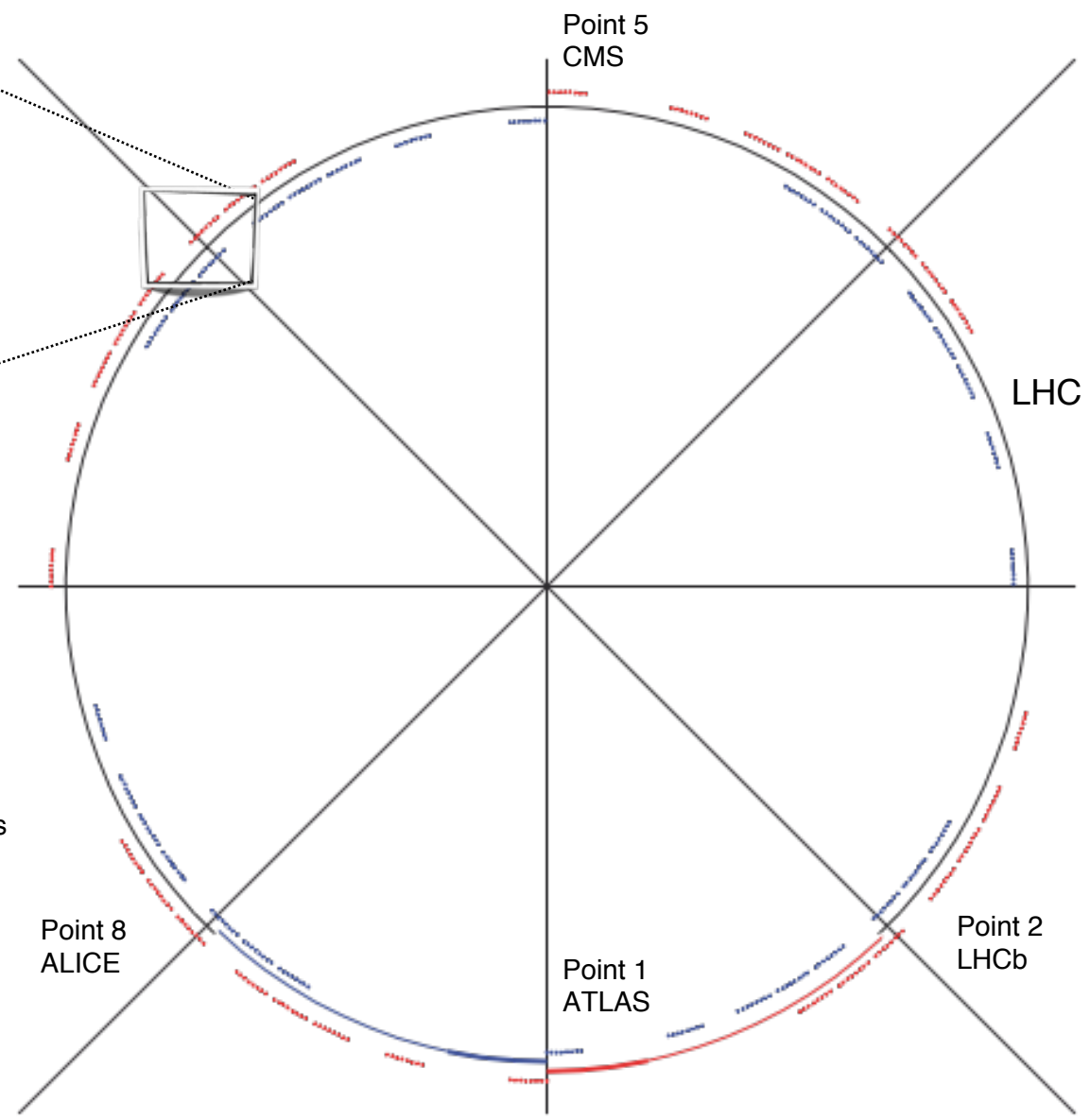
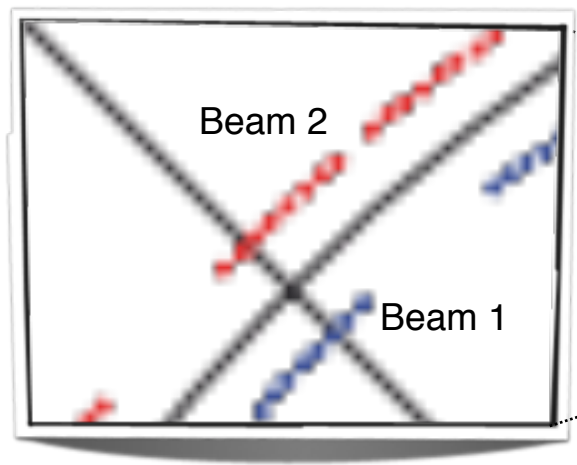
LHC Nominal Bunch Structure



Bunch structures in LHC, SPS and PS



Present LHC Status



Present Bunch Structure:

150ns_248b_233_16_233_3x8bpi15inj

bunch distance

number of bunches

colliding bunches in point 8

colliding bunches in point 2

colliding bunches in points 1/5

This text block provides the parameters of the bunch structure: 150ns (bunch distance), 248b (number of bunches), 233 (colliding bunches in point 8), 16 (colliding bunches in point 2), 233 (colliding bunches in points 1/5), and 3x8bpi15inj (likely referring to the injection system).

LHC in Operation

LHC Page1
Fill: 1406
E: 3500 GeV
10-10-2010 20:52:35

PROTON PHYSICS: RAMP

Energy: 3500 GeV

I(B1): 2.70e+13

I(B2): 2.61e+13

FBCT Intensity and Beam Energy Updated: 20:52:35

Comments 10-10-2010 19:40:36 :

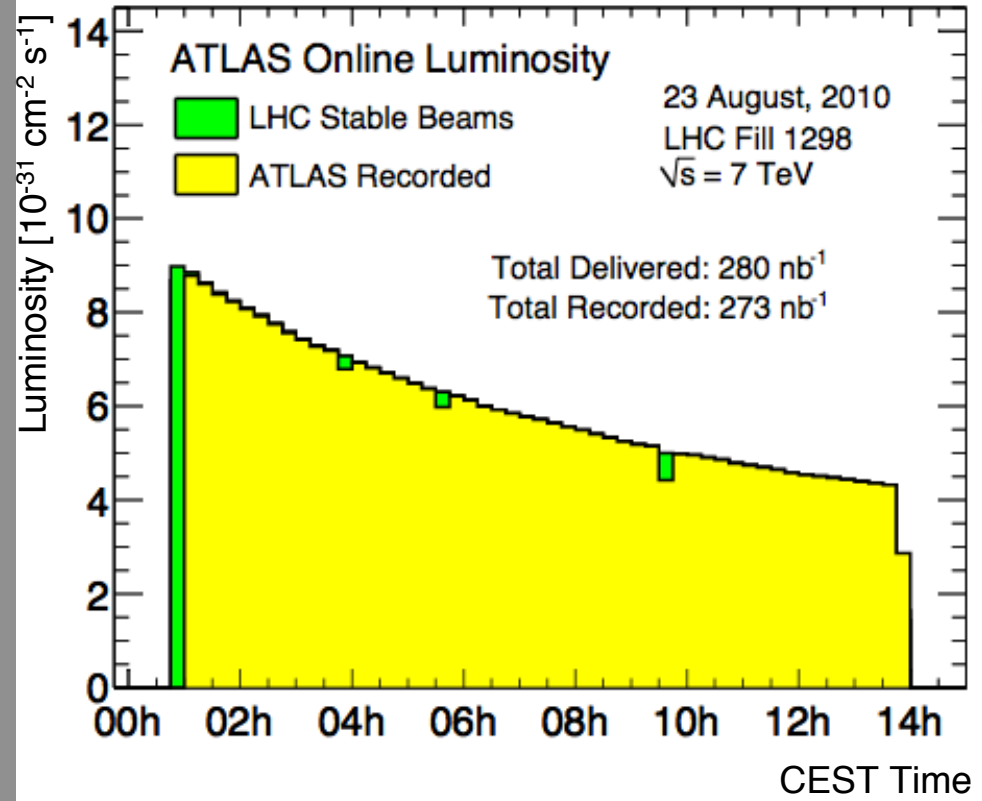
injecting

Next: Fill for physics (248 bu/ring)

BIS status and SMP flags	B1	B2
Link Status of Beam Permits	true	true
Global Beam Permit	true	true
Setup Beam	false	false
Beam Presence	true	true
Moveable Devices Allowed In	false	false
Stable Beams	false	false

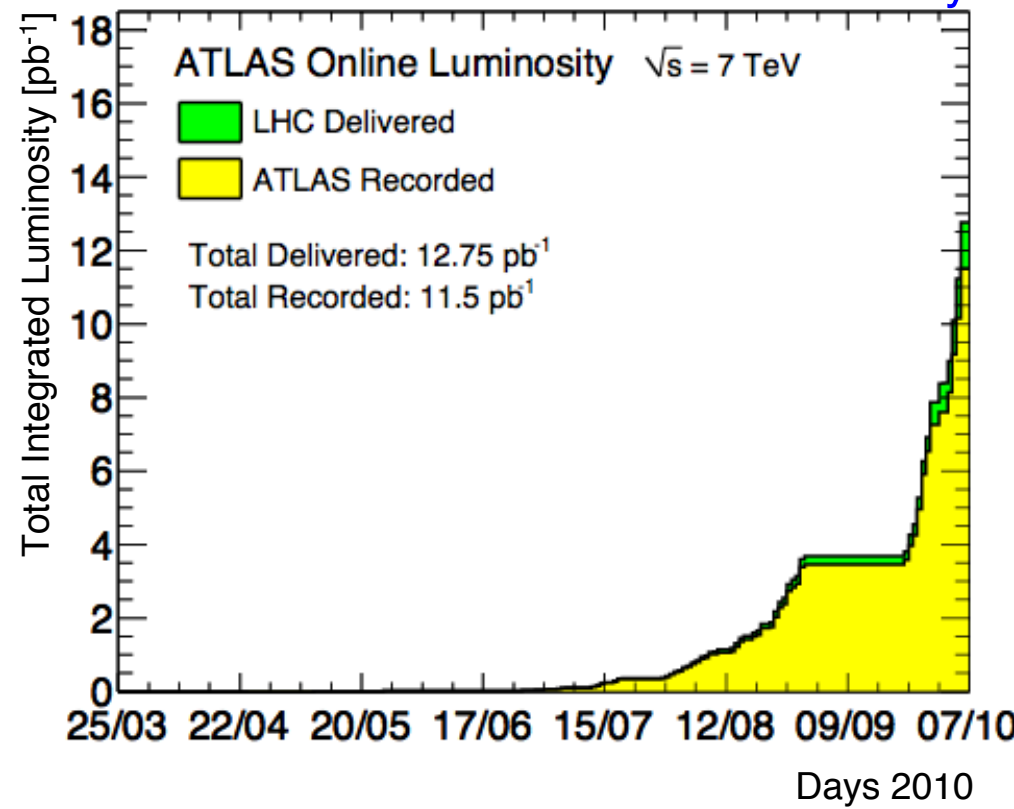
LHC Operation in CCC : 77600, 70480
PM Status B1 ENABLED
PM Status B2 ENABLED

Present LHC Status



LHC Fill
 [August 2010]

Delivered and Recorded
 Luminosity



$$N = L \cdot \sigma$$

Number of Events

Integrated Luminosity

X-Sec.

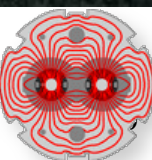
Introduction to Accelerators



Helmut Burkhardt, CERN



[ISEF 2013](#) 24 June 2013



Contents

- **Concepts: Energy Gain, E / B field. Units**
 - **Types of accelerators : Ring, Collider, Linac, e+e-, pp ; Cosmic**
 - **Components: Source, Magnets, resonant Cavities**
 - **Basic machine optics**
 - **Energy and Luminosity**
 - **Synchrotron Radiation**
 - **Limitations, current and future challenges**
-
- **Mixed with examples - mostly from CERN machines and in particular the LHC**

General, introductory refs. and books on Accelerators :

E. D. Courant and H. S. Snyder, *Theory of the Alternating-Gradient Synchrotron*, [pdf](#)

M. Sands, *Physics of Electron Storage Rings*, [SLAC Report No. 121](#); Wiedemann, *Particle Accelerator Physics* Bd. I,II

S.Y. Lee, *Accelerator Physics*, [World Scientific](#); M. Conte, W. MacKay, *Physics of Particle Accelerators*, [World Scientific](#)

CERN CAS yellow reports ; K. Wille, *The physics of particle accelerators*, Oxford University Press, 1996

Accelerators for Particle Physics, H. Burkhardt, in Handbook of Particle Detection and Imaging, [Ed. C. Grupen](#), Oct. 2011

The **Large Hadron Collider** : O. Brüning, H. Burkhardt, S. Myers, [10.1016/j.ppnp.2012.03.001](#), [CERN-ATS-2012-064](#)

Accelerators and Colliders, Landolt-Börnstein New Series I/21C, [Springer 2013](#)

Accelerators at the Energy Frontier

Livingston plot

Exponential growth
of E_{cm} in **time**

Starting in 60's
with e^+e^- at about 1GeV

Factor 4 every 10 y

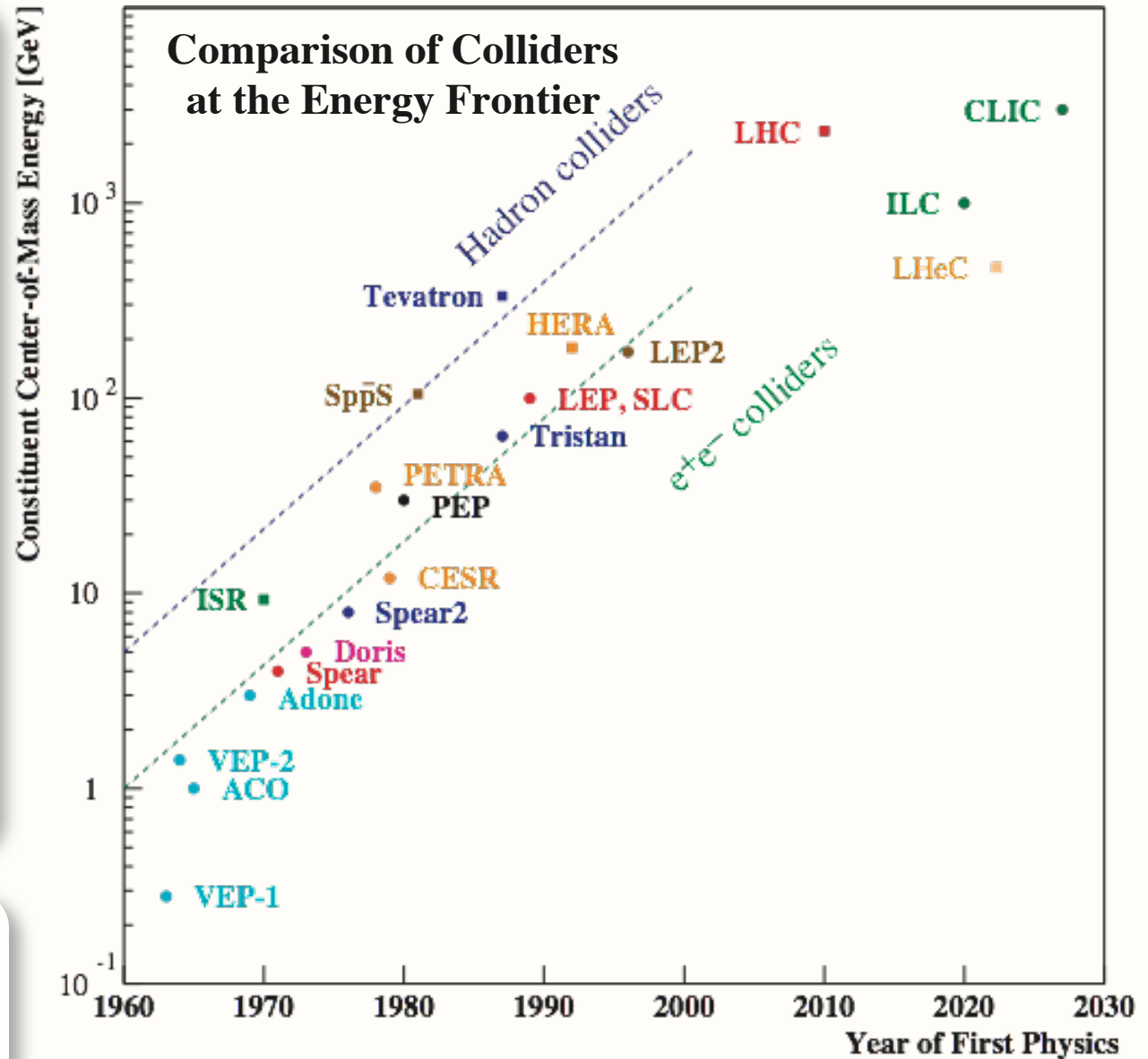
$pp, p\bar{p}$: $E_{cm} / 6$
still $5 \times$ above e^+e^- at
same time

$pp, p\bar{p}$: **discovery**

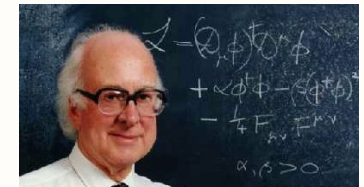
e^+e^- : **precision**

both required machines

+ ep : hadron structure, QCD
HERA, LHeC

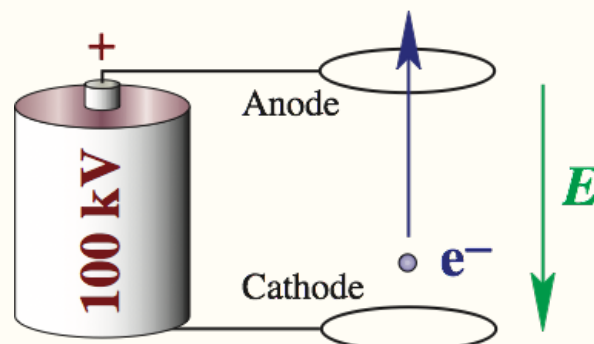


The LHC is a major step forward
Discovery machine : Higgs ...



Basic concepts and units

Electric field :
Acceleration
 or rather
Energy gain
100 keV



Electric charge **e**
 and electric field **E**

Special relativity, Lorentz transformation

$$E = \gamma m c^2 \quad p = \beta \gamma m c \quad \beta = \frac{v}{c} \quad \gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

$$m_e \approx 0.511 \text{ MeV}/c^2 \quad m_p \approx 938 \text{ MeV}/c^2 \quad e \approx 1.602 \times 10^{-19} \text{ C}$$

For $E = 10 \text{ GeV}$:

Electron $\beta = 0.999\,999\,9987 \quad \gamma = 19569.5$

Proton $\beta = 0.995\,588\,4973 \quad \gamma = 10.6579$

Unit conversion

$$\frac{e^2}{4\pi\epsilon_0} = \alpha \hbar c = r_{\text{part}} m_{\text{part}} c^2 = 1.43996 \times 10^{-18} \text{ GeV m}$$

$$\hbar c = 197.327 \times 10^{-18} \text{ GeV m}$$

$$(\hbar c)^2 = 3.8938 \times 10^{-32} \text{ GeV}^2 \text{ m}^2 = 3.8938 \times 10^5 \text{ GeV}^2 \text{ nb}$$

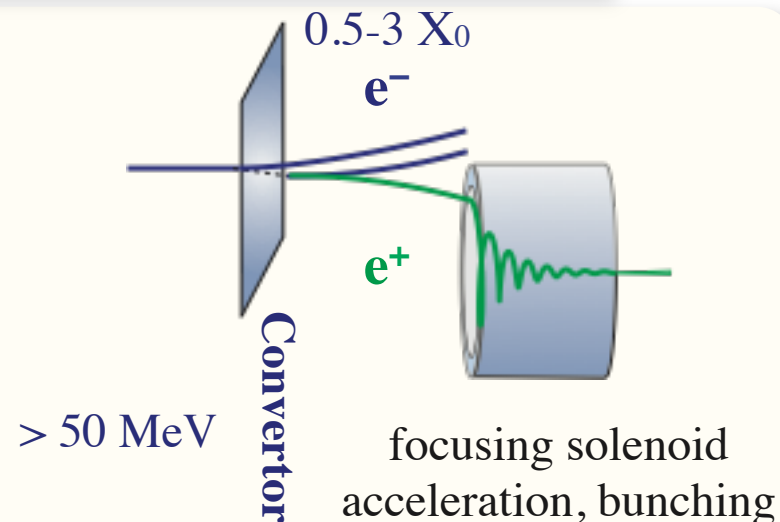
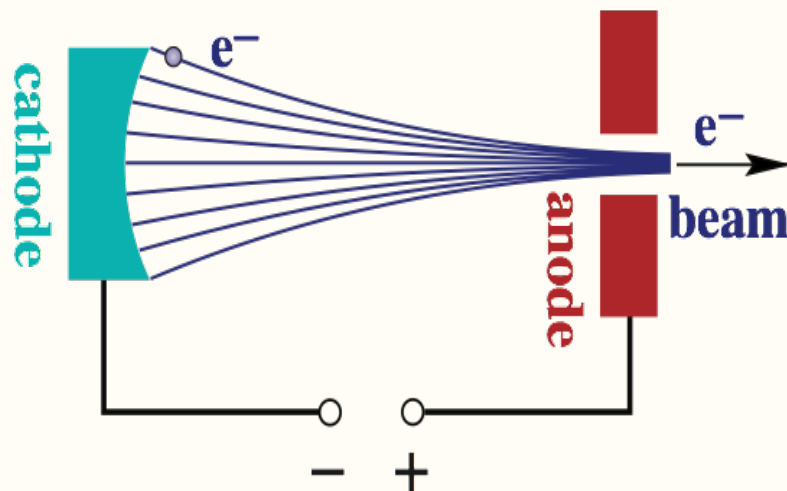
for precise numbers see [PDG](#)

giga G = 10^9 tera T = 10^{12} peta P = 10^{15} exa E = 10^{18} zetta Z = 10^{21} yotta Y = 10^{24}

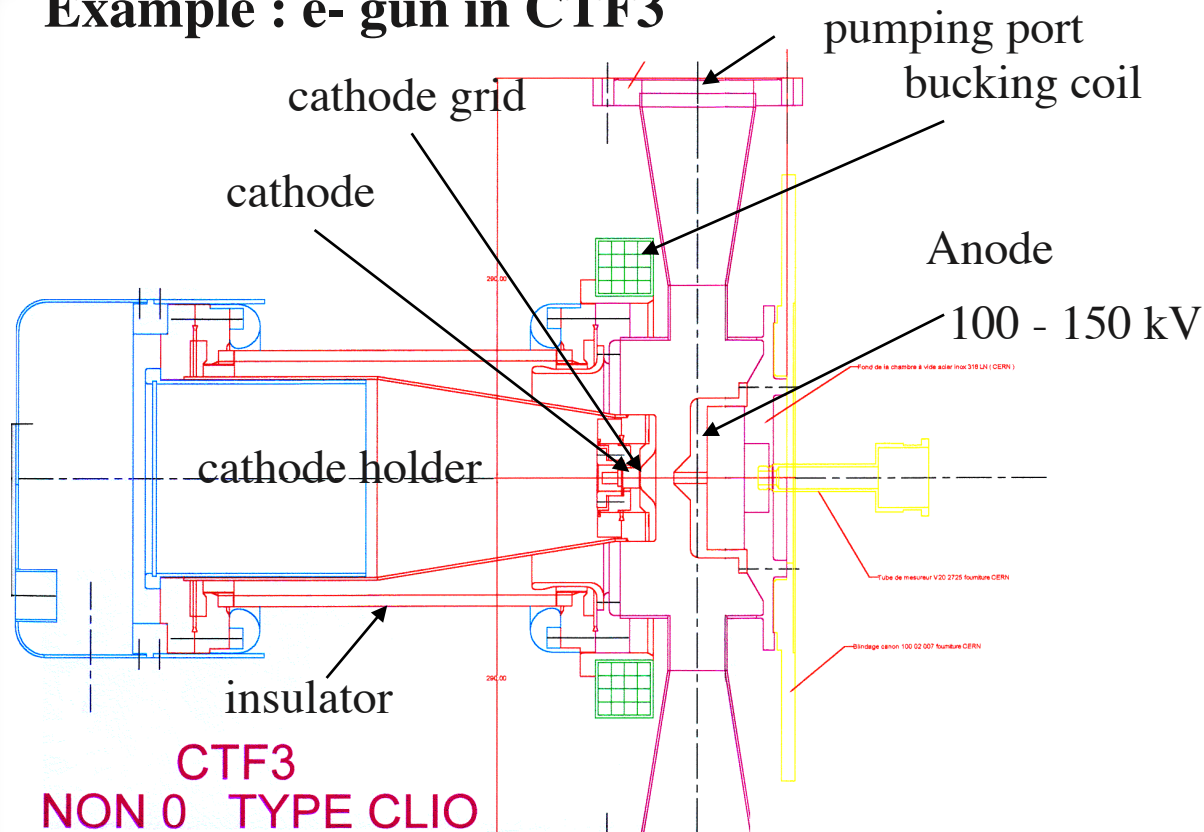
Particle sources

Thermionic electron source principle

same as cathode ray tube



Example : e- gun in CTF3



challenges :

high intensity

polarized e^- sources

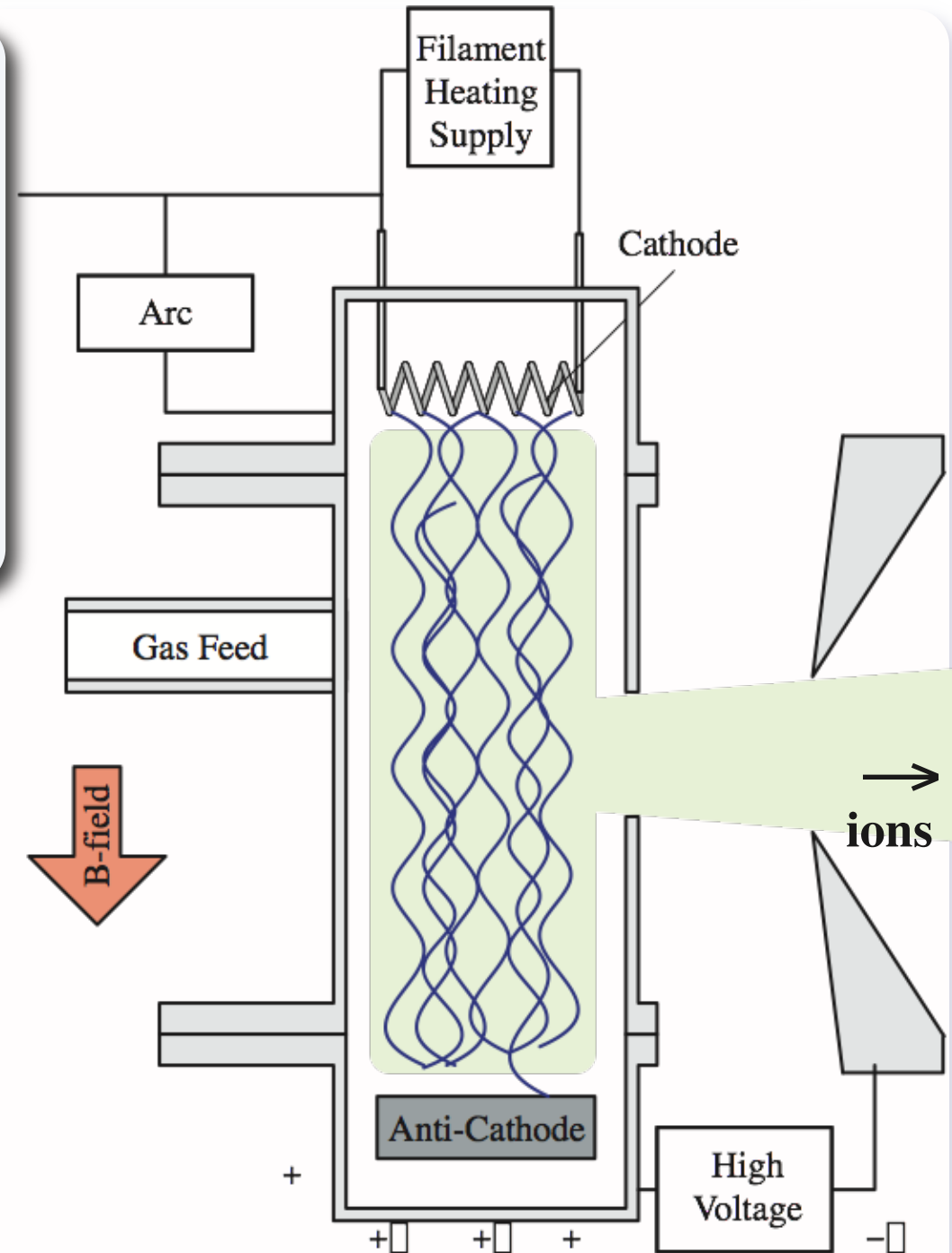
damping rings for minimum emittance

undulator polarized e^+ sources

Proton and ion sources

Various methods exist to produce p (H^+), H^- (p with $2 e^-$) and heavy ions - heavier atoms, most electrons removed

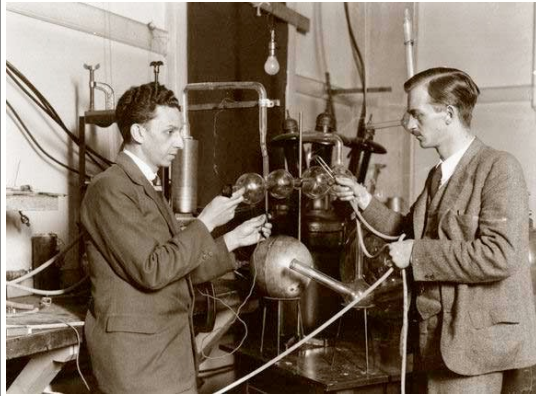
Typically involves : **low pressure heated gas ionized gas / plasma**, inject H_2 to get protons, **or surface sputtering and electric and magnetic fields** to keep the electrons



CERN p-source and 50 MeV Linac

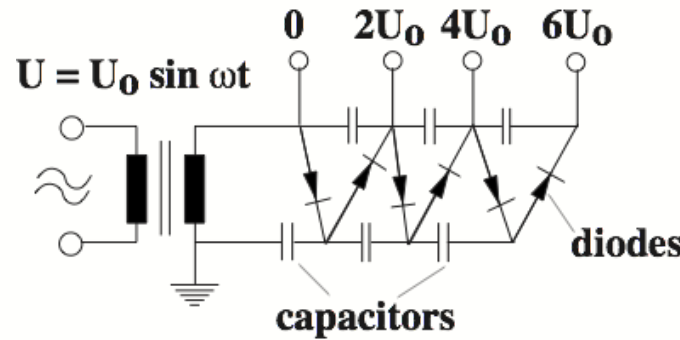
special techniques
H⁻ injection
RadioFrequency
Quadrupole

Linear Acceleration with Electrostatic Field



Cockcroft Walton
voltage multiplier

allows for DC, 100 % duty factor
limited by HV-breakdown $\sim 1 \text{ MV} / \text{m}$

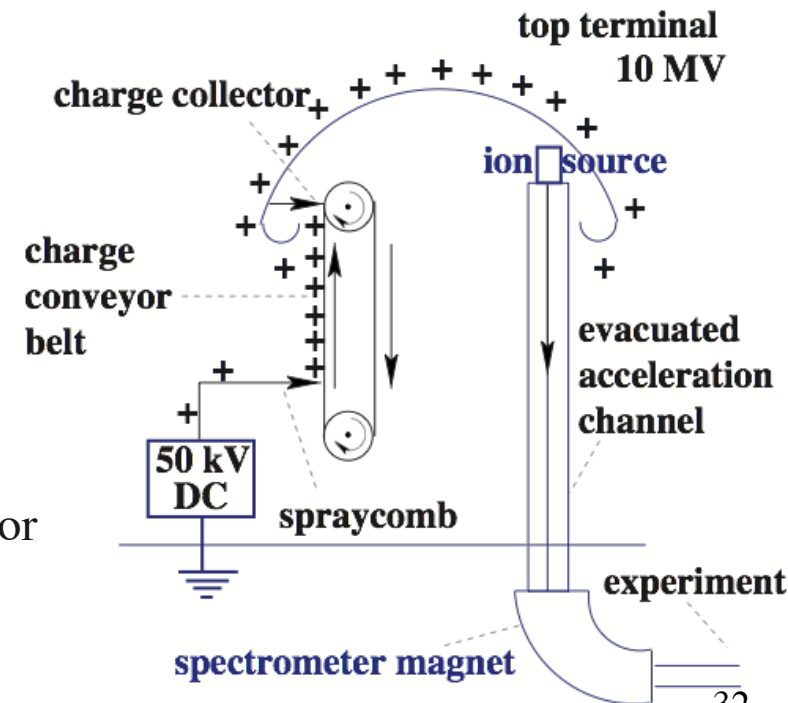


800 kV
 proton pre-
 injector
 used at
 CERN
 until 1993



Van de Graaff generator
 static electricity from belts

Oak Ridge Tandem Van de Graaff generator
 reached 25.5 MV using pressurised SF₆



Time Varying Fields

Radio-frequency or short **RF** acceleration

- allows for multiple passages
- **bunched beams, reduced duty cycle**
- **higher RF frequencies allow for higher acceleration gradients**

no time for breakdown / flashover

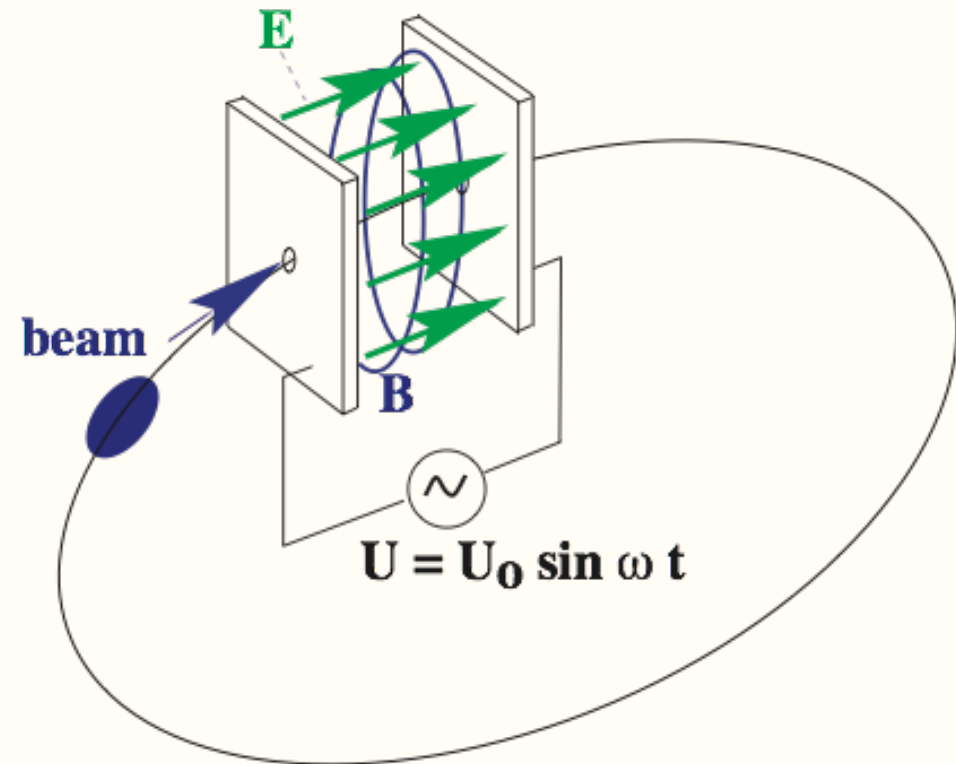
LEP , SC	8 MV / m at 352 MHz
Tesla / ILC, SC	31.5 MV / m at 1.3 GHz
CLIC	100 MV / m at 12 GHz

little gain above 12 GHz

SC limit ~ 50 MV/m, reached for single cell surface gradients higher than acceleration gradients, smooth structures

high f : shorter bunches - collective effects (peak current) and alignment more difficult

less energy stored in structure



9 cell 1.3 GHz SC niobium TESLA / ILC cavity

Basic parameters, Lorentz Force

$$\mathbf{F} = q (\mathbf{E} + \mathbf{v} \times \mathbf{B})$$

charge q , normally $q = e$; $q = Z e$ for ions

- Electric field \mathbf{E} provides the acceleration or rather energy gain
- The magnetic field \mathbf{B} keeps the particles on their path

ρ is the radius of curvature for motion perpendicular to the static magnetic field. Often called

- gyromagnetic or Larmor radius in astroparticle physics
- bending radius for accelerators

$B\rho$ known as magnetic rigidity, units Tm

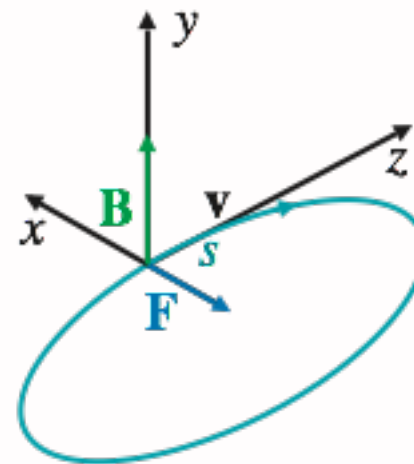
LHC

- Momentum $p = 7 \text{ TeV}/c$
- LHC bending radius $\rho = 2804 \text{ m}$
- Bending field $B = 8.33 \text{ Tesla}$
- magnets at 1.9 K , super-fluid He

Circular motion for

$$\mathbf{E} = 0$$

$$\mathbf{v} \perp \mathbf{B}$$



$$B = \frac{p}{q \rho}$$

for $q = e$ numerically
 $B \text{ [T]} = p \text{ [GeV}/c] \cdot 3.336 \text{ m} / \rho$
high energy, $v = c$ “ $p = E$ ”
 $E < E_H = q B \rho$ Hillas criterion

Astroparticle

units $10^{-4} \text{ T} = 1 \text{ Gauss}$; a.u. = $1.5 \times 10^{11} \text{ m}$

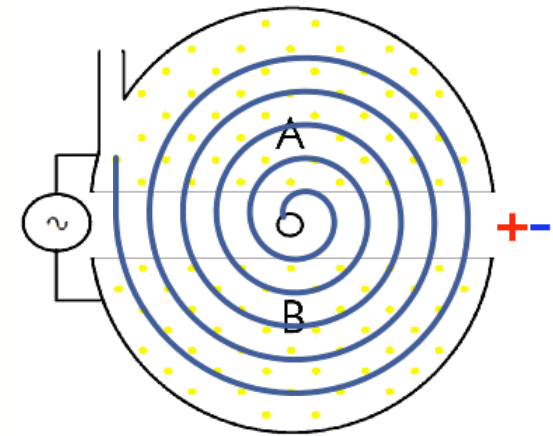
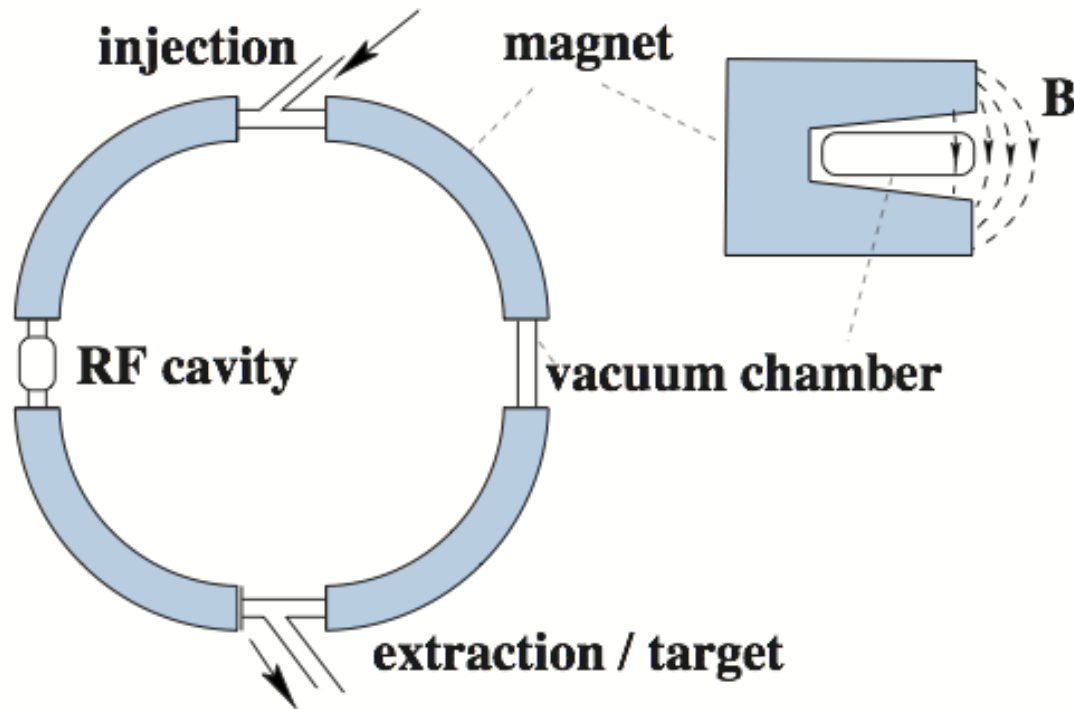
Solar system $B = 10 \mu\text{G}$ $E = 5 \text{ TeV}$ $\rho = 11 \text{ a.u.}$

Intergalactic $B = 1 \text{ nG}$ $E = 5 \text{ PeV}$ (knee)

$\rho = 1.7 \times 10^{19} \text{ m}$ (4 % of galaxy-radius)

Circular Accelerator

Cyclotron : constant rf-frequency. Magnetic field radius ρ increases with energy. Used for smaller machines



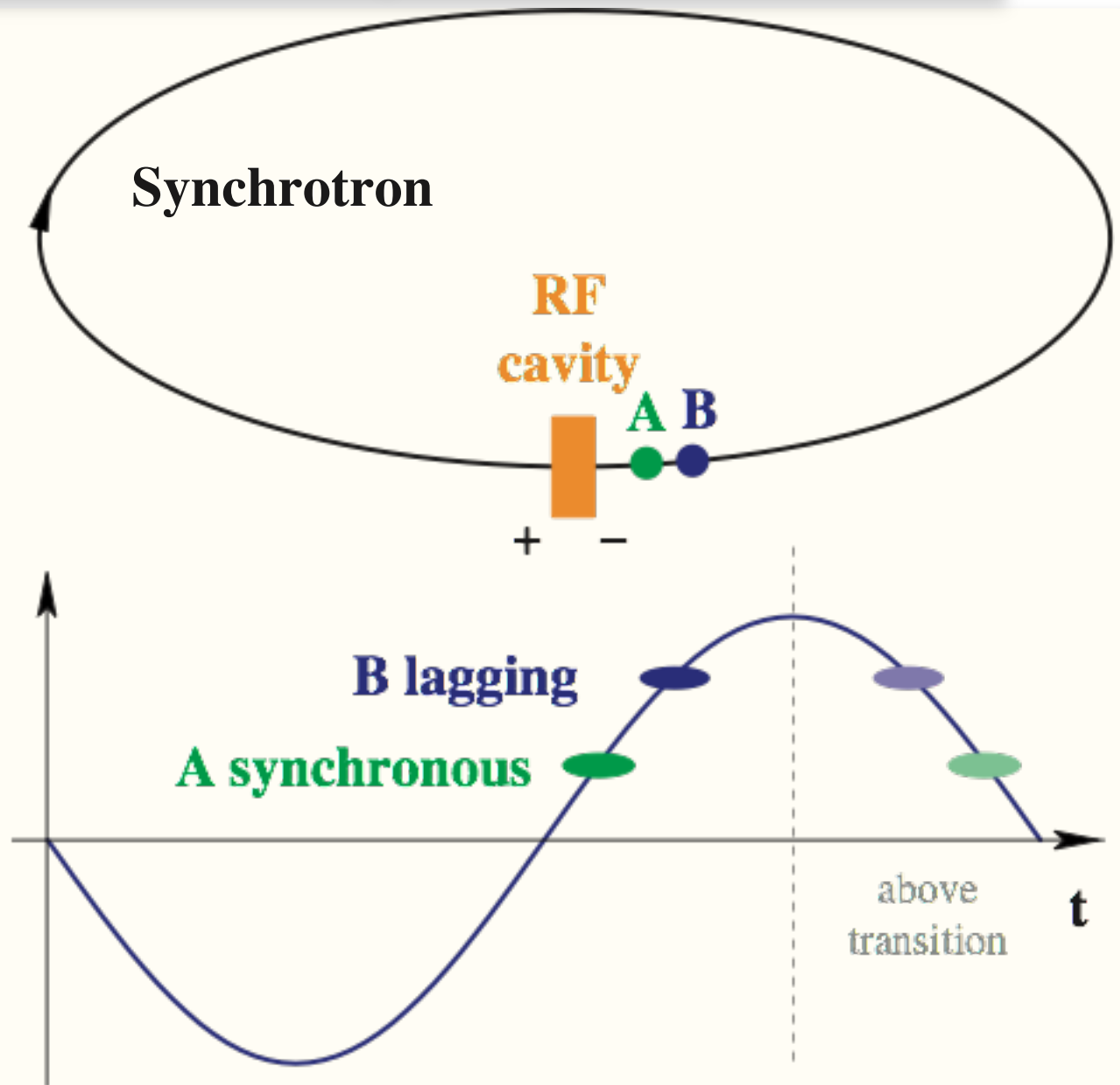
Cyclotron

- **Synchrotron** : $\rho = \text{const.}$ **B increased with energy.** RF-frequency adjusted slightly ($\beta = 0.999 \dots 1.0$). Most HEP and all CERN ring accelerators PS, SPS, LEP, LHC of this type. Principle same for e, p, heavy-ion – PS, SPS – accelerate(d) all of these, in some cases switching within seconds

Phase stability I

acceleration,
ramping up in energy :

- allow for enough RF-voltage
- ramp up magnets
- particle adjust themselves in radius and phase to gain on average the right amount of energy



LHC nominal RF parameters

Voltage at injection 8 MV

top energy 16 MV

Revolution frequency $f_{rf} = h f_{rev}$

Circumference $L = v / f_{rev} = \beta c / f_{rev}$

$h = 35\,640$ $f_{rf} = 400.7896$ MHz $L = 26658.864$ m

$f_{rev} = 11.2455$ kHz 1 turn in 88.92446 μ s

Magnets and Power Consumption

Why super conducting magnets ?

$$P = R I^2$$

LEP

B = 0.1 T LEP2 ~ 100 GeV

(half) cells with each three 11.55 m long dipole magnets

I = 4500 A together **R = 1 mΩ** **P = 20 kW / cell**

488 cells **P = 10 MW**

if we would have kept the same magnets for the LHC

LHC **B ∝ I** **B = 8.38 T**

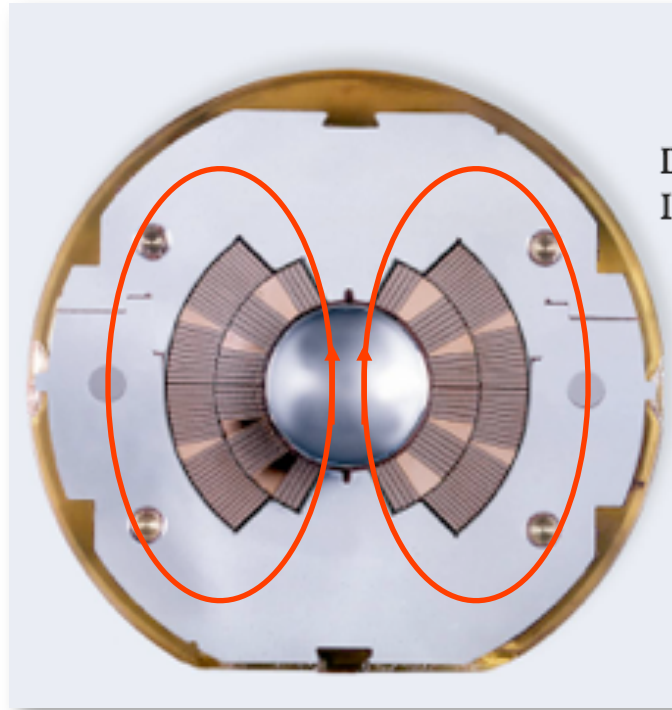
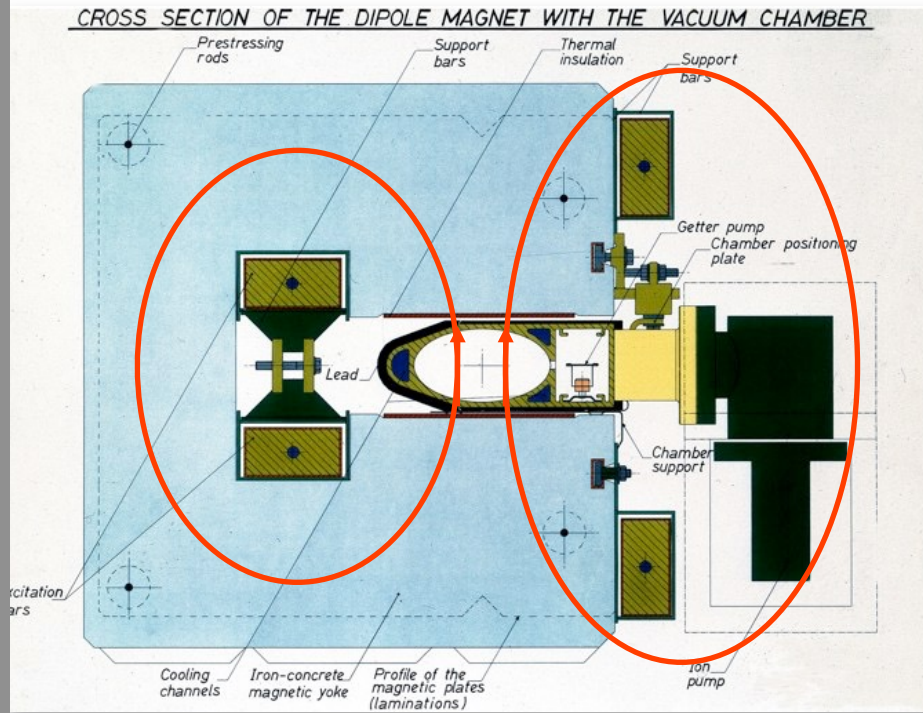
would need now **I = 280 kA** with LEP magnets **R = 1 mΩ**

P = 78 MW / cell × 488 cells **total power P = 38 GW**

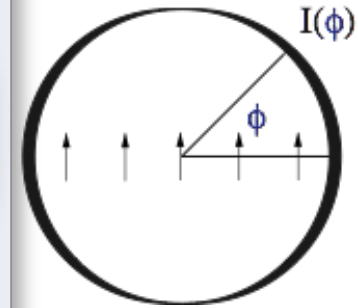
Magnet technology

warm

cold



Dipole current distribution
 $I(\Phi) = I_0 \cos(\Phi)$

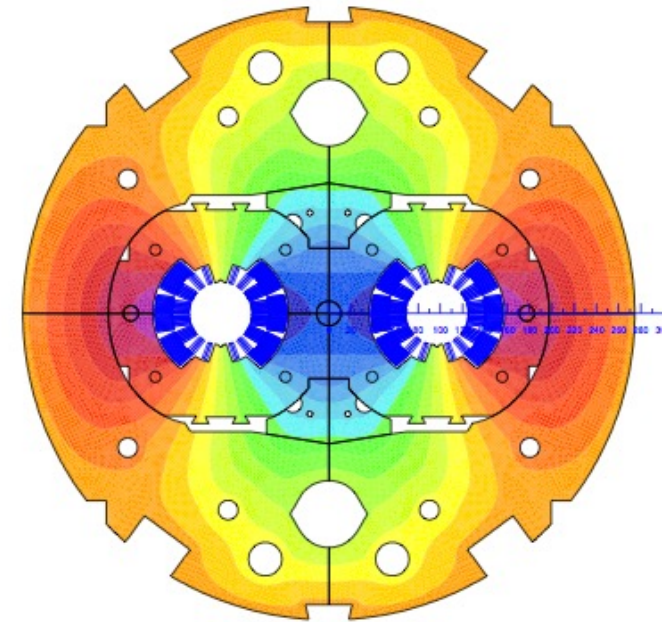
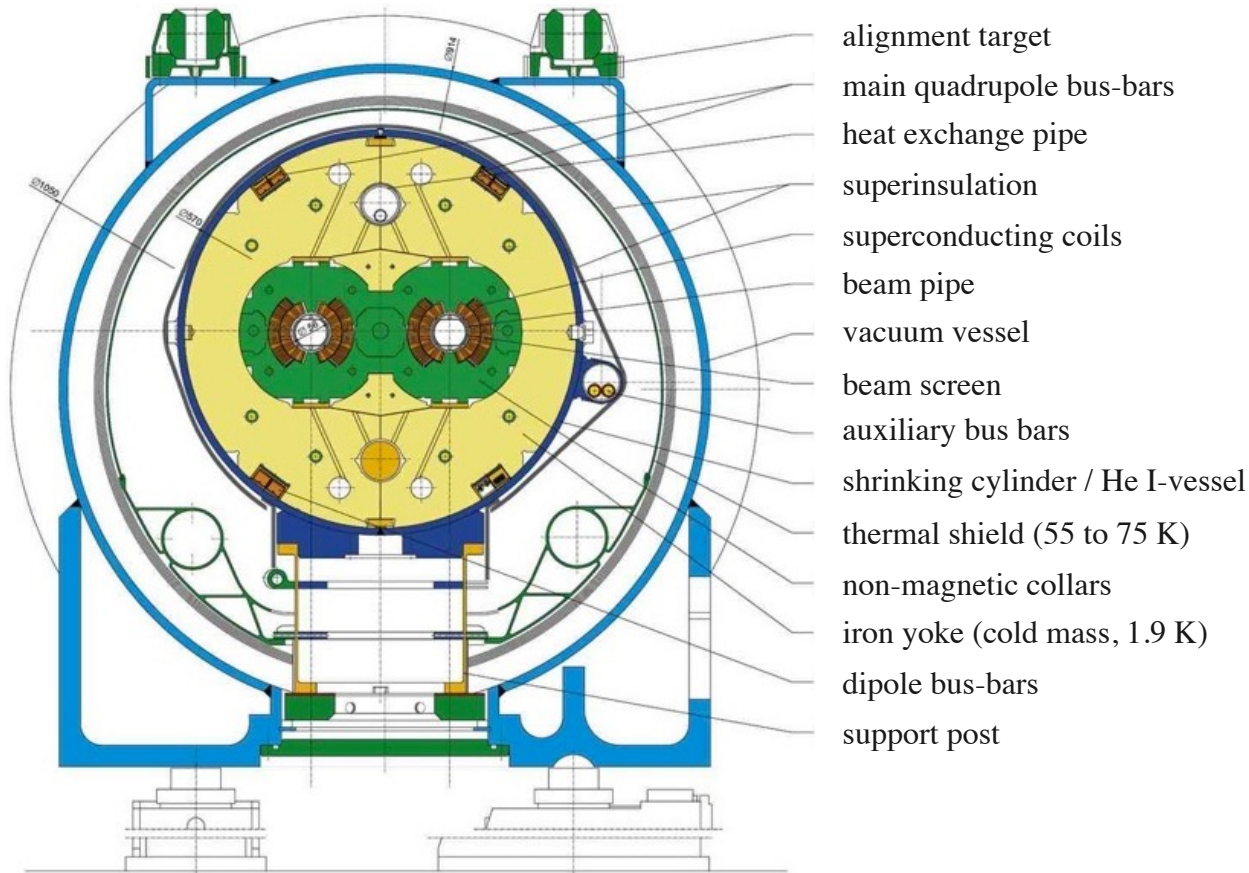


- field quality given by pole face geometry
- field amplified by Ferromagnetic material
- hysteresis and saturation ~ 2 T
- Ohmic losses for high magnet currents

- field quality given by coil geometry
- requires cooling to cryogenic temperatures
- persistent currents and snap back
- risk of magnet quenches

LHC dipole magnet

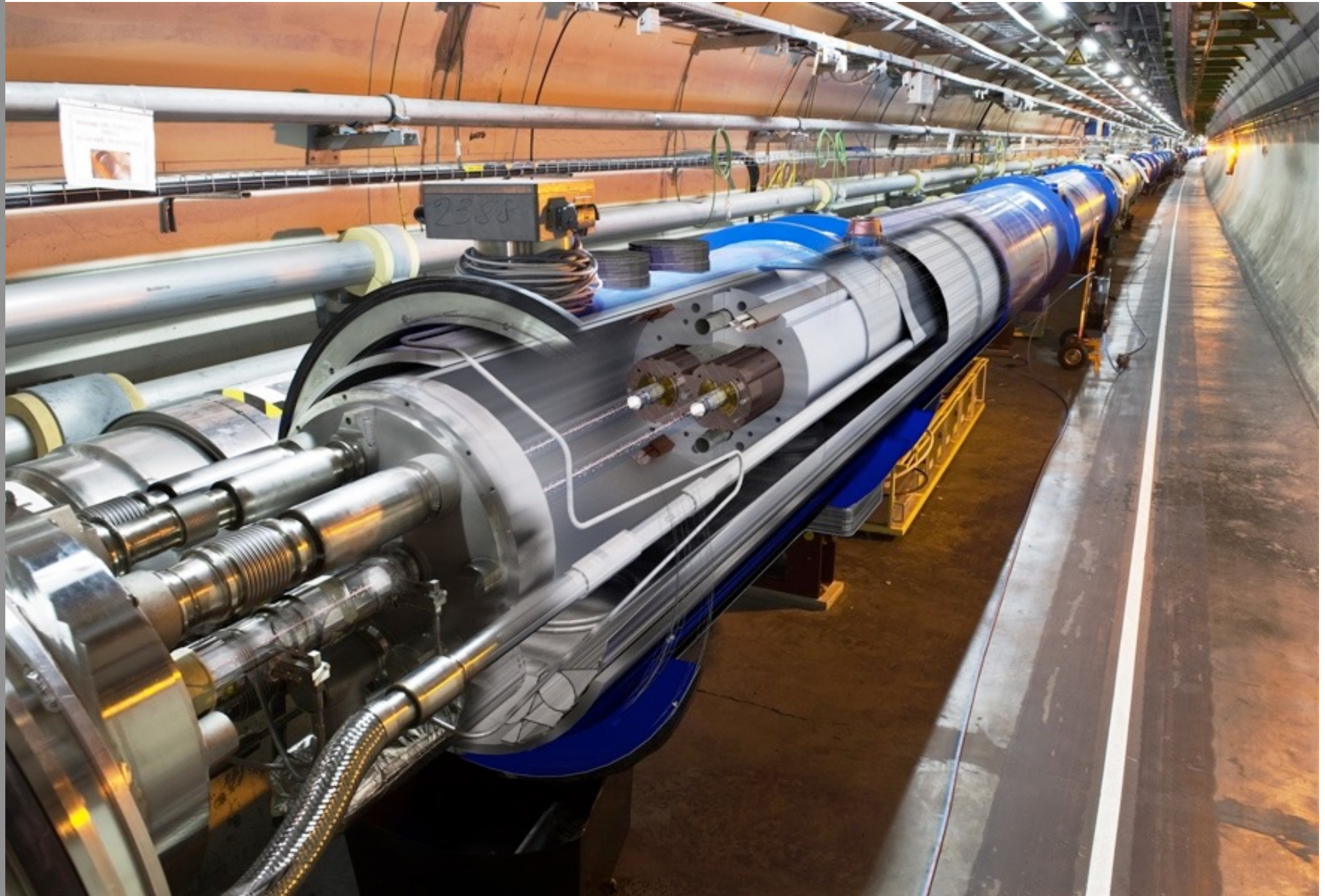
2-in-1 dipole magnet, 8.33 T field, 15 m long, mass 30 ton



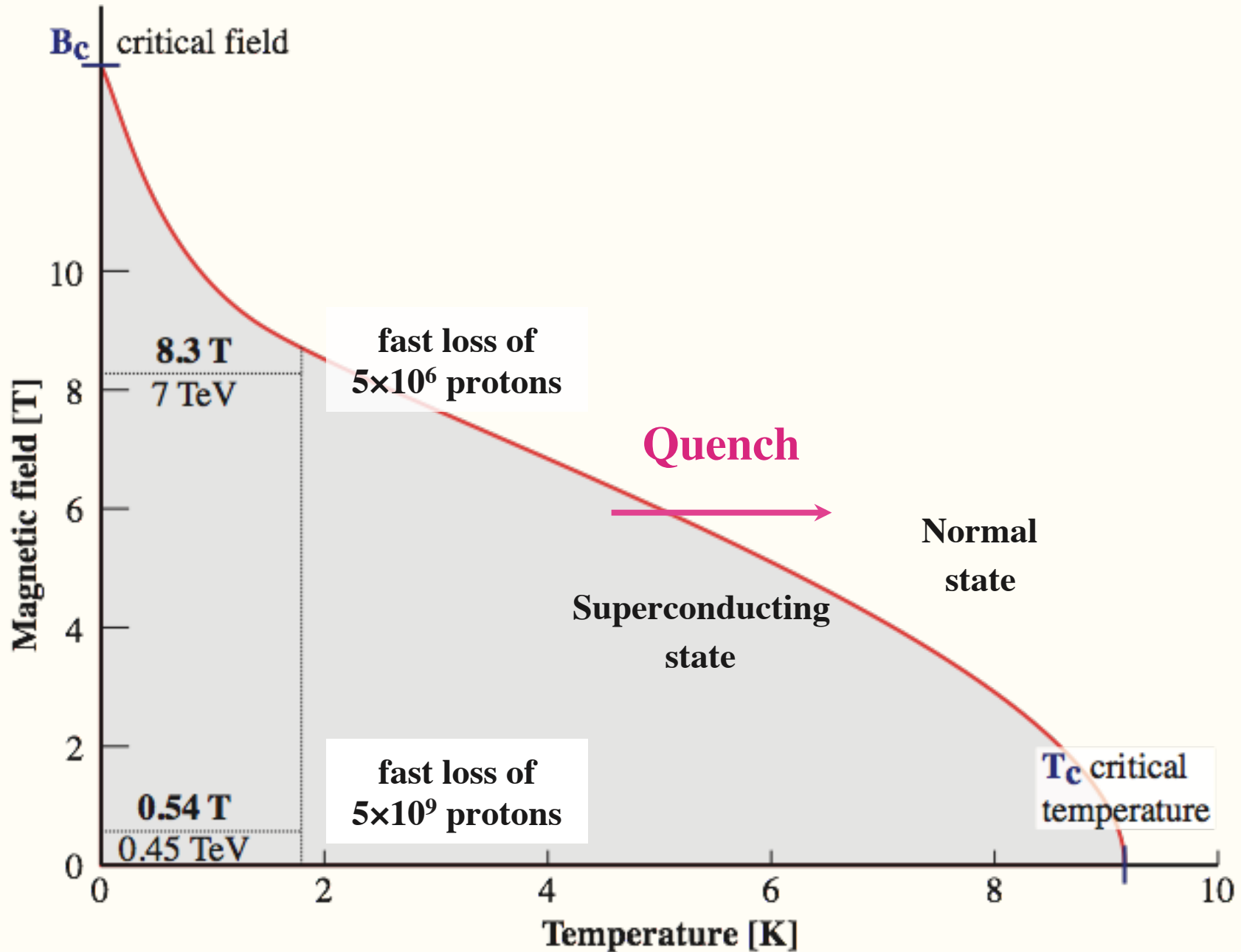
current distribution

LHC dipole magnet cross-section

LHC magnets installed in the tunnel



Operational margin of a superconducting LHC dipole



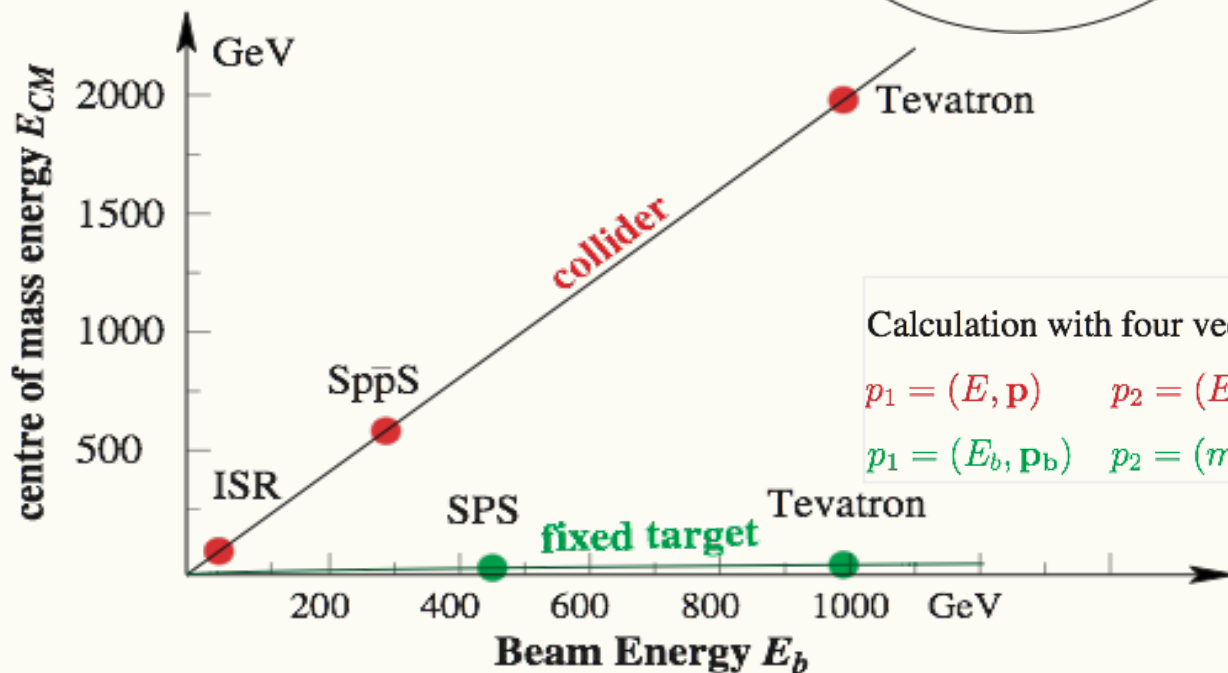
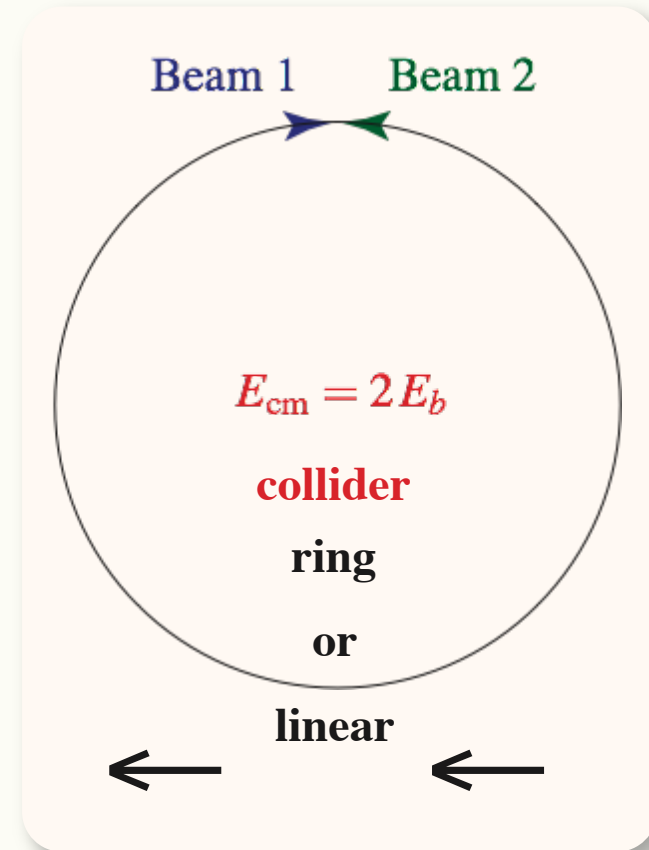
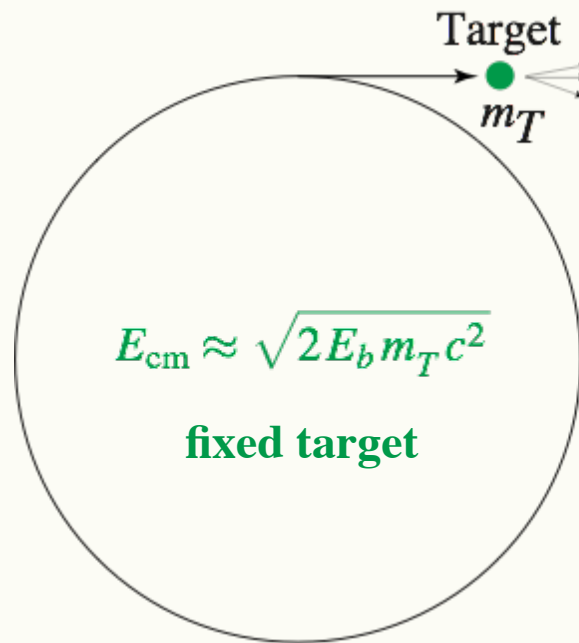
Fixed Target vs Collider

Fixed target, high energy collisions :

Energy “lost” as kinetic energy

High Energy $e+e^-$ and very high energy pp gain a lot from **colliders**

Gain for LHC is by **$\times 122$**
(14 TeV / 114.6 GeV)



Calculation with four vectors for $c = 1$ $E_{CM} = \sqrt{s}$ $s = (p_1 + p_2)^2$

$p_1 = (E, \mathbf{p})$ $p_2 = (E, -\mathbf{p})$ $s = 2m^2 + 2E^2 + 2p^2 = 4E^2$ collider

$p_1 = (E_b, \mathbf{p}_b)$ $p_2 = (m_T, \mathbf{0})$ $s = m_b^2 + m_T^2 + 2m_T E_b$ fixed target

Primary cosmic ray spectrum

E spectrum falls as $E^{-2.7}$
 to knee at $E \approx 5 \times 10^{15}$ eV
 $= 5 \times 10^6$ GeV
 ~ 1 particle/m² and year
 origin galactic

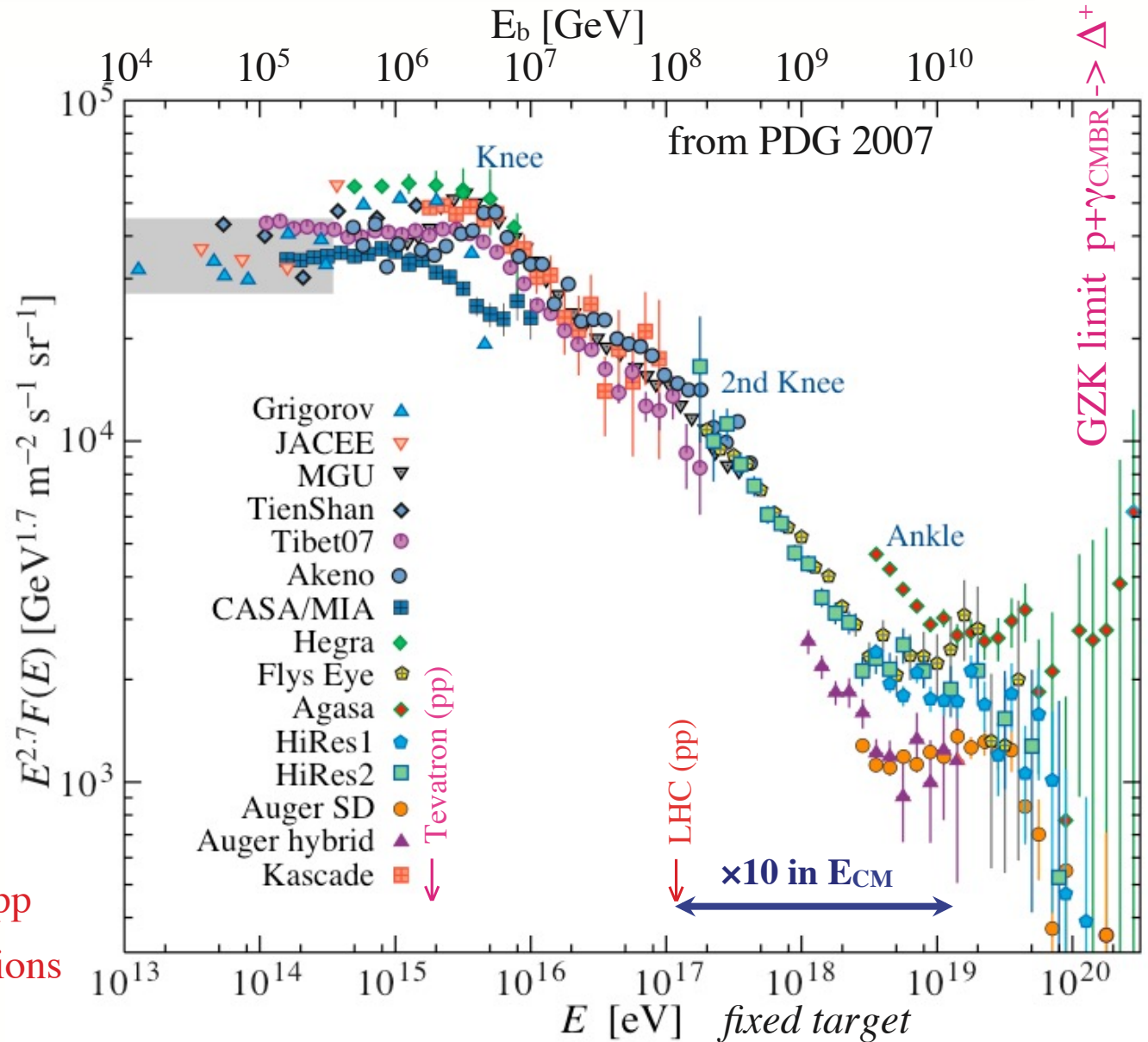
above $\sim E^{-3}$

back to $E^{-2.7}$ at very
 highest energies

conversion to E_{cm}

E_b [eV]	E_{cm} [TeV]
10^{13}	0.137
10^{15}	1.370
10^{17}	13.70
10^{19}	137.0
10^{21}	1370.

\approx LHC pp
 \leftarrow LHC ions



Nature has much larger and more powerful **cosmic accelerators** than we can ever built.

With colliders we can get to these collision energies in clean laboratory conditions.

The LHC already gets us to within 1-2 orders of magnitude of the very highest cosmic rays.

Luminosity and collision rates

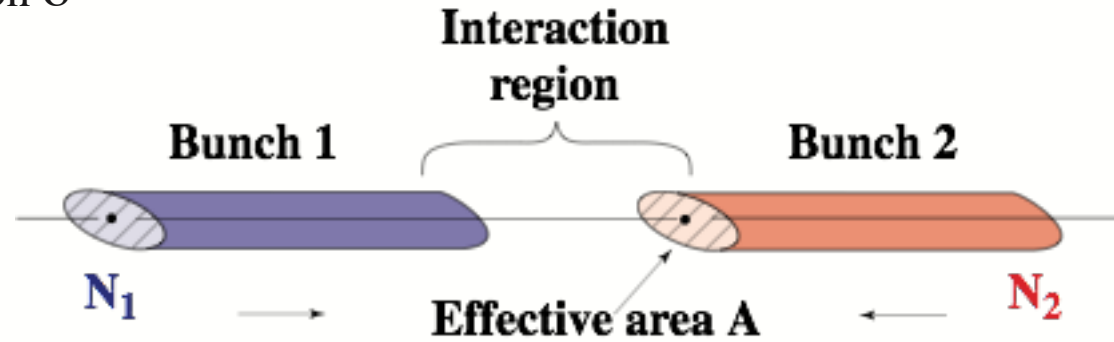
Event rate for process with cross section σ

$$\dot{n} = \mathcal{L} \sigma$$

Luminosity from bunch

crossings at frequency $f = f_{\text{rev}} n_b$

$$\mathcal{L} = \frac{N_1 N_2 f}{A}$$



for Gaussian bunches with rms sizes $\sigma_x \sigma_y$ $A = 4 \pi \sigma_x \sigma_y$

High Luminosity : $N \uparrow$ collide many particles, $A \downarrow$ squeezed in small bunches

LHC 1.15×10^{11} protons, $n_b = 2808$ ($f \uparrow$ crossings at 25 ns intervals)

Beams squeezed using strong

large aperture quadrupoles

around the interaction points

from ~ 0.2 mm to

$$\sigma_x = \sigma_y = 17 \mu\text{m}$$



$$\langle \beta \rangle_{\text{arc}} = 80 \text{ m}$$

$$\beta_{\text{IP}} = 0.5 \text{ m}$$

Rare new processes, like Higgs production can have very small cross section,

like $1\text{fb} = 10^{-39}\text{cm}^2$. LHC designed for very high Luminosity $\mathcal{L} = 10^{34} \text{cm}^{-2}\text{s}^{-1}$

Event rate for such rare processes : ~ 1 new particle every 28h.

Instead pp $\sigma_{\text{tot}} \approx 0.1$ barn 30 / crossing

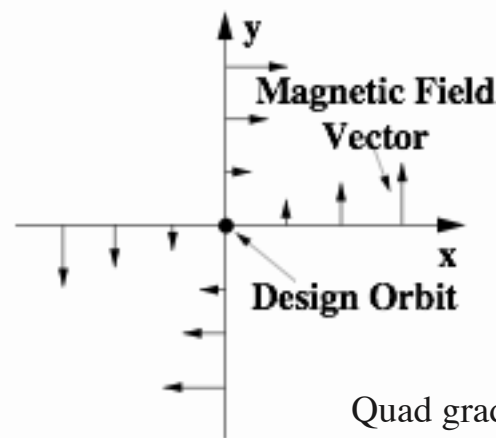
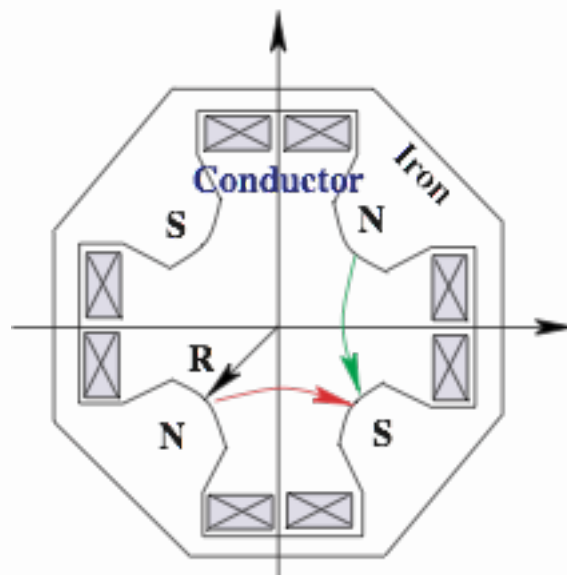
Alternate gradient focusing

Quadrupole lens focusing in x, defocusing in y or vice versa

$$\mathbf{F} = e (\mathbf{v} \times \mathbf{B})$$

here

$$\begin{aligned} \mathbf{F} &= e (0, 0, v) \times (B_x, B_y, 0) \\ &= e (-v B_y, +v B_x, 0) \end{aligned}$$



$$B_x = k y$$

$$B_y = k x$$

$$B_z = 0$$

$$\nabla \times \mathbf{B} = \mathbf{0}$$

Quad gradients in the LHC
 $K = 1/B_0 \partial B_y / \partial x \approx 200 \text{ T/m}$

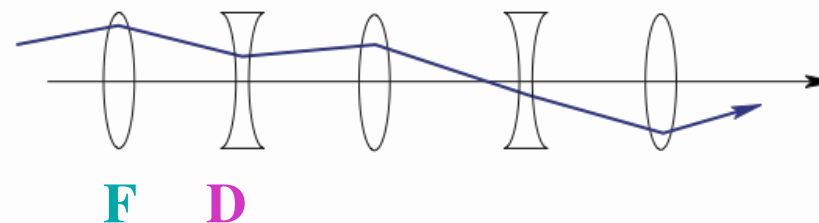
Combine F D

Defocusing when at

small amplitude

Overall focusing

alternate gradient focusing



Normal (light) optics :

Focal length of two lenses

at distance D

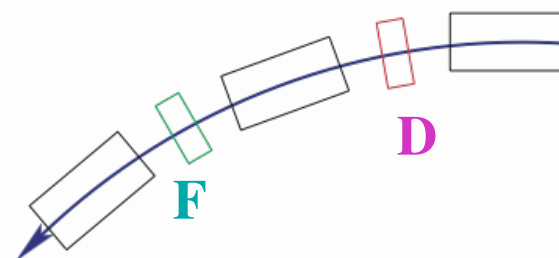
$$1/f = 1/f_1 + 1/f_2 - D/f_1 f_2$$

is overall focusing

with $1/f = D/f^2$

for $f = f_1 = -f_2$

together with bending magnets FODO lattice



N. C. Christofilos, unpublished manuscript in 1950 and patent

Courant, Snyder in 1952, Phys. Rev. 88, pp 1190 - 1196 + longer review in [Annals of Physics 3 \(1958\)](#)

Betatron motion

Equation of motion of particles in a ring (with bending fields) **and quadrupoles** (field gradients $\propto \partial B / \partial r$)

In both transverse planes, here written with x for x, y : known as Mathieu-Hill equation

$$x''(s) + k(s) x(s) = 0, \quad \text{derived in 1801 to describe planetary motion}$$

Generalised oscillator equation with position dependent, periodic restoring force $k(L+s) = k(s)$ given by the quadrupole gradients (+ the small weakly focusing bending term in the ring plane)

Solution : $x(s) = \sqrt{\epsilon \beta(s)} \cos(\mu(s) + \phi)$

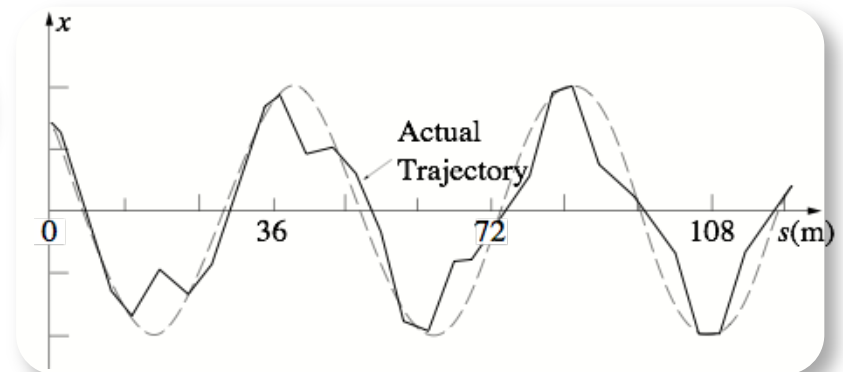
Phase advance

Lyapunov-Floquet Transformation

$$\mu(s) = \int_0^s \frac{ds}{\beta(s)}$$

Tune # of betatron oscillations

$$Q = \mu / 2\pi$$



motion $x/\sqrt{\beta}$ plotted with phase advance normalised coordinates - becomes simple cos

$\beta(s)$ **beta function**, describes the focusing properties of the magnetic lattice

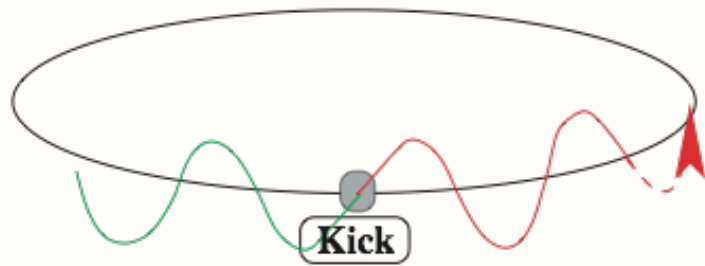
\mathcal{E} invariant, together with $\beta(s)$ amplitude. "single particle emittance"

Motion conveniently described in phase space (x, x') where $x' = p_x / p$ and linear optics elements as matrices ; with simple case for M, applies for IP to IP

$$\begin{pmatrix} x(s) \\ x'(s) \end{pmatrix} = \mathbf{M} \begin{pmatrix} x(s_0) \\ x'(s_0) \end{pmatrix} \quad \mathbf{M} = \begin{pmatrix} \cos 2\pi Q & \beta \sin 2\pi Q \\ -\frac{1}{\beta} \sin 2\pi Q & \cos 2\pi Q \end{pmatrix}$$

Accelerator design : starts with magnet lattice based on linear beam optics ; MAD program

Orbit stability and tune



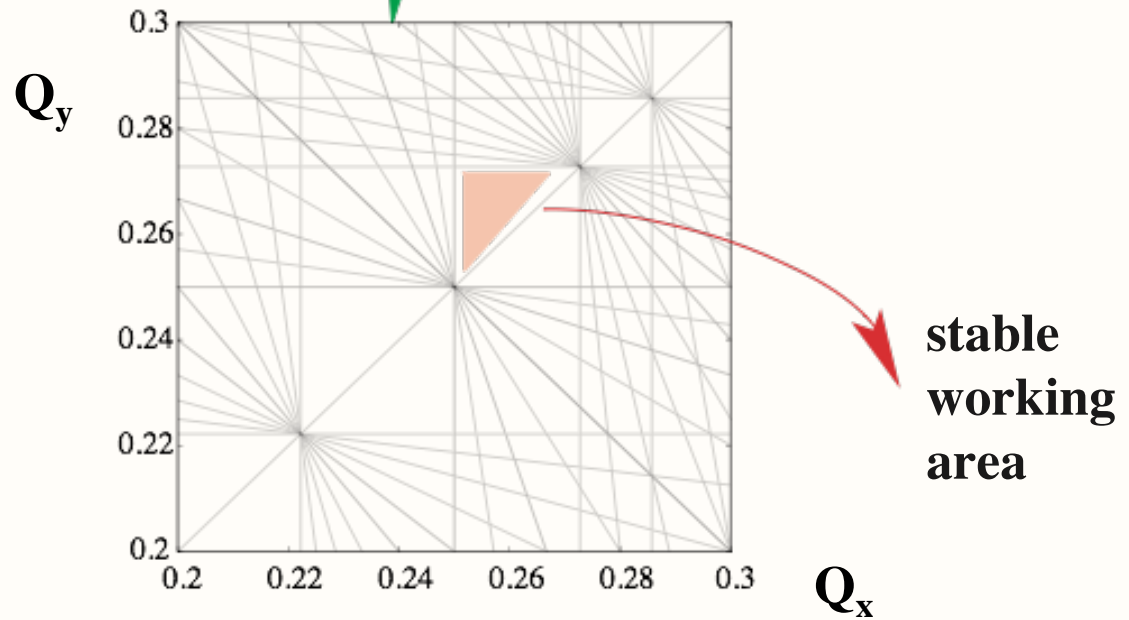
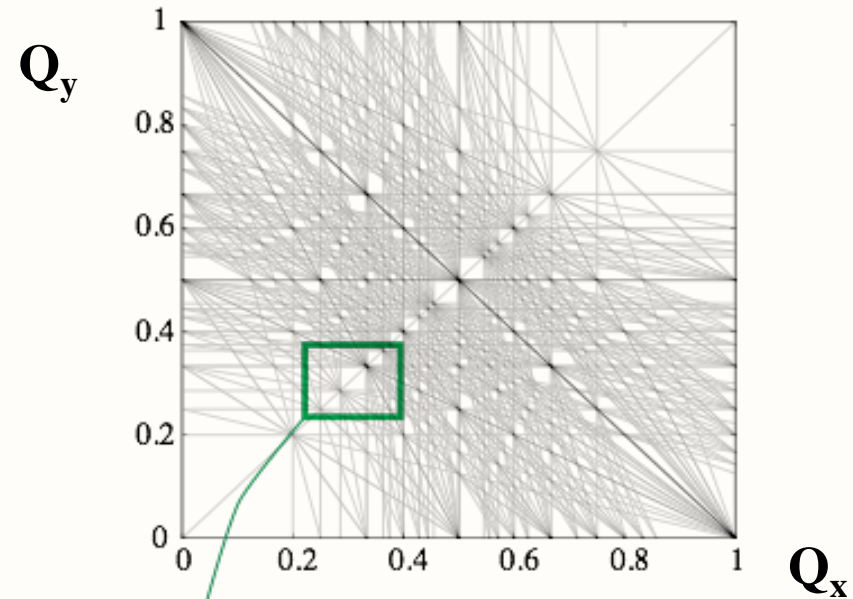
Misalignments and dipole field errors

→ **orbit perturbations**

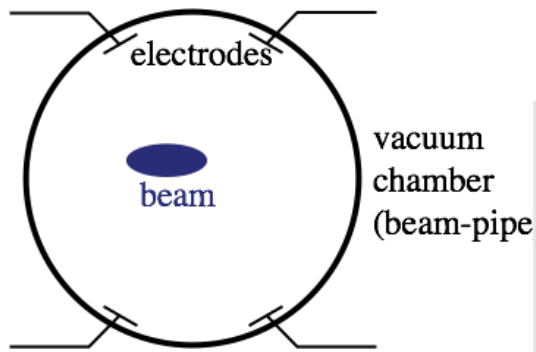
would add up on successive turns
for integer tune $Q = N$

Higher order field errors,
Quad., Sext. perturbations.
Avoid simple fractional tunes
 $nQ_x + m Q_y + m Q_s = \text{int.}$

Minimise field and alignment
errors

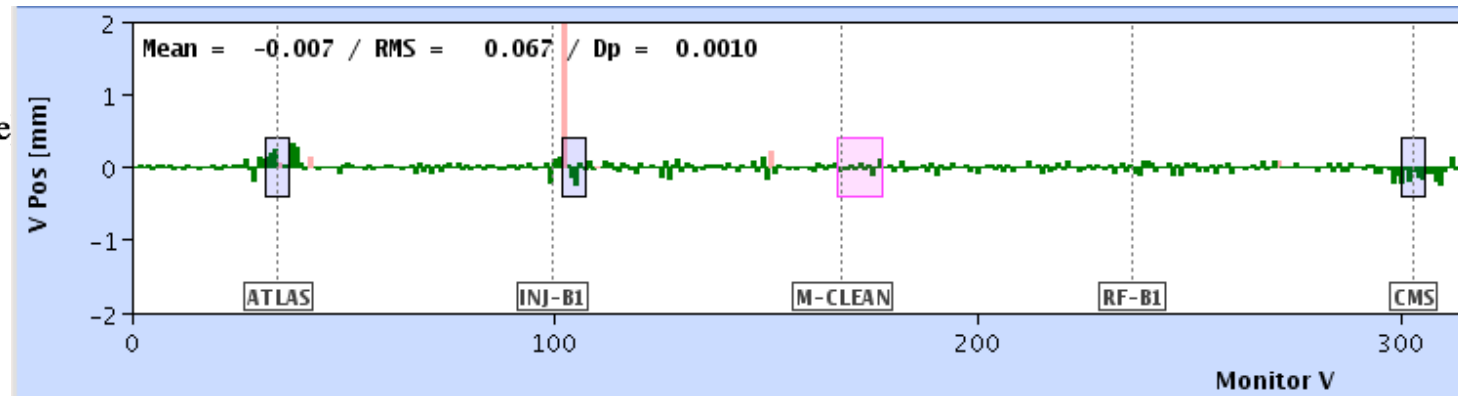


Orbit, tune measurement and peak beam current



Beam Pickup Monitor

vertical orbit, June 2011, 1st half of LHC shown



$\langle I_b \rangle$ average ring
and
 \hat{I} local peak
current

$$\hat{I} = \frac{\langle I_b \rangle L}{\sqrt{2\pi} \sigma_z}$$

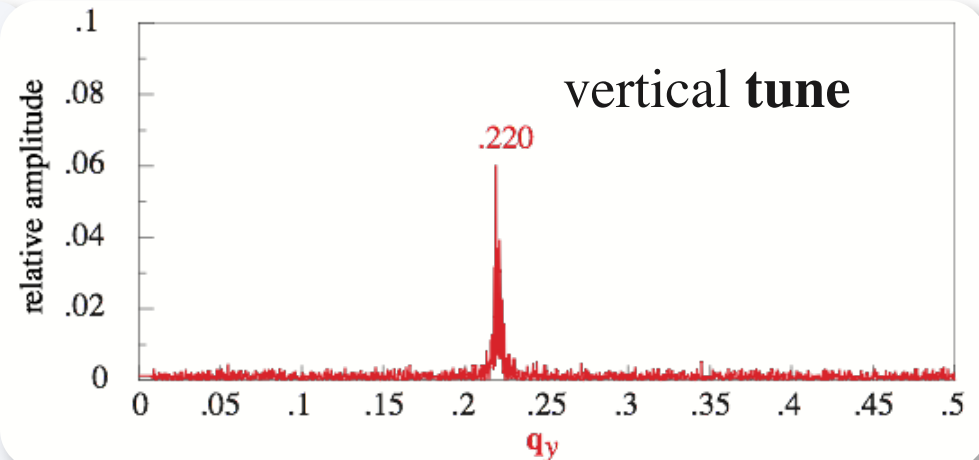
Typical numbers, for a single bunch $\langle I_b \rangle = n e f_{\text{rev}}$

LEP	$n = 4 \times 10^{11}$	$\langle I_b \rangle = 0.72 \text{ mA}$	$\sigma_z = 2 \text{ cm}$	$\hat{I} = 960 \text{ A}$
LHC	$n = 1.15 \times 10^{11}$	$\langle I_b \rangle = 0.21 \text{ mA}$	$\sigma_z = 7.55 \text{ cm}$	$\hat{I} = 73.2 \text{ A}$

$f_{\text{rev}} = 11245 \text{ kHz}$, $L = 26658.9 \text{ m}$

Bunch peak currents are many Amperes !
Strong signals, used to monitor beam position and oscillations

Also source of undesirable effects :
wake fields, heating, instabilities



Transverse beam size and emittance

consider : beam of many particles on stable orbit and

simple case : dispersion and slope $\beta' = 0$ by default at IP - relevant for experiments

beam size, r.m.s.	$\sigma(s) = \sqrt{\varepsilon\beta(s)}$
beam divergence, r.m.s.	$\theta(s) = \sqrt{\varepsilon/\beta(s)}$
product	$\varepsilon = \sigma(s)\theta(s)$

β - function : local machine quantity - focusing of lattice

Emittance ε : beam quantity - the average action

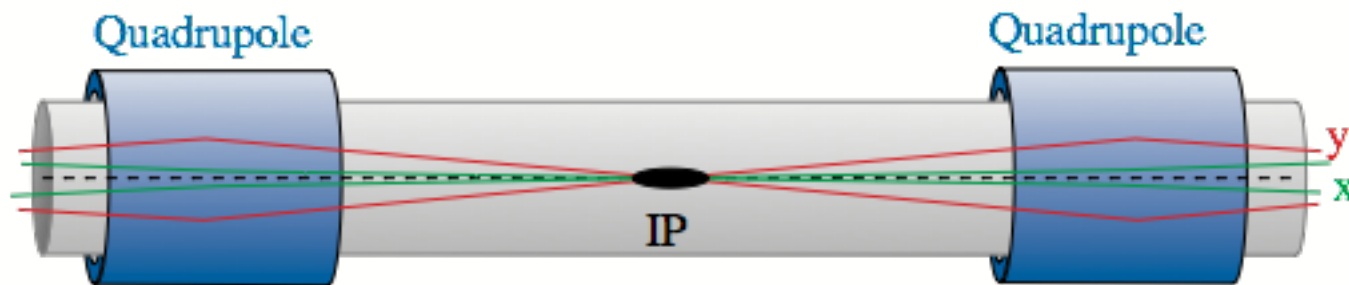
related to phase space density or kind of beam temperature

given by initial conditions (injected beam)

or equilibrium of quantum excitation and damping - 2nd lecture

in ideal machine : x, y, z motion uncoupled, 3 emittances $\varepsilon_x, \varepsilon_y, \varepsilon_z$

IP: squeeze β to a minimum, called β^* \Rightarrow maximum of divergence, needs aperture



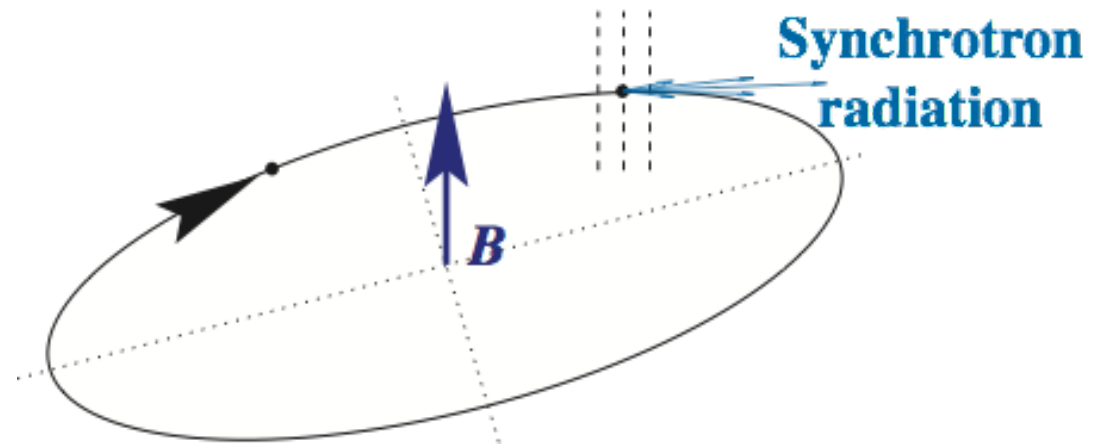
LHC $\varepsilon_N = \varepsilon \beta \gamma = 3.75 \mu\text{m}$, at top $E_b = 7 \text{ TeV}$: $\varepsilon = 0.503 \text{ nm}$, $\beta^* = 0.55 \text{ m}$, $\sigma^* = 16.63 \mu\text{m}$, $\theta^* = 30 \mu\text{rad}$

Standard Synchrotron Radiation

$$E_c = \frac{3}{2} \frac{\hbar c \gamma^3}{\rho} = 2.96 \times 10^{-7} \text{ eV m} \frac{\gamma^3}{\rho}$$

$$U_0 = \frac{e^2}{3\epsilon_0} \frac{\gamma^4}{\rho} \approx 6.0317 \cdot 10^{-9} \text{ eV m} \frac{\gamma^4}{\rho}$$

$$P_b = \frac{U_0 I_b}{e}$$



		E GeV	γ	q m	U_0 MeV	E_c keV	τ_d s	N 10^{12}	I mA	P_b MW	B T
RHIC	Au	A×100	107.4	242.8	21×10^{-6}	1.5×10^{-6}	4.9×10^6	0.06	60	1.3×10^{-12}	3.42
LHC	p	7000	7460.5	2804	0.0067	0.044	61729	646	1163	0.0072	8.33
LEP1	e	45.6	89237	3026	126	69.5	23×10^{-3}	2.22	4	0.5	0.05
LEP2	e	104.5	20450 1	3026	3490	836	1.9×10^{-3}	2.8	5	18	0.115

Same beam energy E and radius ρ : electron instead of proton $U_0 \sim \gamma^4 : (m_p/m_e)^4 = 1.13 \times 10^{13}$

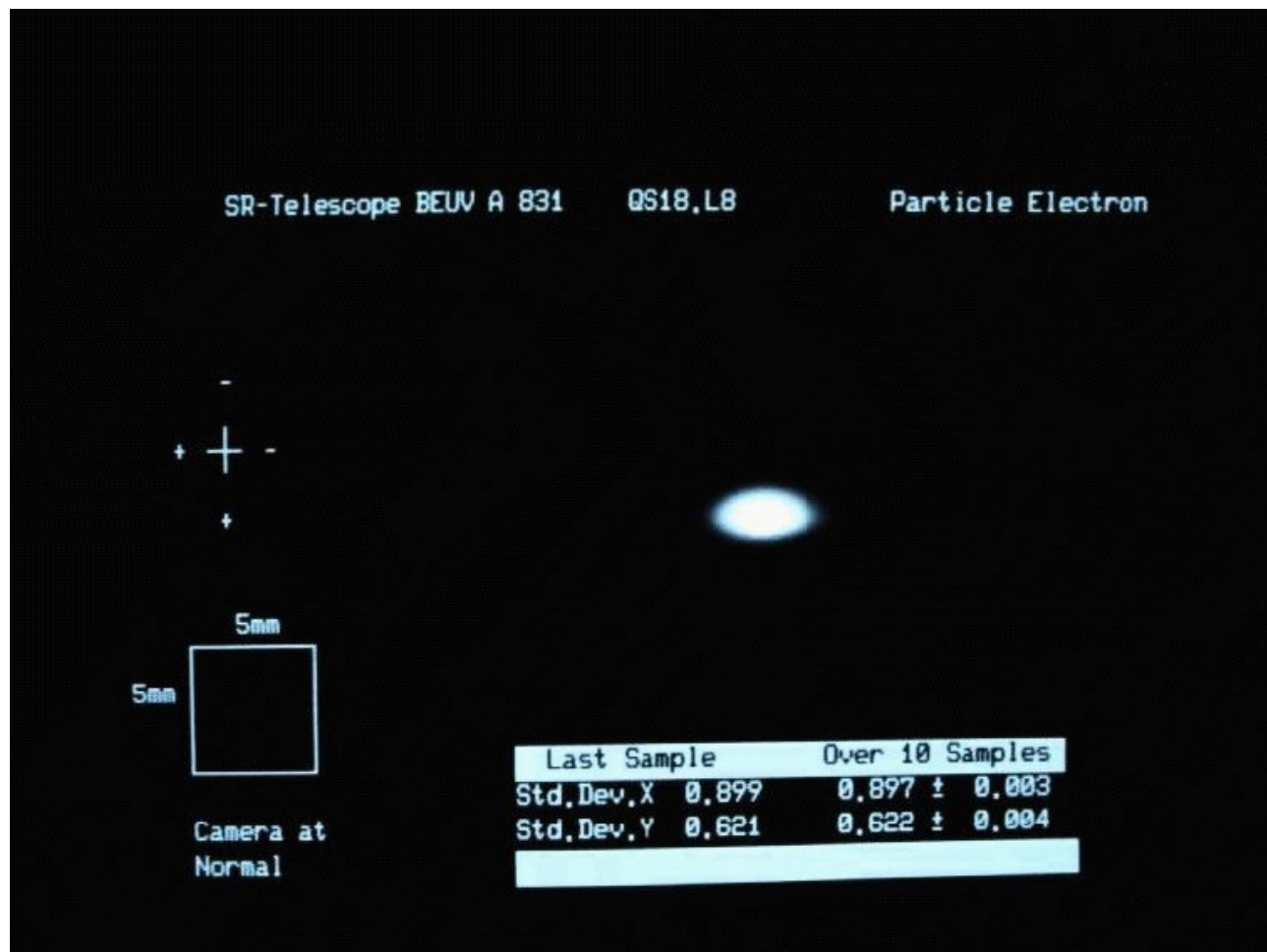
Electrons, $E \gg 100$ GeV needs linear collider (ILC / CLIC)

Damping time E / U_0 turns or $\tau_d = t_{rev} E / U_0$ revolution time LEP/LHC $t_{rev} = 88.9 \mu\text{s}$

Gold ions Au^{79+} $A=197$ $\langle E_\gamma \rangle = 8/(15\sqrt{3}) E_c$ $8/(15\sqrt{3}) \approx 0.308$

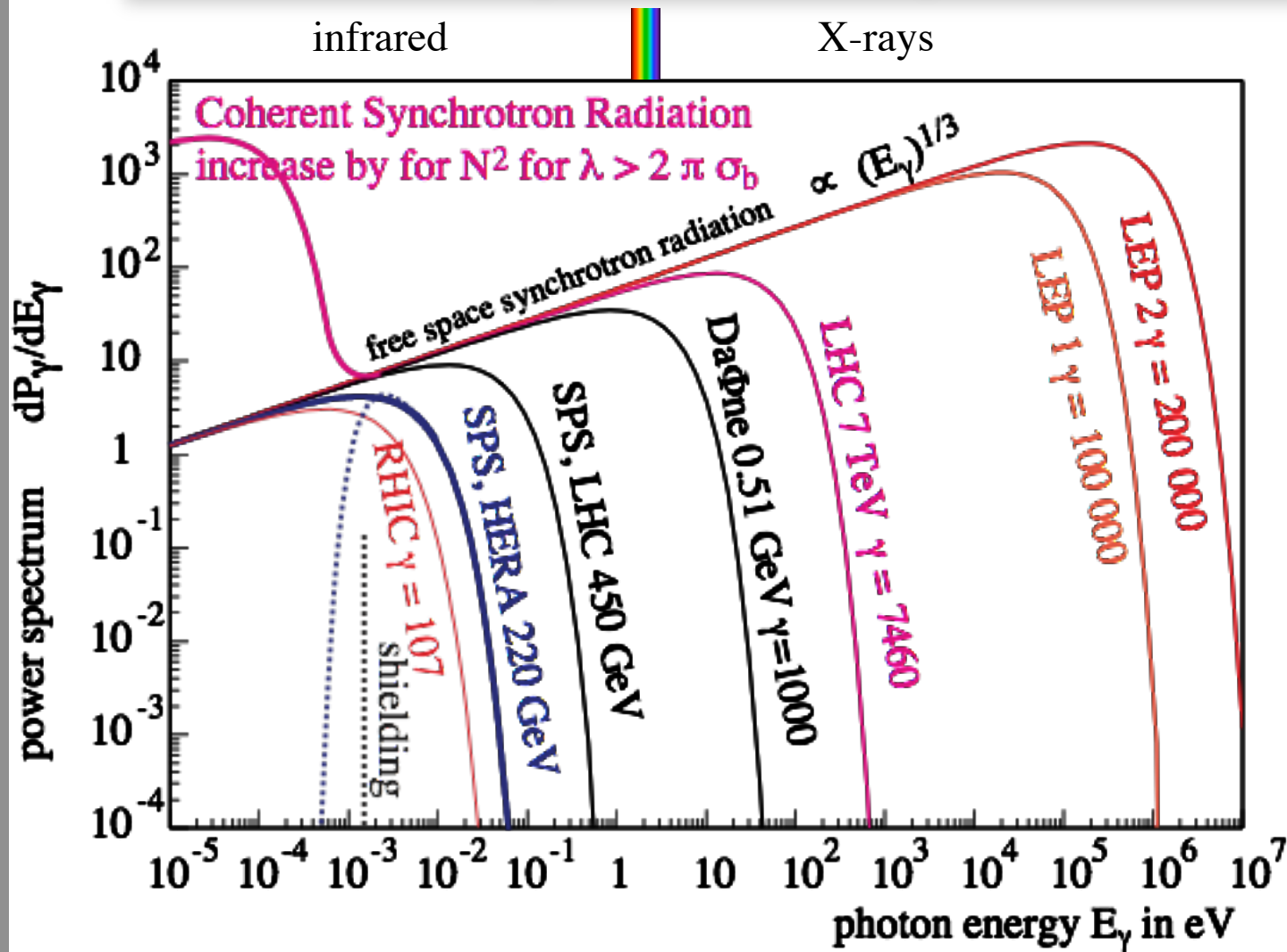
Synchrotron light monitor

**Picture from LEP.
Typical transverse
rms beam size 0.15
mm vertical 1.5
mm horiz.**



**Mirror, small slit, telescope and camera : beams continuously visible.
Now also used for protons in the LHC.**

Power Spectrum, Free space, Cutoff and CSR



$$\frac{f_{\text{cutoff}}}{f_{\text{rev}}} = \sqrt{\frac{2}{3}} \left(\frac{\pi \rho}{h} \right)^{3/2}$$

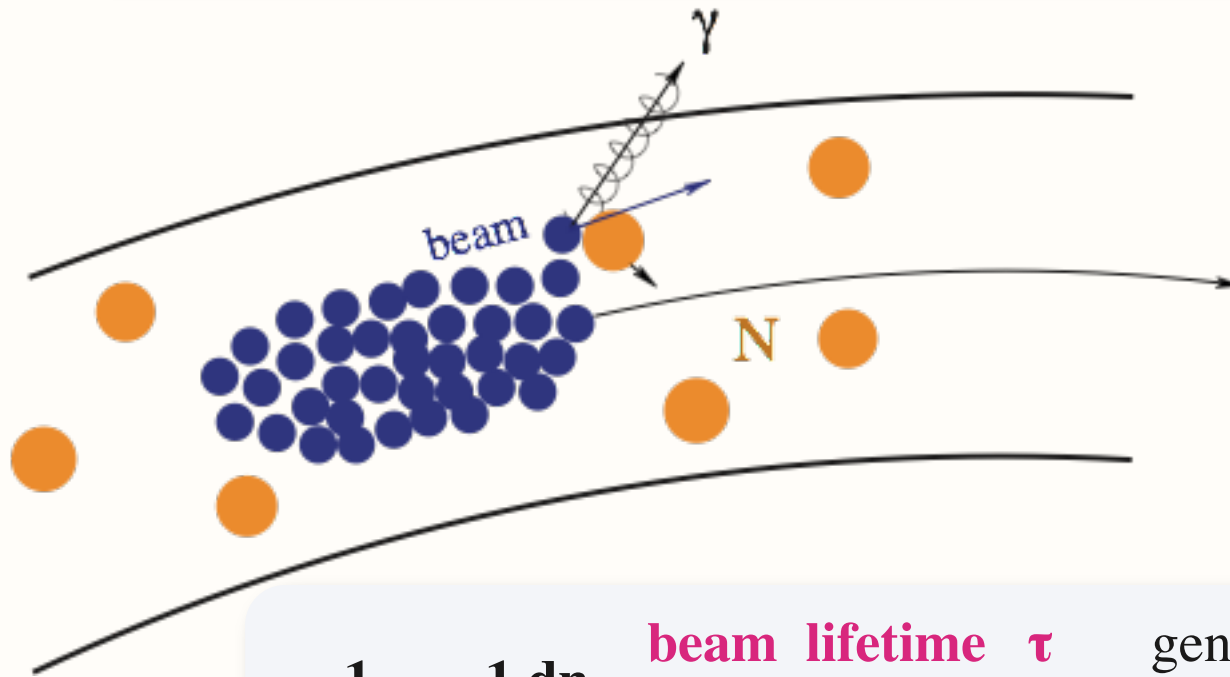
ρ bending radius
 h chamber height
 cutoff relevant
 for $\gamma \approx 100$

12 orders of magnitude
 in E_γ and λ
 10^{-5} eV $\lambda = 0.124$ m
 10^{+7} eV $\lambda = 124$ fm

Effects which can modify the low energy, long wavelength spectrum :

- i) **Coherent Synchrotron Radiation CSR** increases radiation and loss
 - ii) **Boundary conditions - cutoff by conducting chamber** decreases radiation and loss
- Energy Loss of Gold Ions in RHIC, [EPAC 2008](#)

Vacuum, beam Gas - lifetime



Beam blow up, core + halo
Background to experiments
loss, radiation, beam and
Luminosity lifetime

Minimize effect :
Good vacuum
O(nTorr or 10^{-9} mb)
Collimation

$$\frac{1}{\tau} = - \frac{1}{n} \frac{dn}{dt}$$

beam lifetime τ general expression
average time between collisions leading to beam loss
inverse normalised loss rate

$$p = 1 \text{ ntorr} = 1.33 \times 10^{-7} \text{ Pa}$$

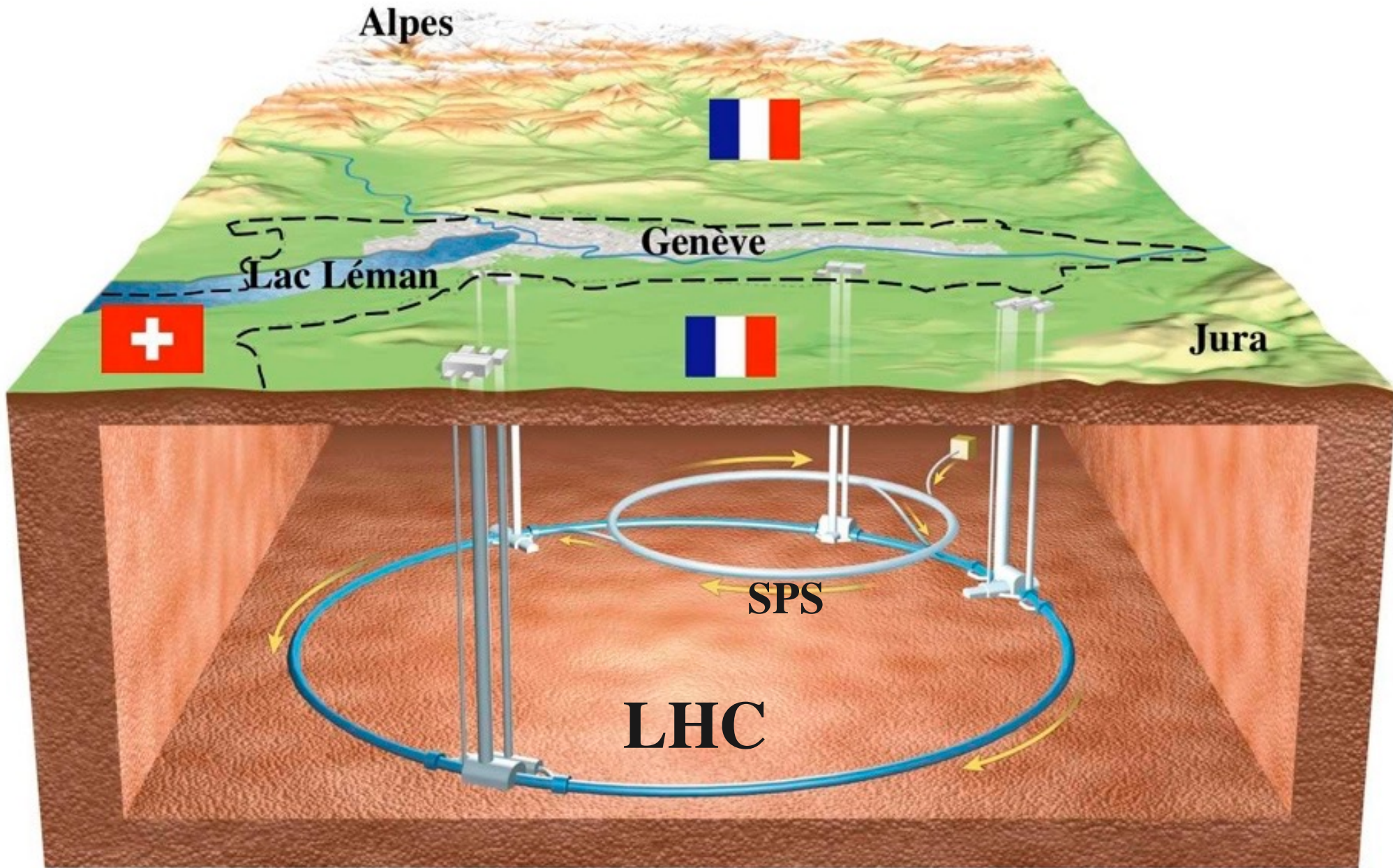
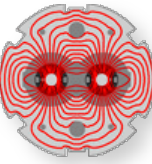
$$\rho_m = \frac{p}{kT} = 3.26 \times 10^{13} \text{ molecules / m}^3$$

typical cross section $\sigma = 6 \text{ barn} = 6 \times 10^{-28} \text{ m}^2$

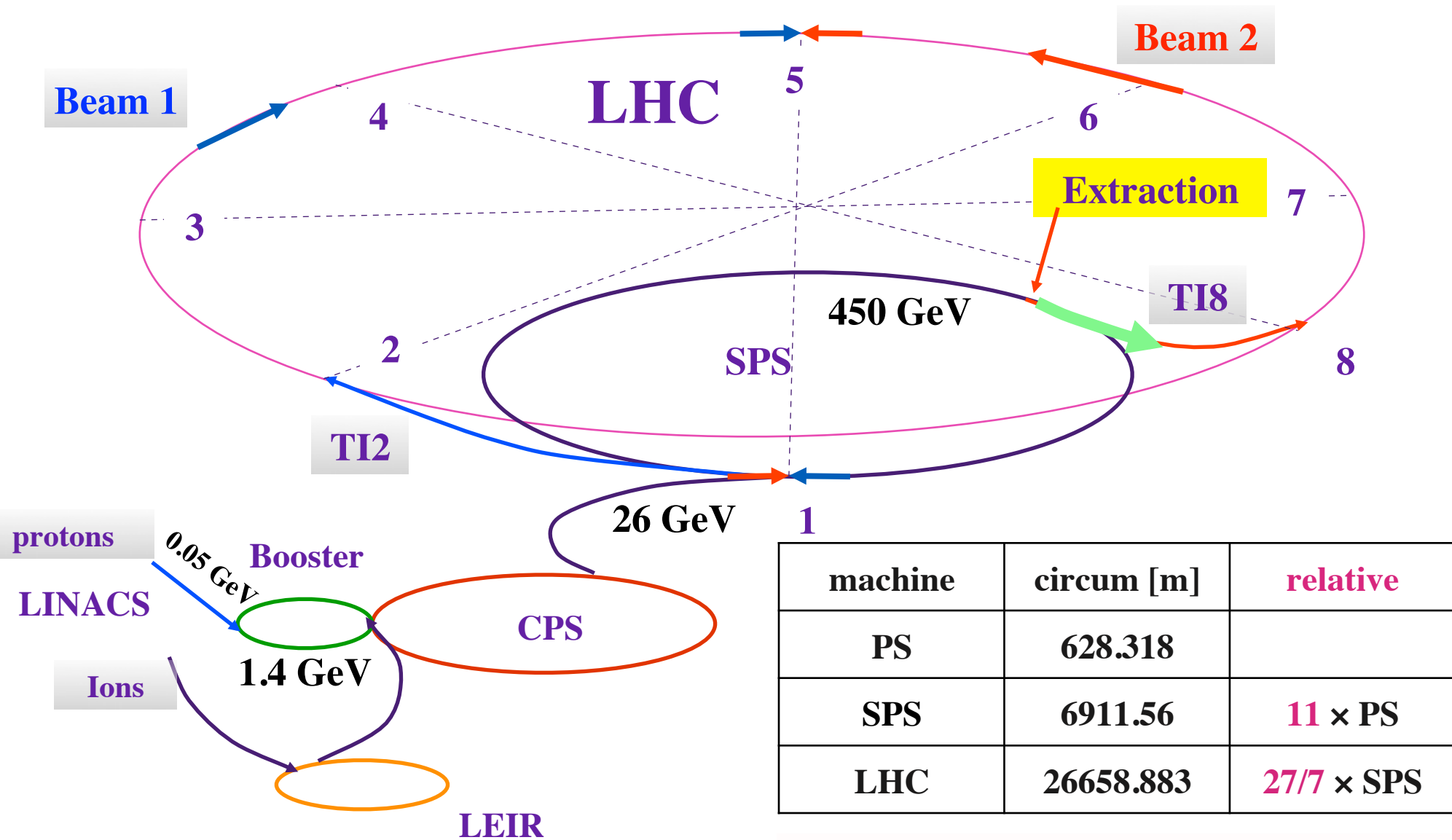
collision probability $P_{\text{coll}} = \sigma \rho_m = 1.96 \times 10^{-14} / \text{m}$

$$\tau = \frac{1}{P_{\text{coll}} c} = 1.7 \times 10^5 \text{ s} = 47 \text{ hours} \quad \text{for } v \approx c$$

Examples from CERN with the LHC



The CERN accelerator complex : injectors and transfer

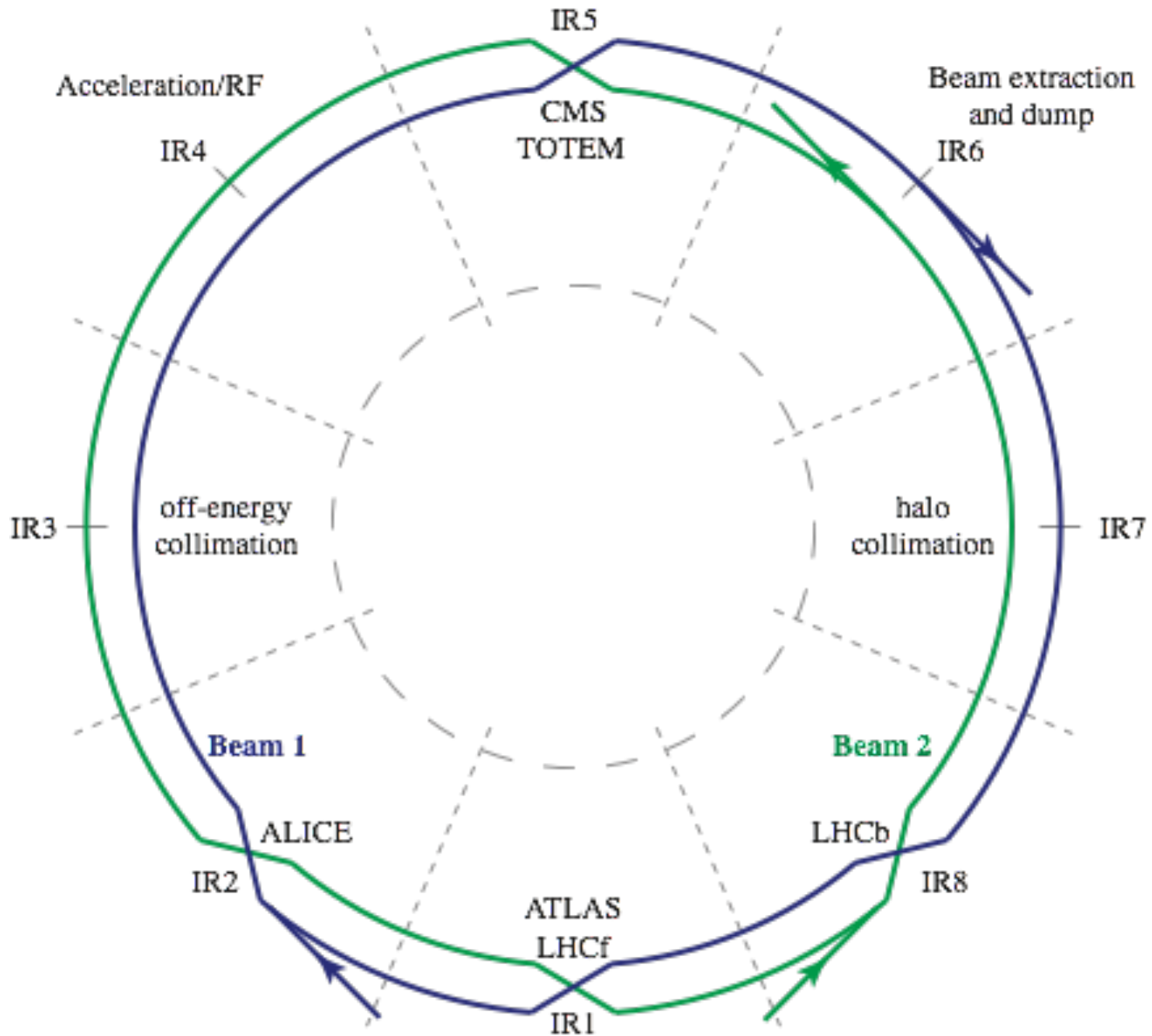
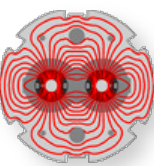


machine	circum [m]	relative
PS	628.318	
SPS	6911.56	11 × PS
LHC	26658.883	27/7 × SPS

simple rational fractions for **synchronization** based on a single frequency generator at injection

Beam size of protons decreases with energy : area $\sigma^2 \propto 1 / E$
 Beam size largest at injection, using the full aperture

Layout of the LHC



10 September 2008

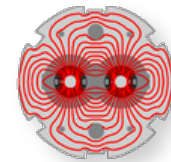


10:30 beam 1 3 turns

15:00 beam 2 3 turns

22:00 beam 2 several 100 turns





- main LHC challenge : damage potential --- increase safely (slowly) the intensity
- enormous stored energy : nominal is 10 GJ in magnets, 362 MJ in beam; 0.7 MJ melts 1kg Cu
- currently 3.3 GJ in magnets, 130 MJ in beam

LHC :

2009 first collisions, mostly at injection energy 2x450 GeV

2010 2x3.5 TeV, $\beta^* = 3.5$ m, $L_{\text{peak}} = 0.2 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ $\int L dt = 0.044 \text{ fb}^{-1}$ 368 bunches

2011 2x3.5 TeV, $\beta^* = 1.0$ m, $L_{\text{peak}} = 3.5 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ $\int L dt = 6.1 \text{ fb}^{-1}$ 1380 bunches

2012 2x4.0 TeV, $\beta^* = 0.6$ m, $L_{\text{peak}} = 7.7 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ $\int L dt = 23.3 \text{ fb}^{-1}$ 1380 bunches

2013 Pb-p run, shutdown, magnet interconnects, restart in 2015 at 2x6.5 TeV, increase #bunches

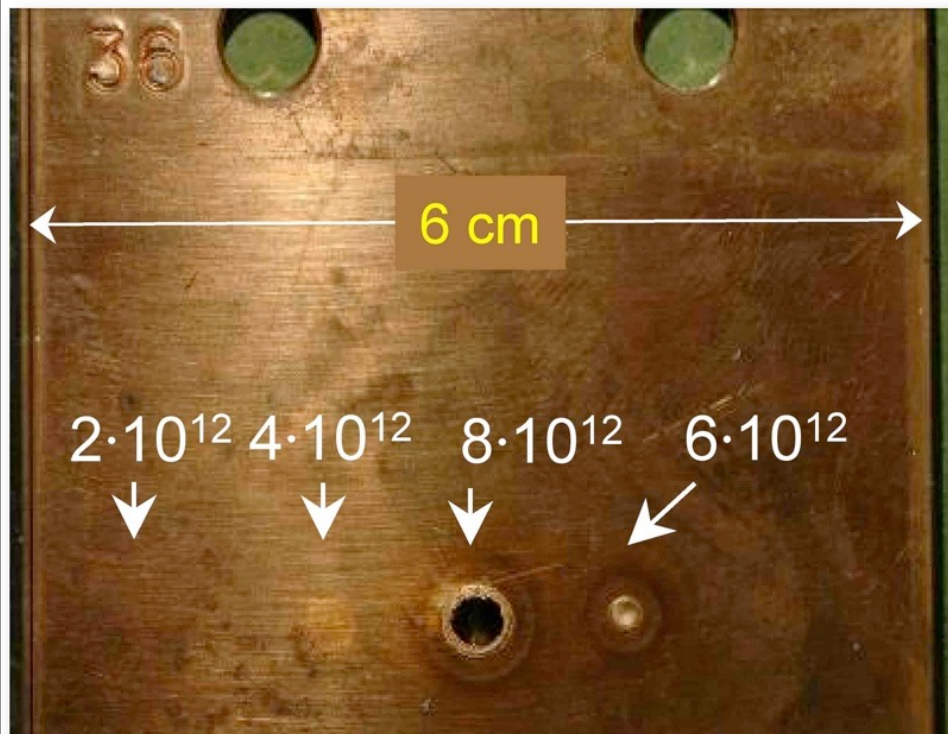
	LHC design	achieved
Momentum at collision, TeV/c	7	4
Luminosity, $\text{cm}^{-2}\text{s}^{-1}$	1.0E+34	7.7E+33
Dipole field at top energy, T	8.33	4.8
Number of bunches, each beam	2808	1380
Particles / bunch	1.15E+11	1.7E+11
Typical beam size in ring, μm	200 – 300	~300
Beam size at IP, μm	17	20

Damage potential : confirmed in controlled SPS experiment

controlled experiment with beam
extracted from SPS at 450 GeV in a single
turn, with perpendicular impact on
Cu + stainless steel target

450 GeV protons →

r.m.s. beam sizes $\sigma_{x/y} \approx 1$ mm



SPS results confirmed :

$8 \cdot 10^{12}$ clear damage

$2 \cdot 10^{12}$ below damage limit

for details see V. Kain et al., PAC 2005 [RPPE018](#)

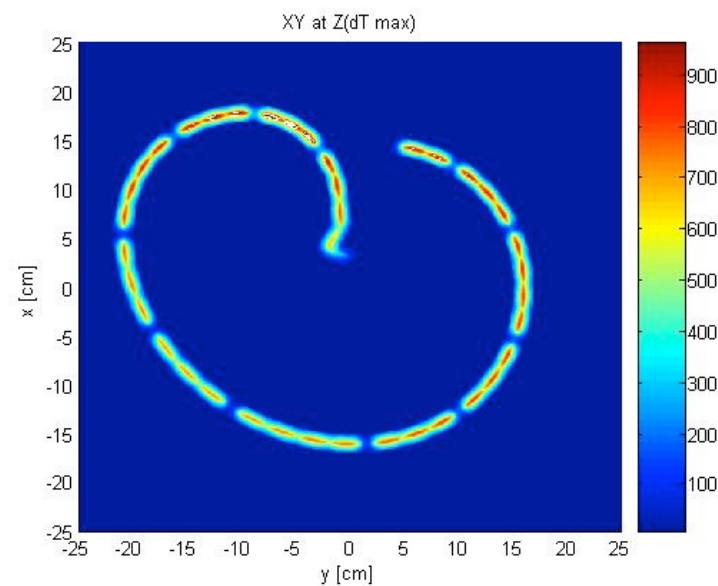
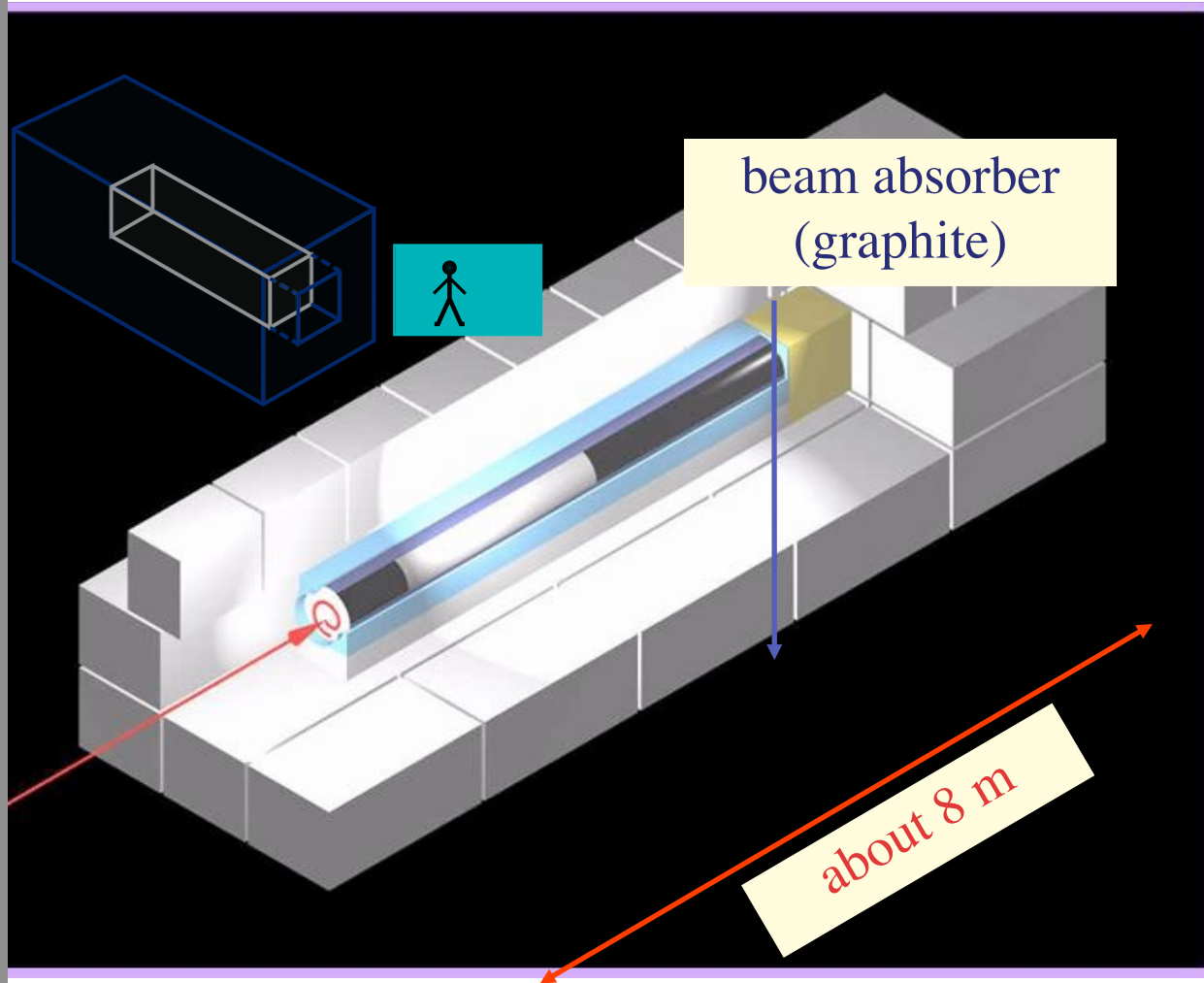
For comparison, the LHC nominal at 7 TeV :
 $2808 \times 1.15 \cdot 10^{11} = 3.2 \cdot 10^{14}$ p/beam

at $\langle \sigma_{x/y} \rangle \approx 0.2$ mm

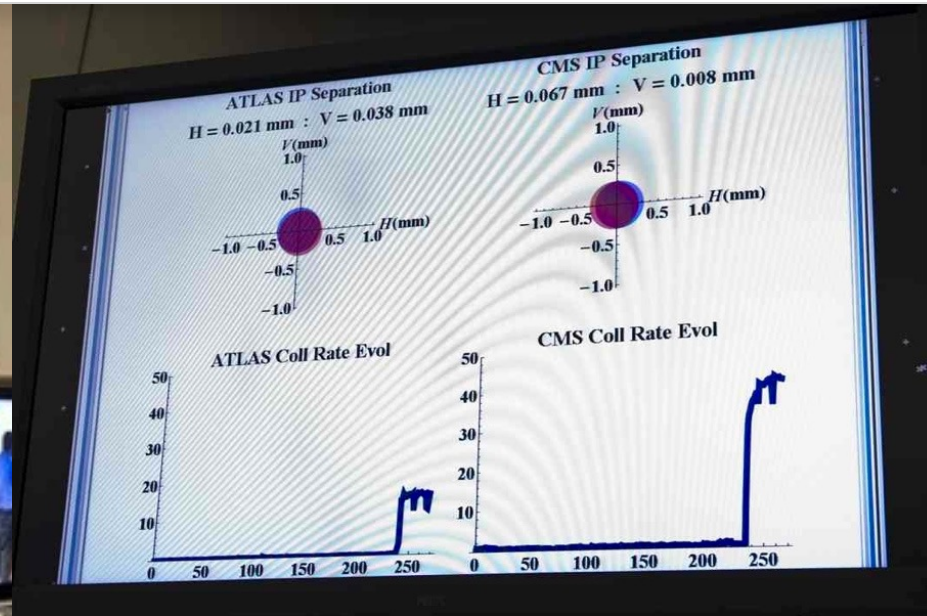
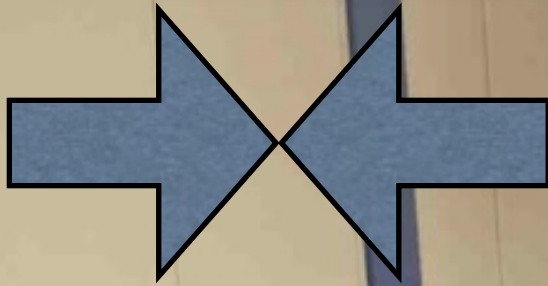
over 3 orders of magnitude above damage
level for perpendicular impact

Dumping the LHC beam

Helmut Burkhardt: Introduction to accelerators June 2013



First high energy 3.5TeV+3.5TeV collisions, 30 March 2010



LHC running very well

22-Oct-2012 01:59:26 Fill #: 3207 Energy: 4000 GeV I(B1): 2.21e+14 I(B2): 2.23e+14

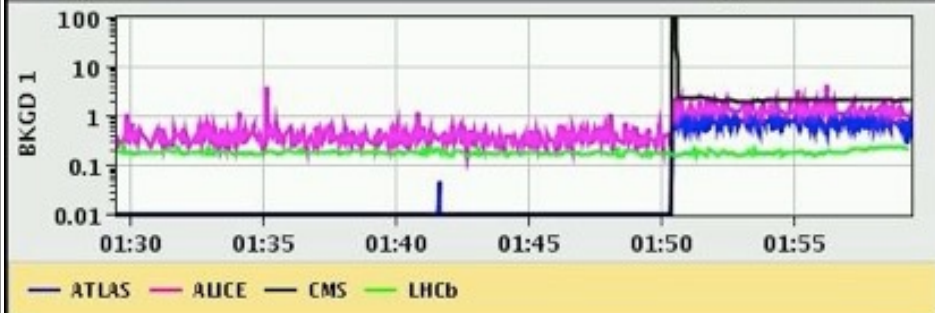
	ATLAS	ALICE	CMS	LHCb
Experiment Status	PHYSICS	STANDBY	PHYSICS	PHYSICS
Instantaneous Lumi [(ub.s) ⁻¹]	7600.9	10.005	7536.3	16.0
BRAN Luminosity [(ub.s) ⁻¹]	6752.0	6.440	6612.4	5.8
Fill Luminosity (nb) ⁻¹	0.0	0.1	548.4	1.2
BKGD 1	0.731	1.080	2.077	0.225
BKGD 2	164.623	0.000	5.492	11.078
BKGD 3	2.398	11.417	24.181	0.137

LHCb VELO Position **out** Gap: 58.0 mm STABLE BEAMS TOTEM: **STANDBY**

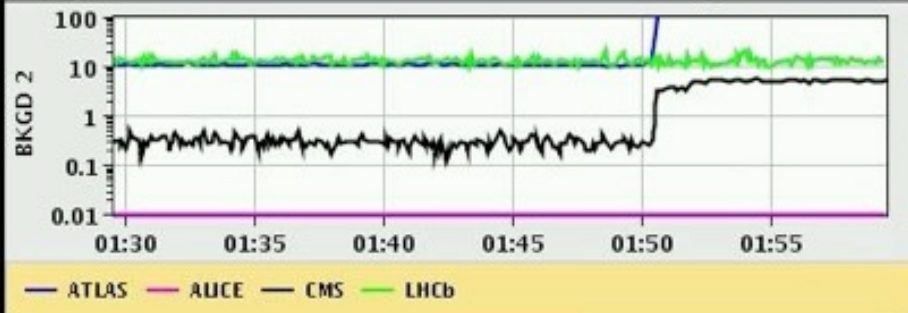
Performance over the last 24 Hrs Updated: 01:59:26



Background 1 Updated: 01:59:26

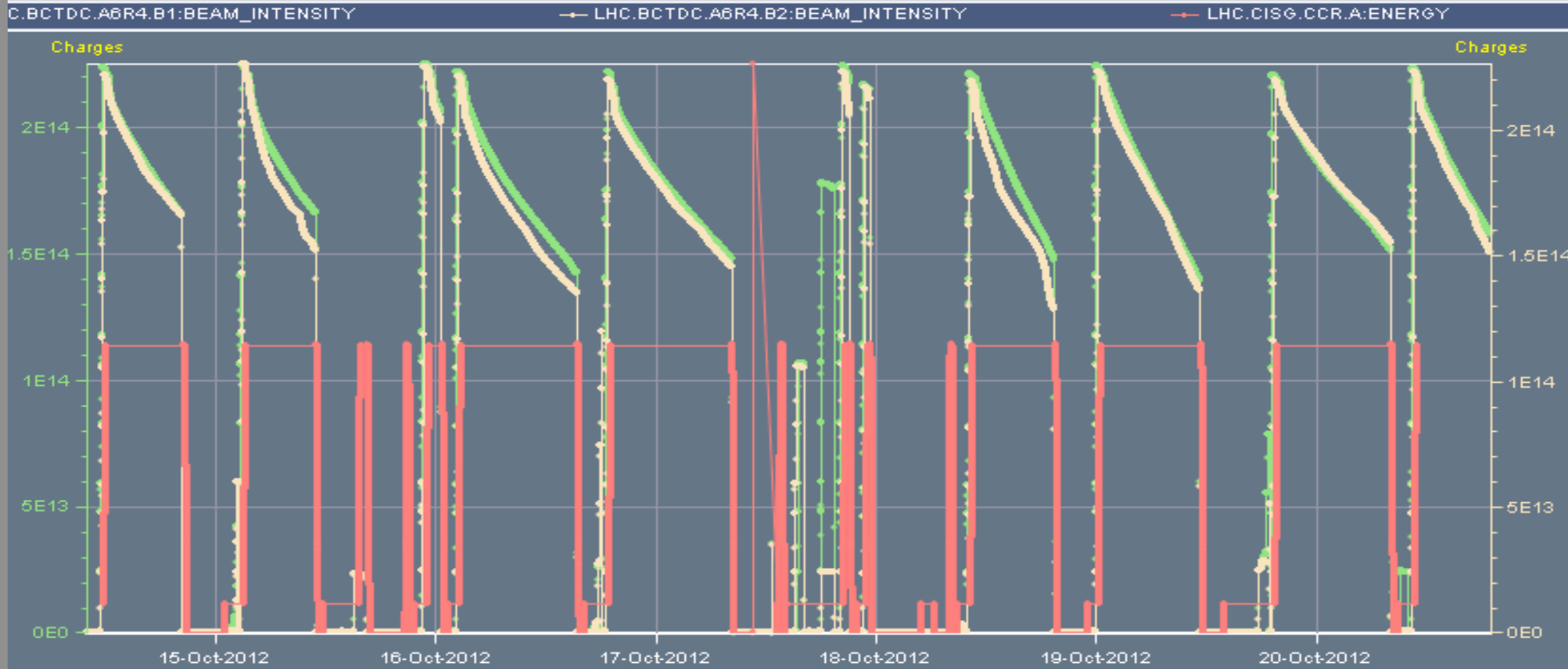


Background 2 Updated: 01:59:26

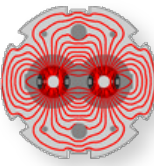


peak Luminosity $7.8 \times 10^{33} \text{cm}^{-2}\text{s}^{-1}$

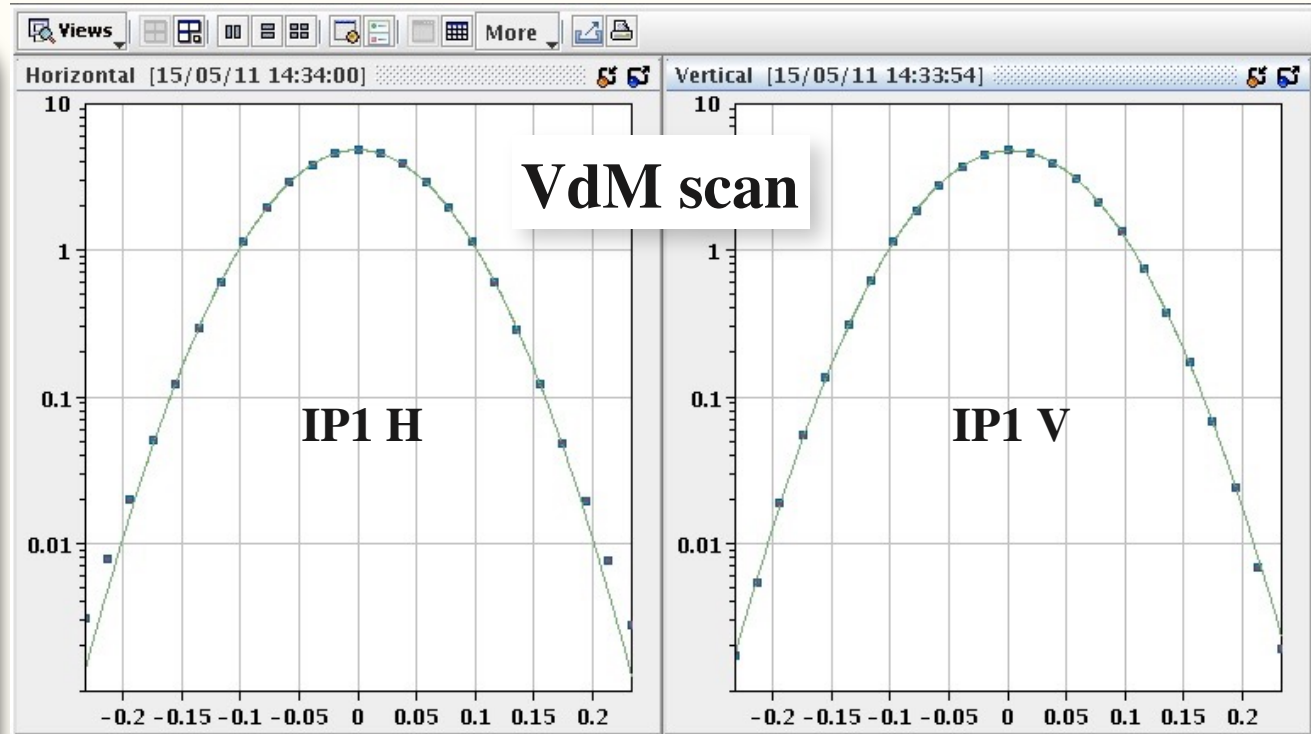
LHC typical week, Oct. '12, 1.2 pb⁻¹



Precision front - high quality of LHC beams



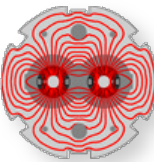
- **absolute luminosity normalization**
 - **low, well understood backgrounds**
 - **precision optics for ATLAS-ALFA and TOTEM**
- $\beta^* = 1000$ m, Oct.'12



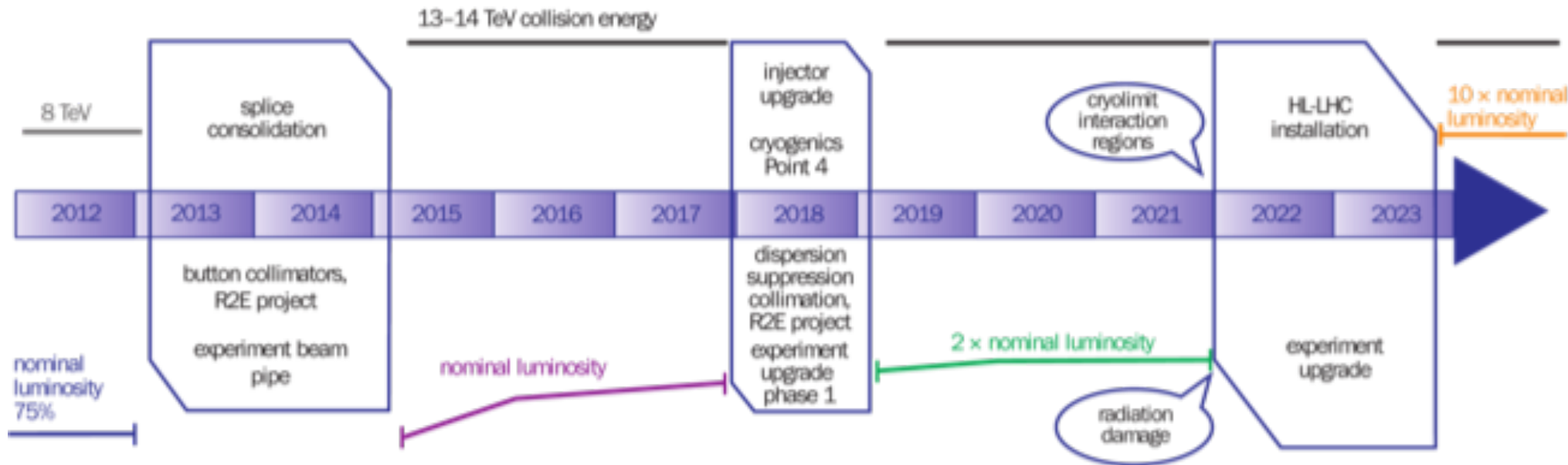
precise measurement of the luminous region + beam intensity --> absolute luminosity and cross section calibration

currently ~ 3 % level (Tevatron had ~ 15 %)

HL-LHC Timeline

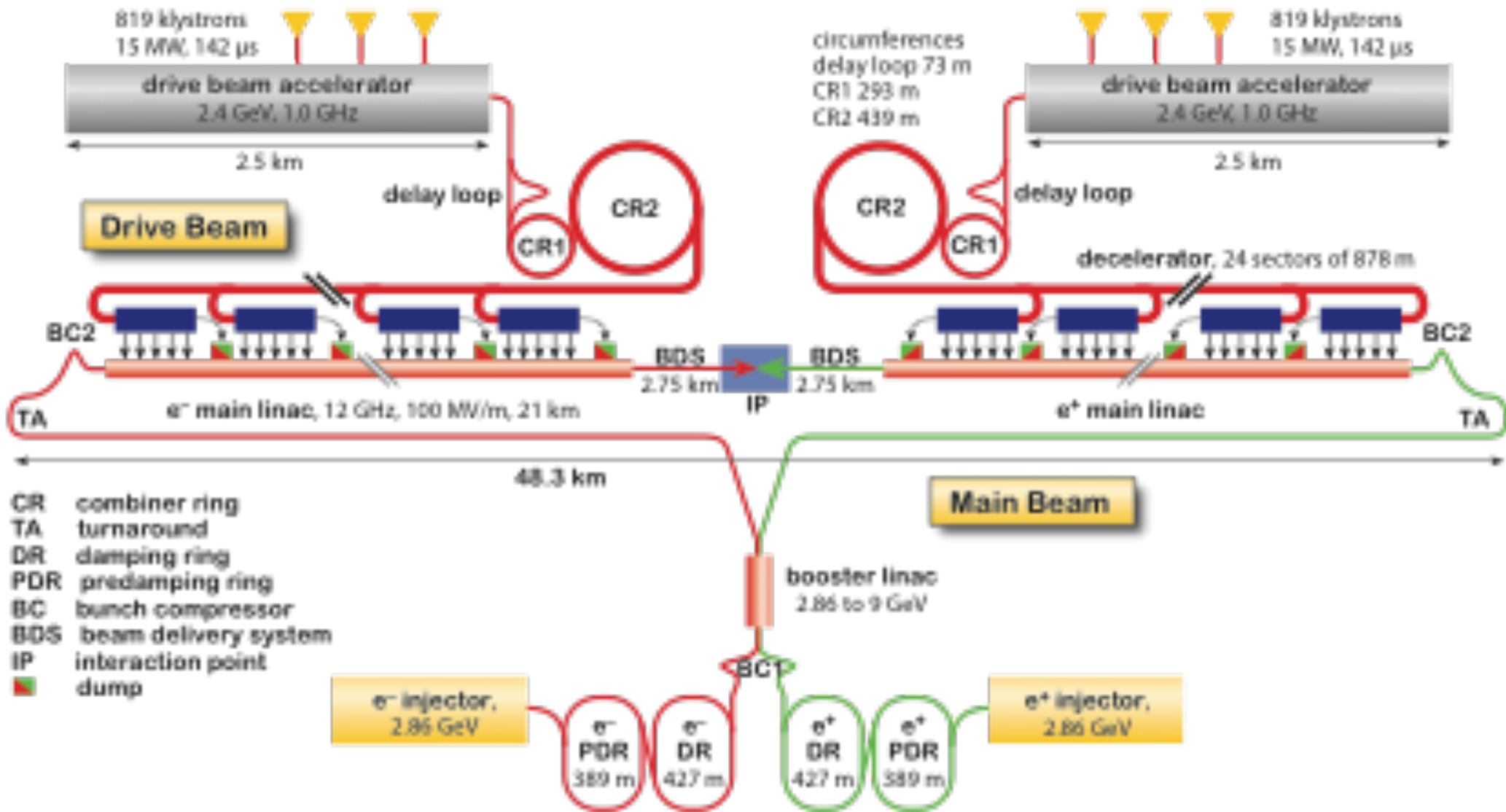


The LHC is still a rather young machine
Operation planning + upgrade studies (HL-LHC) extend to ~ 2030



Further ideas already exist (HE-LHC, LHeC, TLEP)
We also study other machines, and in particular CLIC →

CLIC



Overview of the CLIC layout at $\sqrt{s} = 3$ TeV

The machine requires only one drive beam complex for stages 1 and 2.

Accelerator applications and R&D (last slide)

- **The largest flag-ship accelerator is the LHC here at CERN**
- **By now many more accelerators outside particle physics**

#Accelerators in the world : O (30 000) mostly smaller for medical and industrial applications

- **Broad range of particle accelerator types and applications**

Large research facilities for :

Synchrotron light, UV, X-Ray (electron accelerators)

High intensity proton accelerators + neutron spallation sources

condensed matter, material science and biology research,

accelerator driven subcritical fission (energy production & radioactive waste incineration)

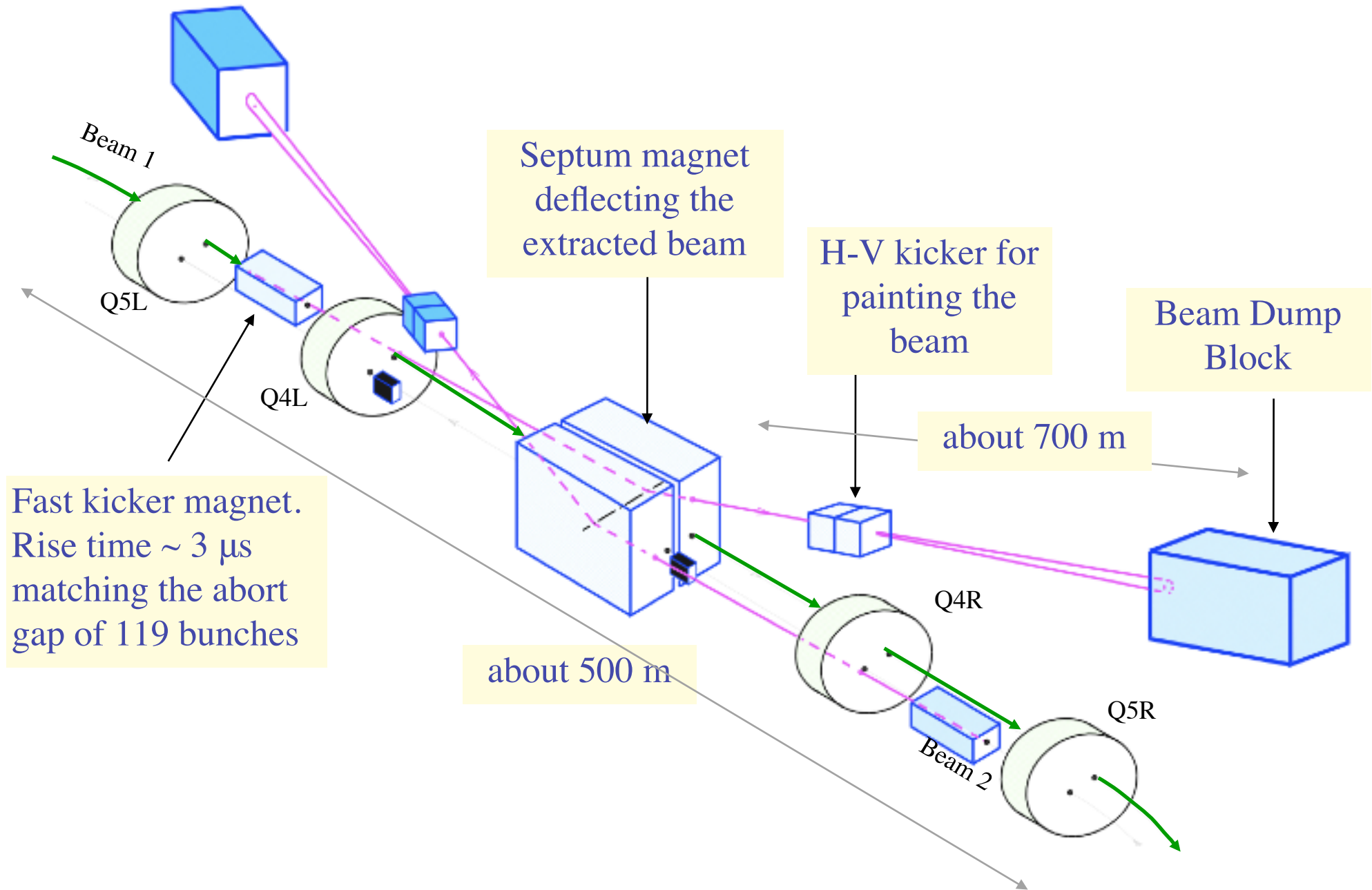
Yearly international accelerator conferences IPAC, last one in May'13 in [Shanghai](#)

Some of the hot-subjects and keywords :

- **Free electrons lasers FEL, X-FEL, Laser induced coherent SR**
- **Advanced LINACS -- including recirculation and energy recovery ERL**
- **New acceleration techniques :**
 - **Dielectric, LASER, Plasma driven**

Reserve

Schematic layout of beam dump system in IR6



Radiation of an accelerated Charge

General concept - power radiated by an accelerated charge. Relativistic version of Lamor's formula, derived by Lienard in 1898, before relativity was known.

Photon spectrum : J. Schwinger Phys. Rev. 75 (1949) pp. 1912-1925

Here written with formulas in SI units. More info + references in my paper on MC generation of [SynRad](#) CERN-OPEN-2007-018

power radiated by an accelerated charge

$$P = \frac{e^2 \gamma^2}{6\pi \epsilon_0 m^2 c^3} \left[\left(\frac{d\mathbf{p}}{dt} \right)^2 - \beta^2 \left(\frac{d\mathbf{p}}{dt} \right)^2 \right]$$

relativistic
Lamor formula

results in a major energy loss for a ring at high γ

$\mathbf{v} \perp \dot{\mathbf{v}}$

$$\left(\frac{d\mathbf{p}}{dt} \right)^2 - \beta^2 \underbrace{\left(\frac{d\mathbf{p}}{dt} \right)^2}_0 = \dot{\mathbf{p}}^2 \quad P = \frac{e^2}{6\pi \epsilon_0 m^2 c^3} \gamma^2 \dot{\mathbf{p}}^2$$

Perpendicular acceleration, B-field (or E_{\perp} field). Motion in circular machine.

$\mathbf{v} \parallel \dot{\mathbf{v}}$

$$\left(\frac{d\mathbf{p}}{dt} \right)^2 = \left(\frac{d\mathbf{p}}{dt} \right)^2 \quad \left(\frac{d\mathbf{p}}{dt} \right)^2 - \beta^2 \left(\frac{d\mathbf{p}}{dt} \right)^2 = \dot{\mathbf{p}}^2 (1 - \beta^2) = \frac{\dot{\mathbf{p}}^2}{\gamma^2}$$

$$P = \frac{e^2}{6\pi \epsilon_0 m^2 c^3} \dot{\mathbf{p}}^2$$

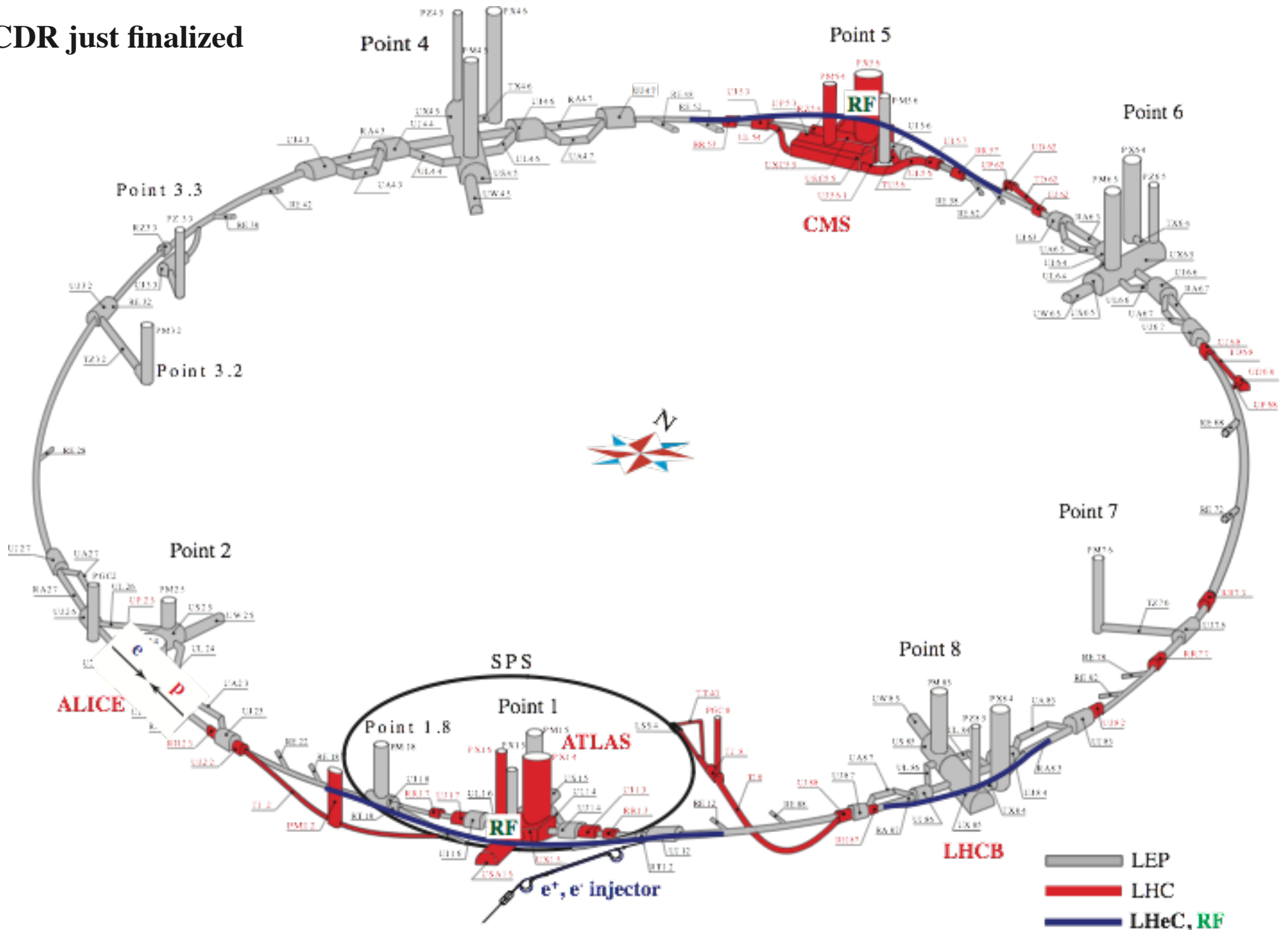
Parallel acceleration, E-field, Linac case
cancellation, $1/\gamma^2$

The energy loss for linear acceleration is very small.

Example: CLIC gradient 100 MV/m. Loss is 11 keV/s or only 0.4 eV for a 1 TeV 10 km Linac

LHeC

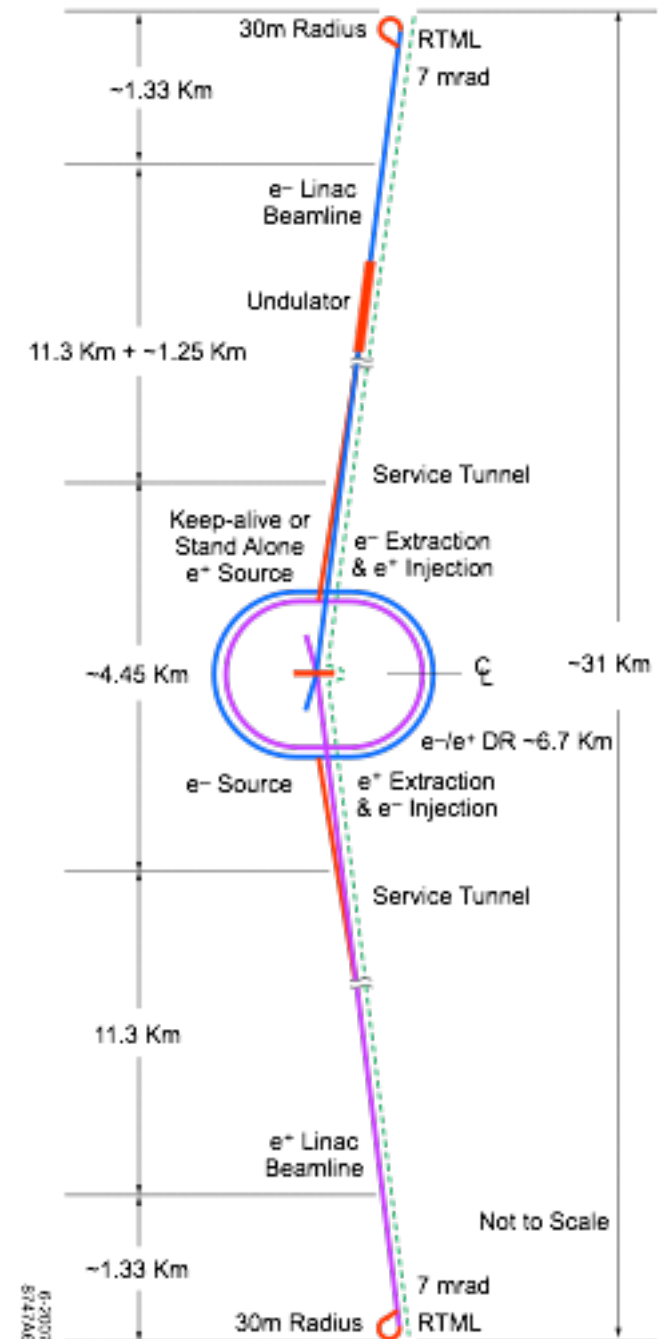
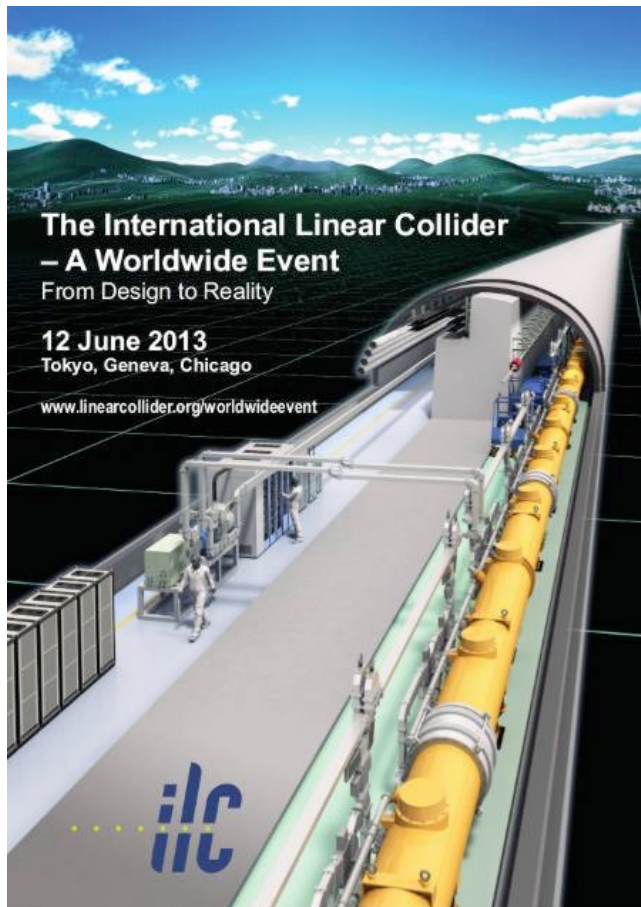
CDR just finalized



ILC

ILC TDR Handover, 12 June 2013

- 200-500 GeV centre-of-mass, 31 km long
- Luminosity: $2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
- Based on accelerating gradient of 31.5 MV/m
1.3 GHz superconducting RF

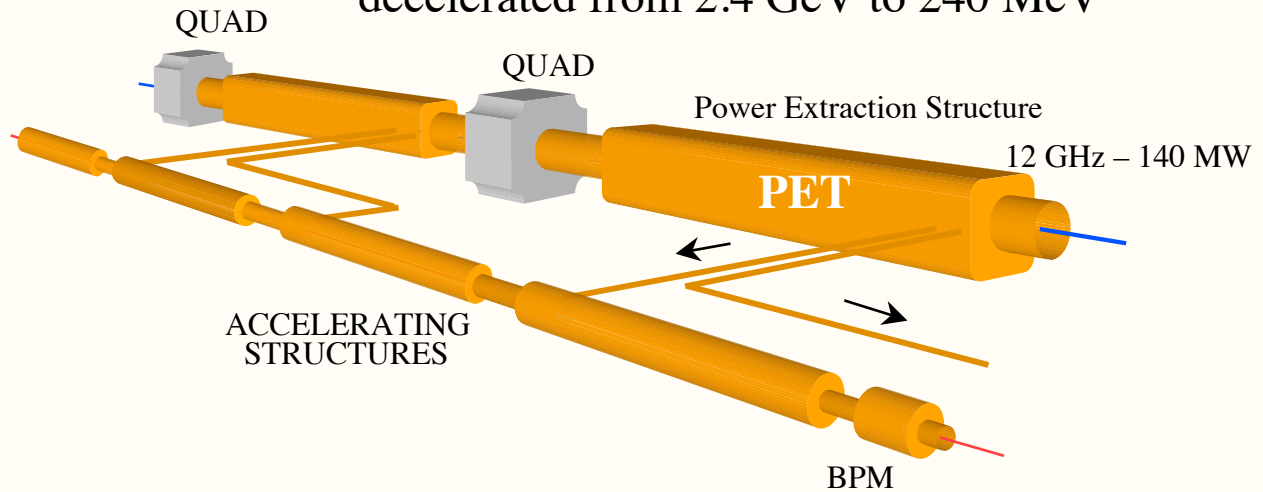


Two Beam Scheme

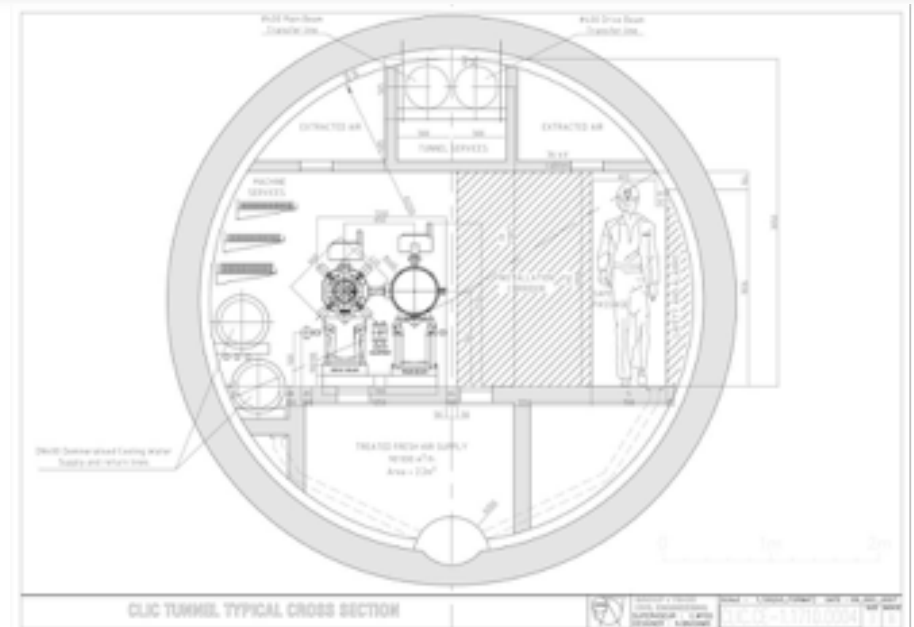
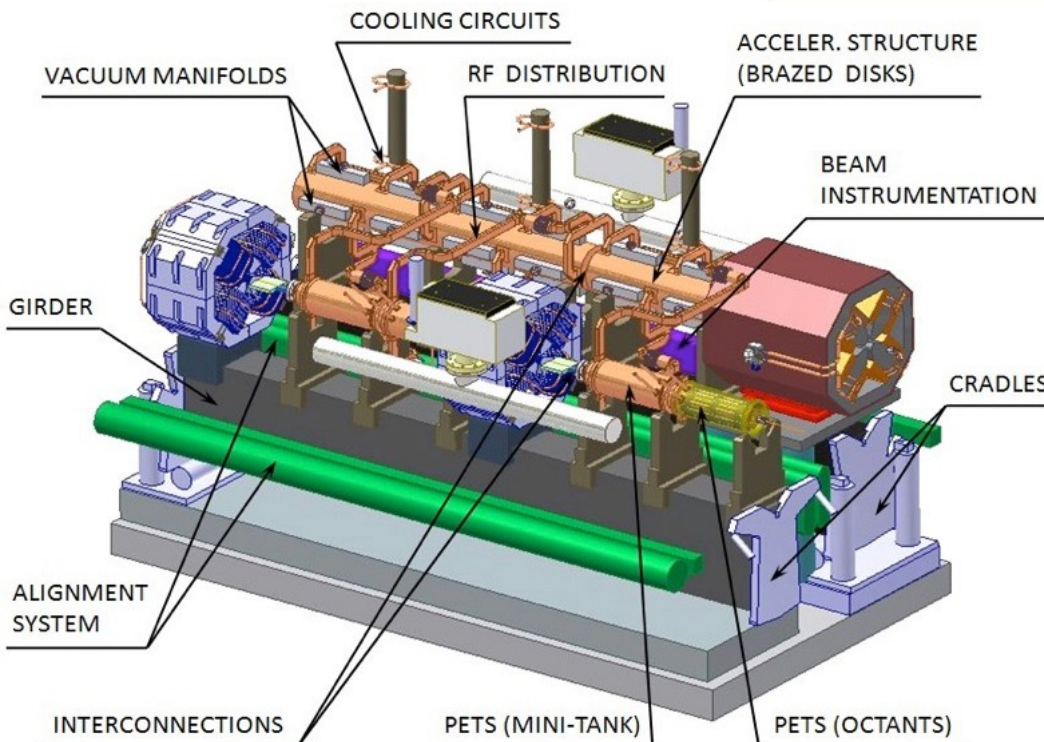
Drive Beam supplies RF power

- 12 GHz bunch structure
 - low energy (2.4 GeV - 240 MeV)
 - high current (100A)
- warm (not superconducting) RF

Drive beam - 100 A, 240 ns
decelerated from 2.4 GeV to 240 MeV



Main beam - 1.2 A, 156 ns bunch trains
accelerated from 9 GeV to 1.5 TeV



ILC and CLIC parameters

ILC: Superconducting RF

500 GeV

CLIC: normal conducting copper RF

3 TeV

accelerating gradient:

31.5 MV/m

100 MV/m

35 MV/m target

RF Peak power:

0.37 MW/m , 1.6 ms, 5 Hz

275 MW/m, 240 ns, 50 Hz

RF average power:

2.9 kW/m

3.7 kW/m

total length:

31 km

48.4 km

site power :

230 MW

392 MW

Beam structure:

particles per bunch:

20×10^9

3.7×10^9

2625 bunches / pulse of

0.96 ms

312 bunches / pulse of 156 ns

bunch spacing

369 ns

0.5 ns



The main 2013-14 LHC consolidations

1695 Openings and final reclosures of the interconnections

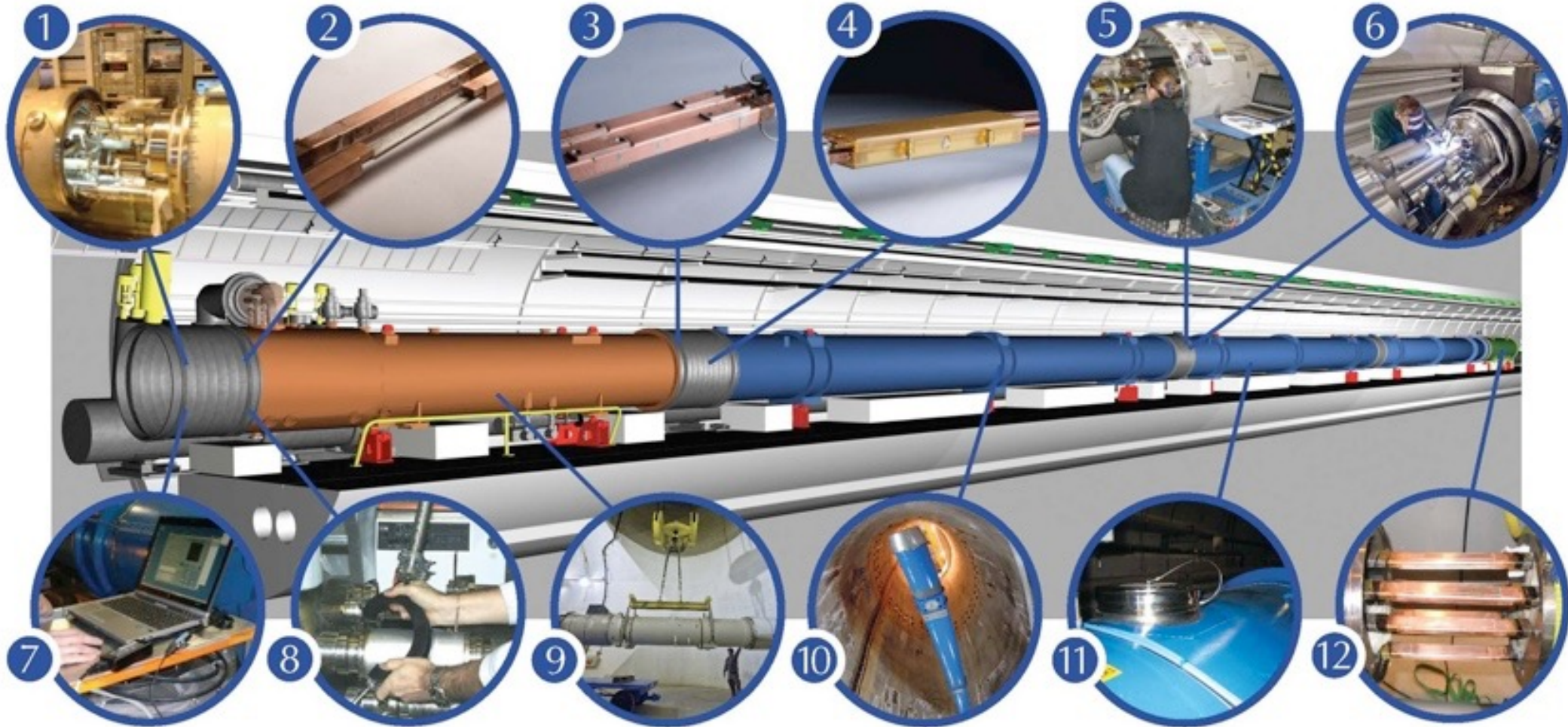
Complete reconstruction of 1500 of these splices

Consolidation of the 10170 13kA splices, installing 27 000 shunts

Installation of 5000 consolidated electrical insulation systems

300 000 electrical resistance measurements

10170 orbital welding of stainless steel lines



18 000 electrical Quality Assurance tests

10170 leak tightness tests

4 quadrupole magnets to be replaced

15 dipole magnets to be replaced

Installation of 612 pressure relief devices to bring the total to 1344

Consolidation of the 13 kA circuits in the 16 main electrical feed-boxes